

Bose-Einstein condensation (of strontium)

Cooling a gas from 10^3 K to 10^{-7} K
to study the Bose-Hubbard model

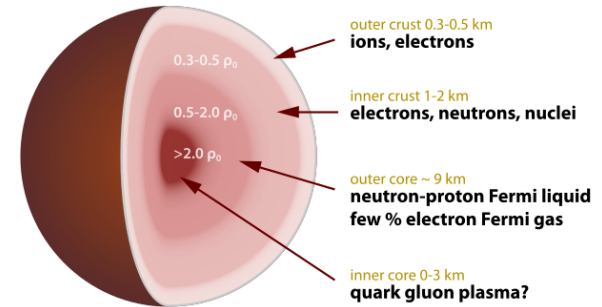
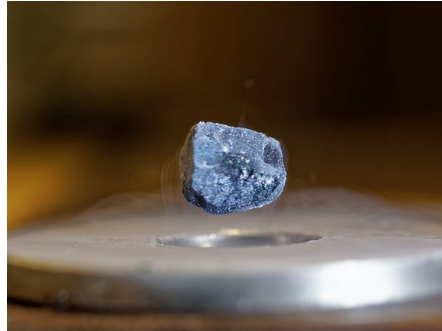
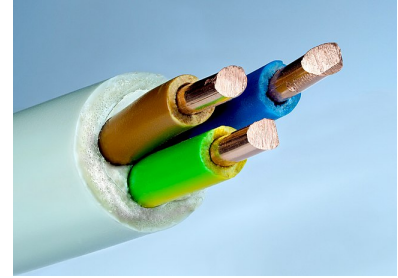
Félix Faisant

Équipe Strontium de Marc Cheneau
Groupe Gaz Quantiques
LCF, IOGS

1. **Degenerate atomic gases (as analogues?)**
2. Laser cooling
3. Evaporative cooling
4. Bose-Hubbard physics

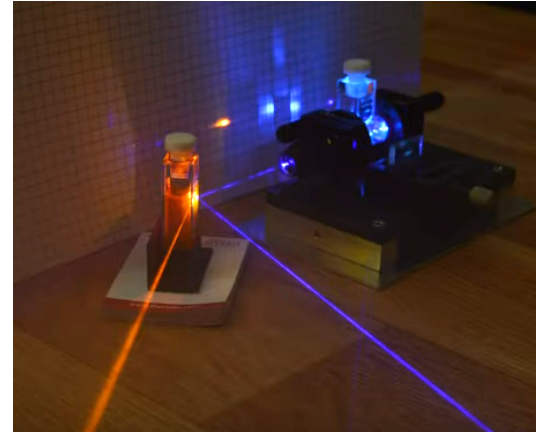
Fermions :

- Electronic matter : electrons in every material (cond-mat)
 - Metals and insulators
 - White dwarfs
 - Superconductivity
 - Magnetism... (spin systems, not really fermion gases)
- Nuclear matter : neutron stars
- $\sim$ Few-body : electron in molecules, nuclei...



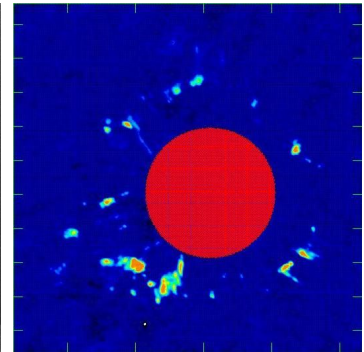
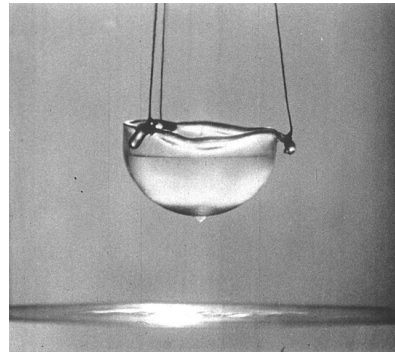
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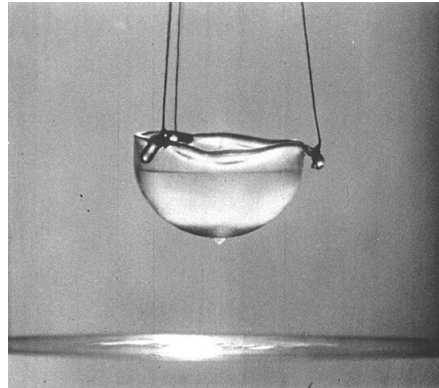
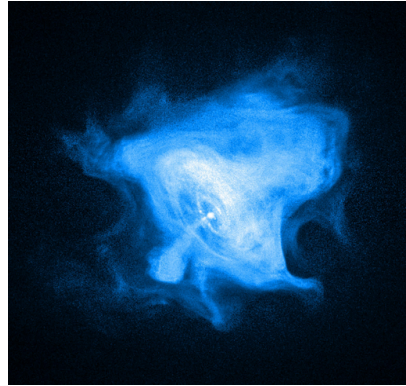
Bosons :

- Superfluid liquid ^4He
- Superluminescence/ASE & Lasers (in some sense...)



Early universe...

Either very **dense** or very “**cold**”.



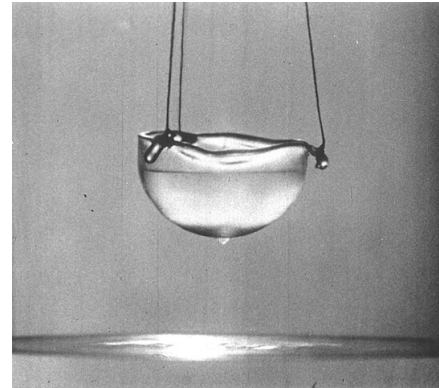
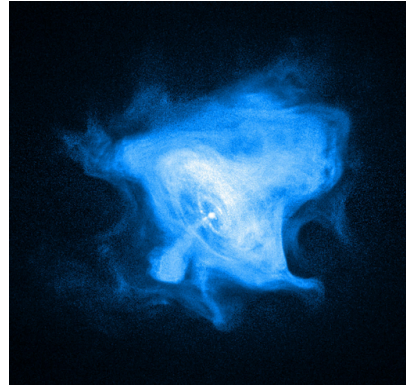
Either very **dense** or very **“cold”**.



slow-moving

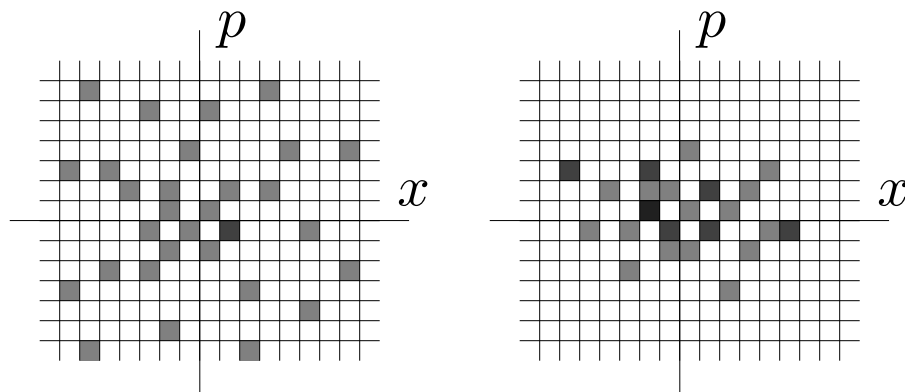


dense in
momentum space



Take N identical particles. And consider external d.o.f. only.

$$\text{phase-space density} = \frac{N}{\text{spatial volume} \times \text{momentum-space volume}} \quad (n \lambda_T^3 \text{ for a 3D gas, } \lambda_T \propto \frac{\hbar}{\sqrt{m k_B T}})$$

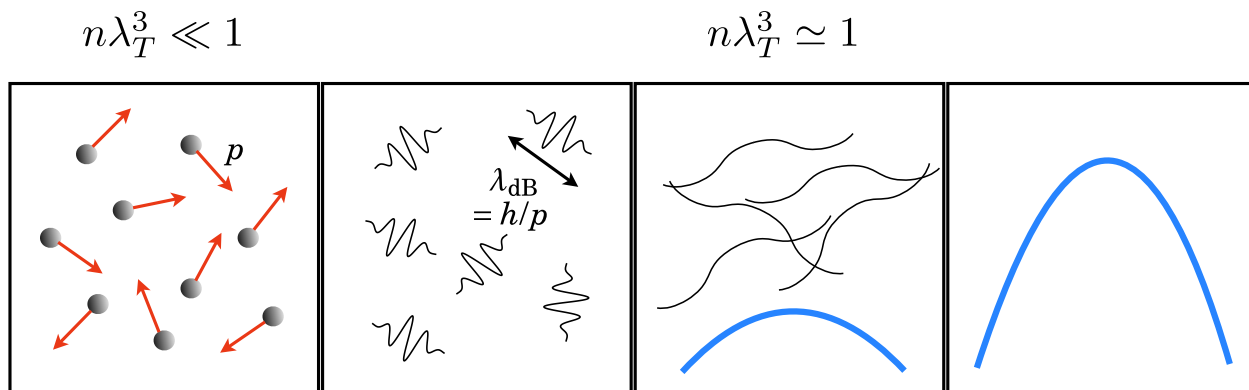


At high phase-space density (PSD $\gtrsim 1$), occupancy of some states $\nless 1$

→ quantum statistics (sym./antisym.) become important

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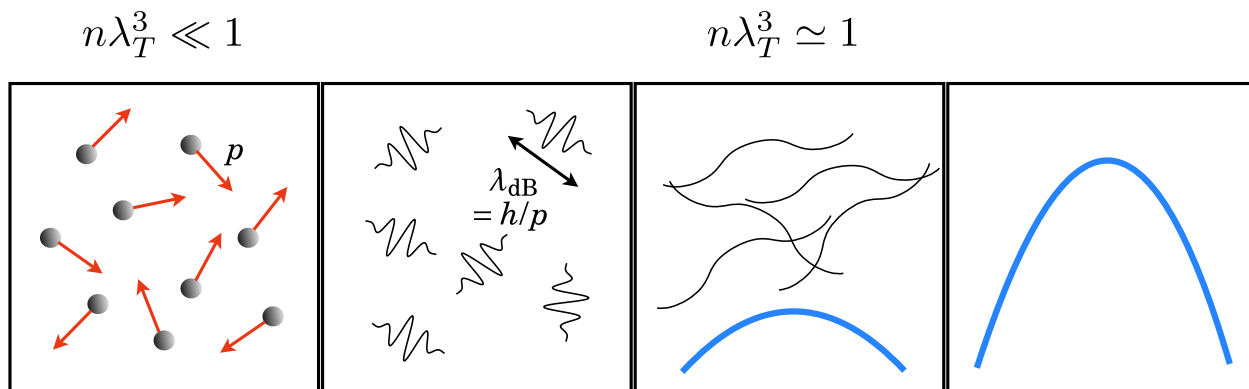


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For fermions : $n \lambda_T^3 \gg 1 \iff k_B T \ll E_F$

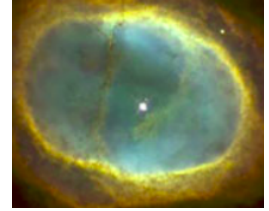
- White dwarfs :

$$n \approx 3 \cdot 10^{29} \text{ el/cm}^3$$

$$T \approx 10^7 \text{ K}$$

$$\lambda_T \approx 20 \text{ pm}$$

$$n \lambda_T^3 \approx 4 \cdot 10^3$$



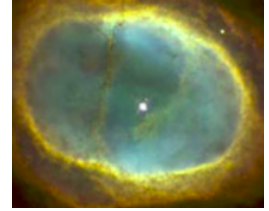
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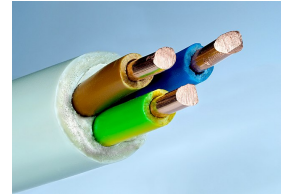
- Room-temp. solid state materials :

$$n \approx 10^{23} \text{ el/cm}^3$$

$$T = 300 \text{ K}$$

$$\lambda_T \approx 4 \text{ nm}$$

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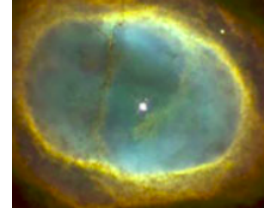
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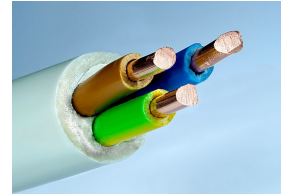
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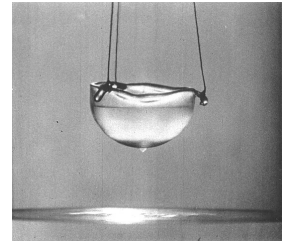
- Superfluid helium :

$$n \approx 2 \cdot 10^{22} \text{ at/cm}^3$$

$$T = 1 \text{ K}$$

$$\lambda_T \approx 1 \text{ nm}$$

$$n \lambda_T^3 \gtrsim 10$$



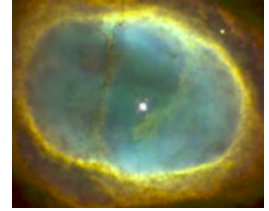
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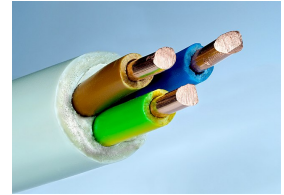
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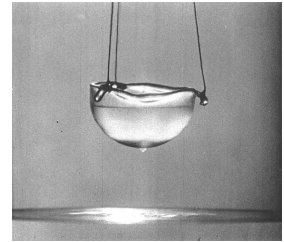
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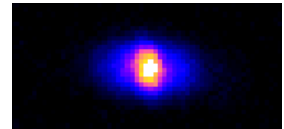
- Dilute atomic BECs :

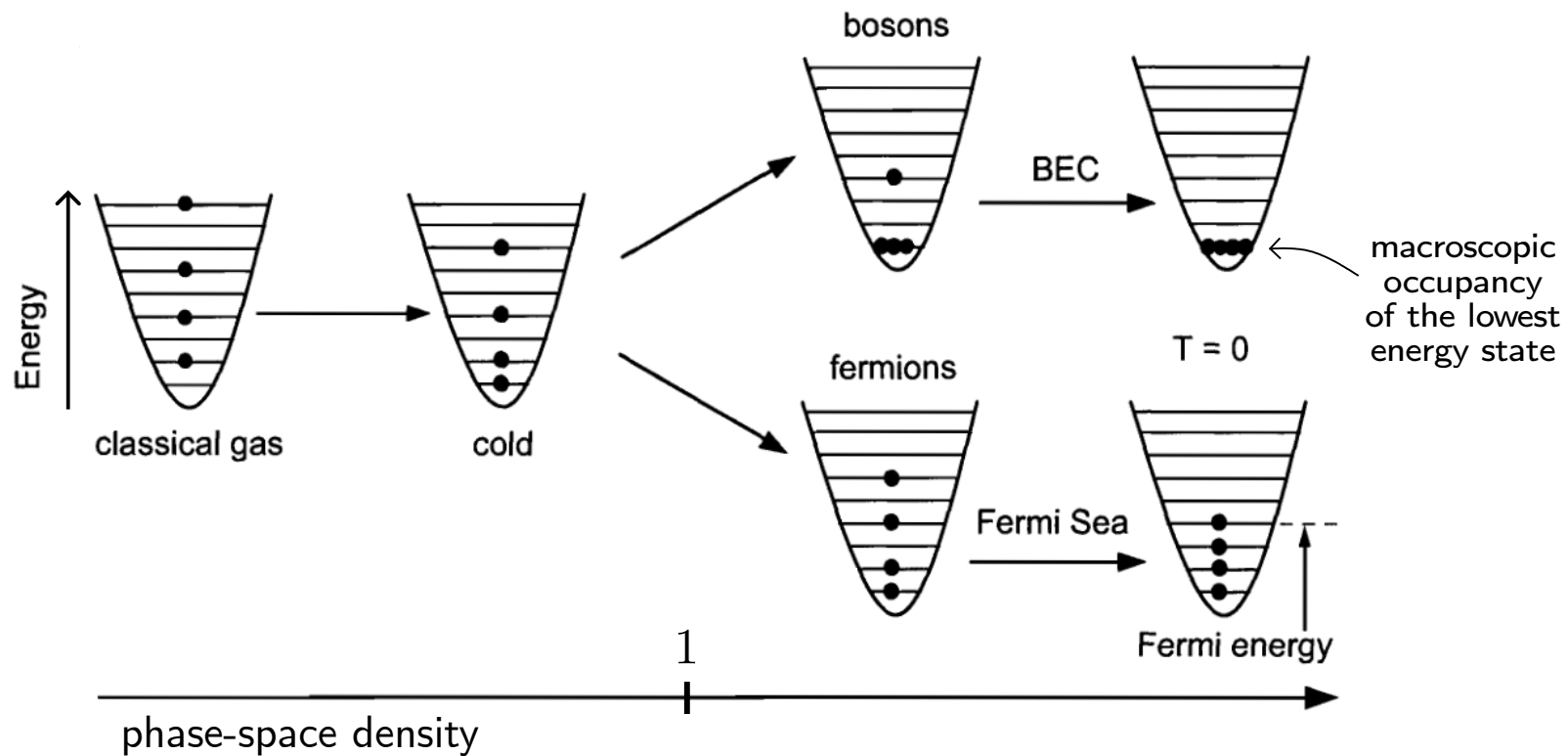
$$n \approx 10^{12 \sim 14} \text{ at/cm}^3$$

$$T \lesssim 10^{-7} \text{ K}$$

$$\lambda_T \approx 1 \mu\text{m}$$

$$n \lambda_T^3 \gtrsim 10$$

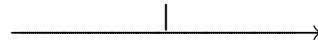






spontaneously emitted light

lasing threshold



laser light

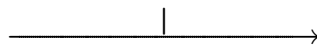
long range
coherence,
diffraction

...



spontaneously emitted light

lasing threshold



$\approx$



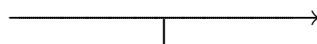
laser light

long range
coherence,
diffraction

...

thermal phase

low PSD



phase transition

$$n \lambda_T^3 = 2.612$$

(ideal 3D homogeneous)

BEC phase

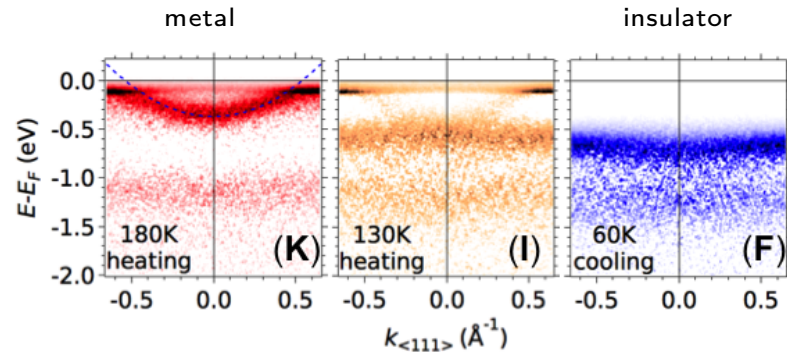
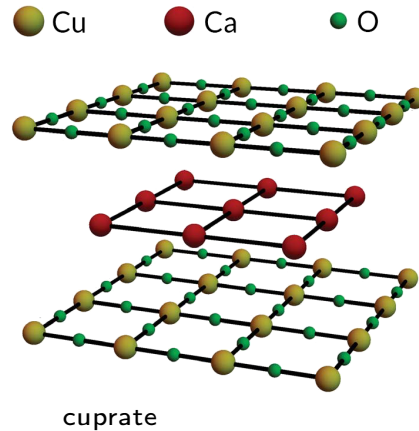
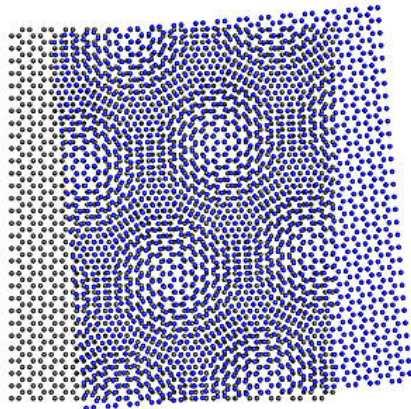
high PSD

long range
coherence,
matter wave,
superfluidity

...

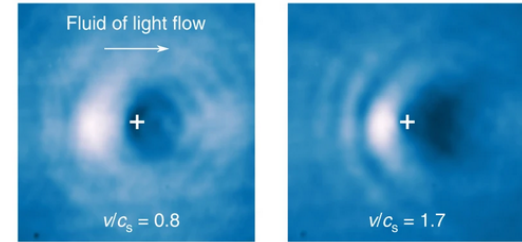
Fermions :

- Electronic matter : all modern condensed matter $\rightarrow$ new / increasingly exotic materials
 - $\rightarrow$ Exotic geom. : monolayers, nanotubes, moirés...
 - $\rightarrow$ High- T_c superconductors
 - $\rightarrow$ Highly correlated
 - $\rightarrow$ Topological; quantum Hall...
- Exotic nuclear matter

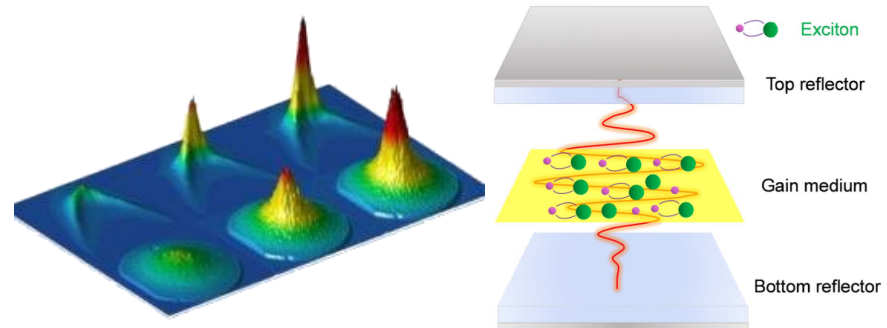
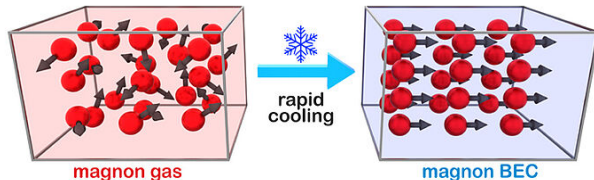


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**Bosons :**

- Fluids of light (interacting laser light)
- Polariton condensates; Exciton systems
- Magnon condensates



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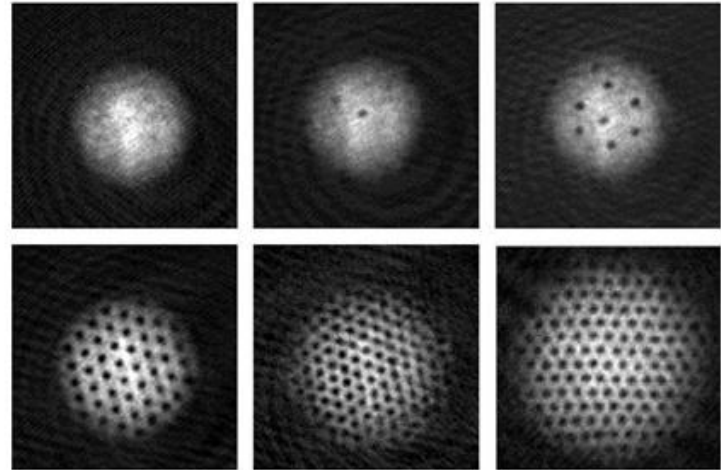
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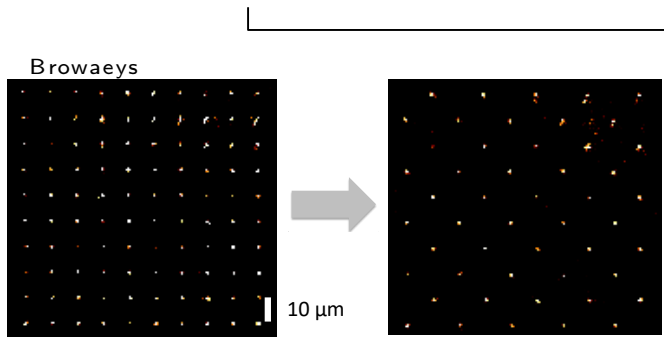
- Fluids of light (interacting laser light)
- Polariton condensates; Exciton systems
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Either or both :

- Dilute ultracold atomic gases



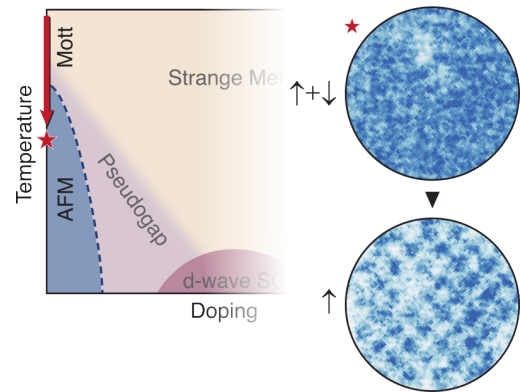
- AMO : ions; atoms or molecules in tweezer arrays or optical lattices



spin systems

Bose or Fermi(+spin) gases

- Tunable interactions
- With or without internal DoF
- Particule-resolved



Greiner 2017

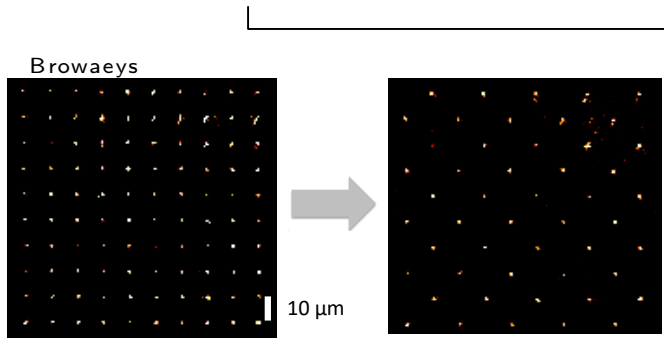
$$H = J \sum_{\langle i,j \rangle} \sigma_i \sigma_j \quad \text{Ising}$$

XY model

...

Harder : Heisenberg...

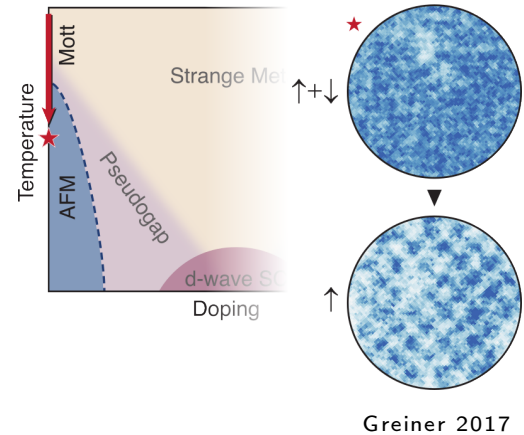
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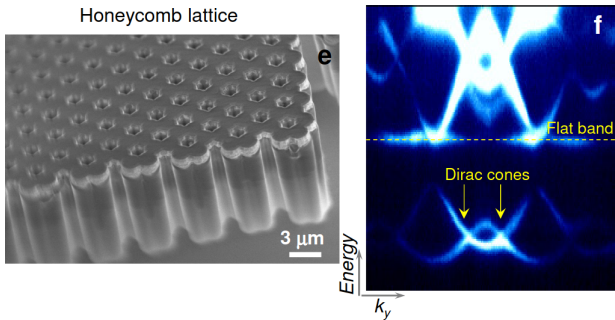
spin systems

Bose or Fermi(+spin) gases

- Tunable interactions
- With or without internal DoF
- Particule-resolved



- Fluids of light. Polariton/electron-photon systems

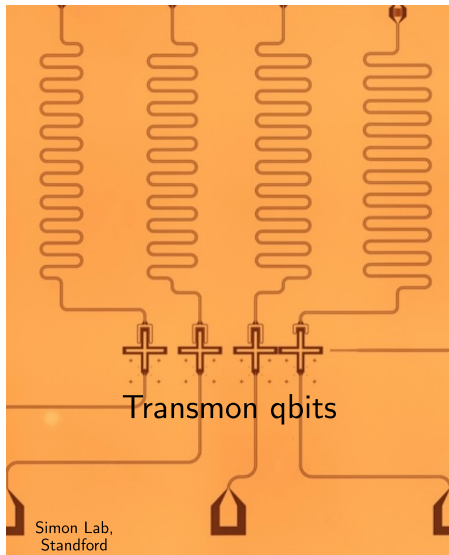


review: [arXiv:2306.07313](https://arxiv.org/abs/2306.07313)

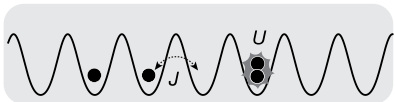
Fake graphene more controllable than true graphene ?

Polariton lattices for quantum simulation
A. Amo

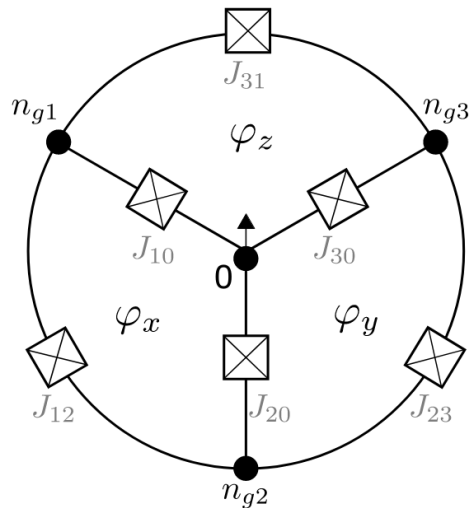
- Superconducting quantum circuits (eg. transmon qubits arrays)



Coherent Bose-Hubbard chain



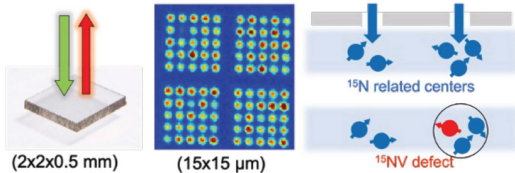
arXiv:1807.11342, Simon/Schuster



arXiv:2008.13758, LPMC, Polytechnique

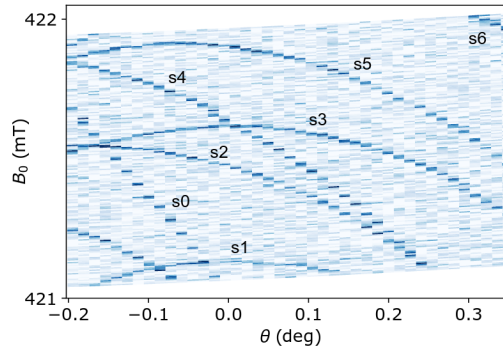
- Superconducting quantum circuits (eg. transmon qubits arrays)
- Spins in solids (NV centers, RE-doped crystals, spin chains; NMR/ESR-controlled)

Experimental system: single NV center coupled to individual electron-nuclear spin defects ($S = 1/2$, $I = 1/2$)



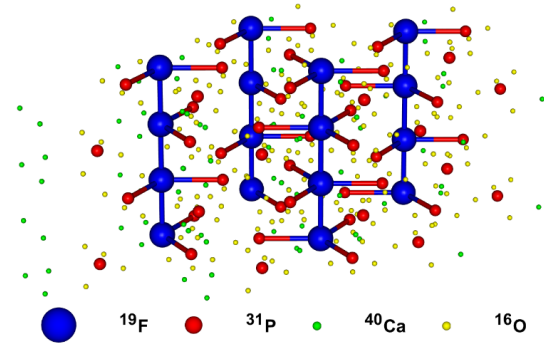
- N15 implanted through aperture array
- Mean NV center depth ~ 20 nm
- Mean nitrogen-related defect distance ~ 17 nm

P. Cappellaro group



arXiv:2301.02653

E. Flurin, Quantronics group @ CEA

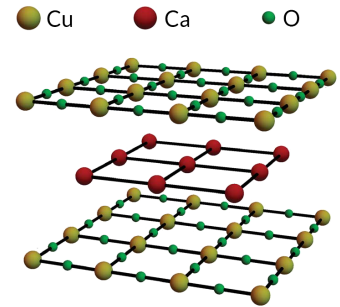


arXiv:2303.10238

P. Cappellaro group

- Superconducting quantum circuits (eg. transmon qubits arrays)
- Spins in solids (NV centers, RE-doped crystals, spin chains; NMR/ESR-controlled)
- Photonic circuits
- ...

Hard-to-study quantum system

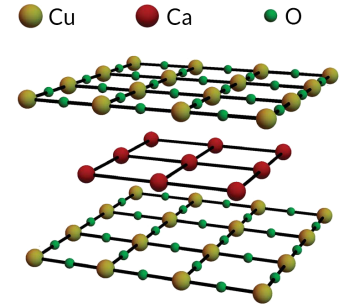
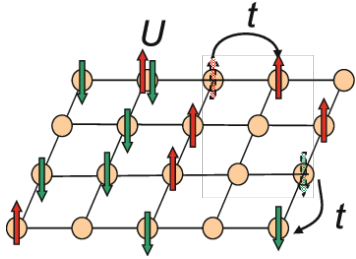


Hard-to-study quantum system



Some model :

$$\mathbf{H} = -t \sum_{\langle i,j \rangle, \sigma} \mathbf{c}_{i\sigma}^\dagger \mathbf{c}_{j\sigma} + \text{h.c.} + U \sum_i \mathbf{n}_{i\uparrow} \mathbf{n}_{i\downarrow}$$

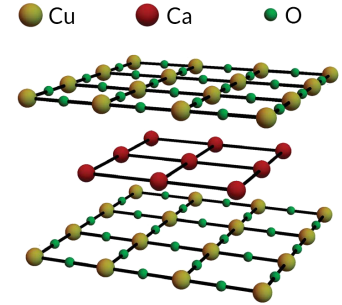
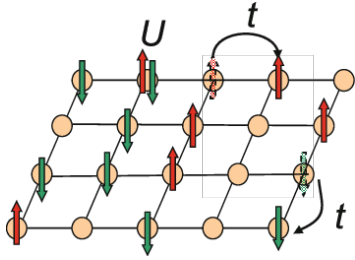


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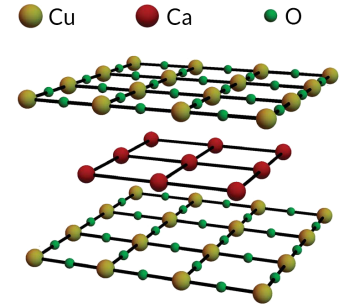
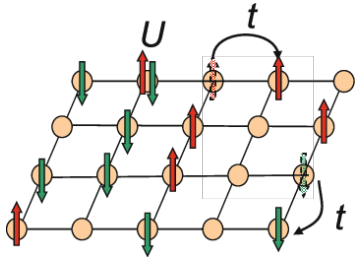


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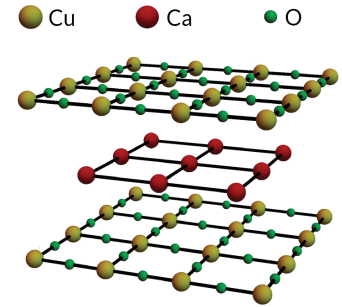
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hard or approximative



Hard-to-study quantum system

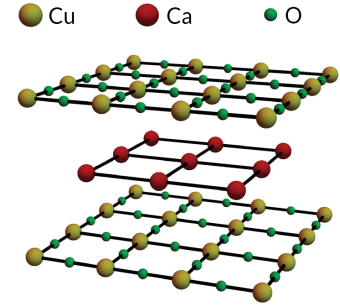
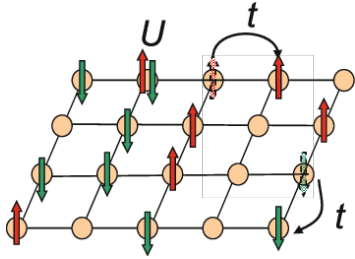


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Hard-to-study quantum system

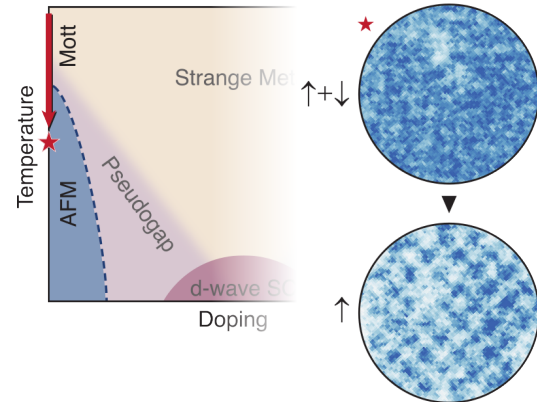
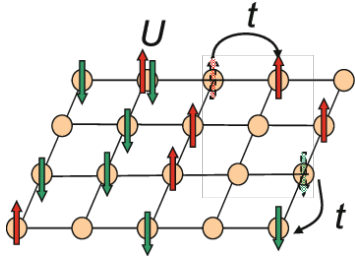
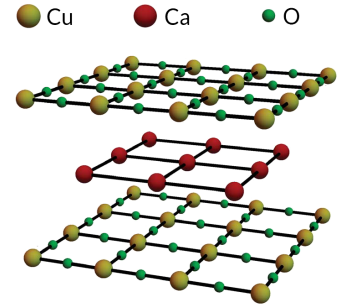


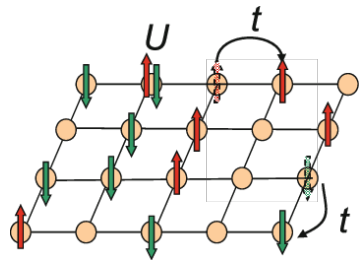
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Implementation
with a controllable
and easy-to-study quantum system





Hard-to-study quantum system

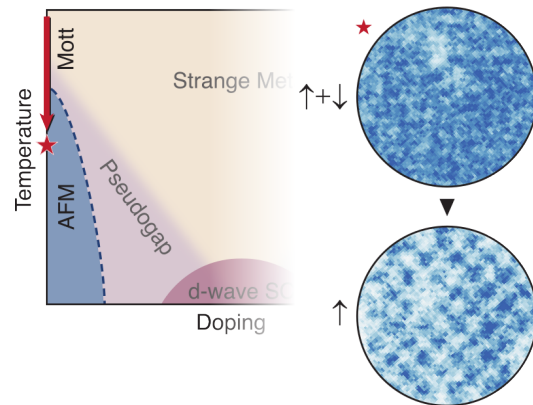
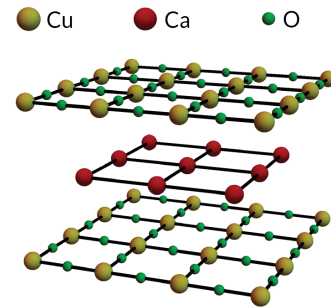


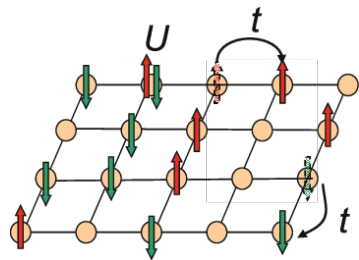
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Hard-to-study quantum system



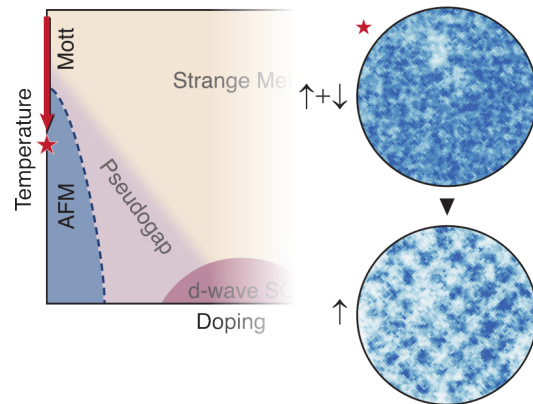
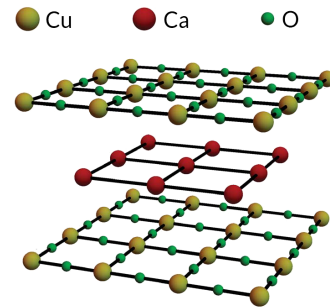
approximate
mapping

Some **simplified** model :

$$H = -t \sum_{\langle i,j \rangle, \sigma} c_{i\sigma}^\dagger c_{j\sigma} + \text{h.c.} + U \sum_i n_{i\uparrow} n_{i\downarrow}$$



Inexact implementation
with a $\sim$ controllable
and easy-to-study quantum system



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- Despite the difficulties, numerical simulation advances *fast* ← more computing power,
better models & approximations

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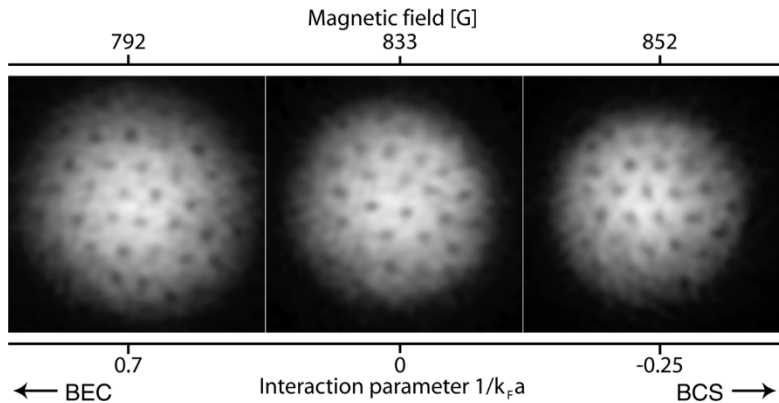
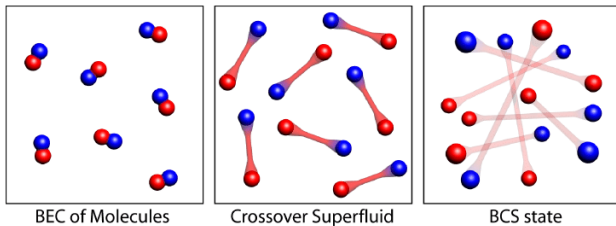
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- Fundamentally, quantum simulation scales better than classical computing.
- Condensed matter physics can advance without quantum simulators.

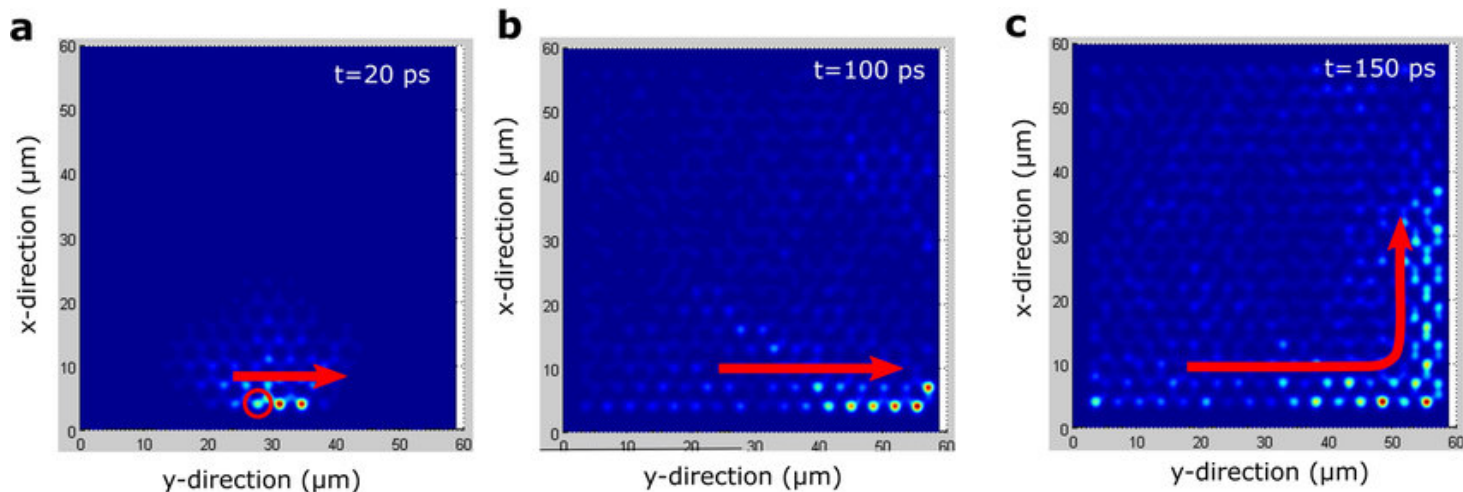
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 - Superfluidity of degen. Fermi gases, even with very strong interactions



Vortices and Superfluidity in a Strongly Interacting Fermi Gas,
Zwierlein et al.

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 - Preparation of topological states & detection of edge states/modes



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 - ...
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- Stimulates the theory
- Anyways, should we need such motivation ?

“Natural next step” :

- Control all d.o.f. of individual particles
- Isolate particles
- Control interactions $\rightarrow$ arbitrary and non-local

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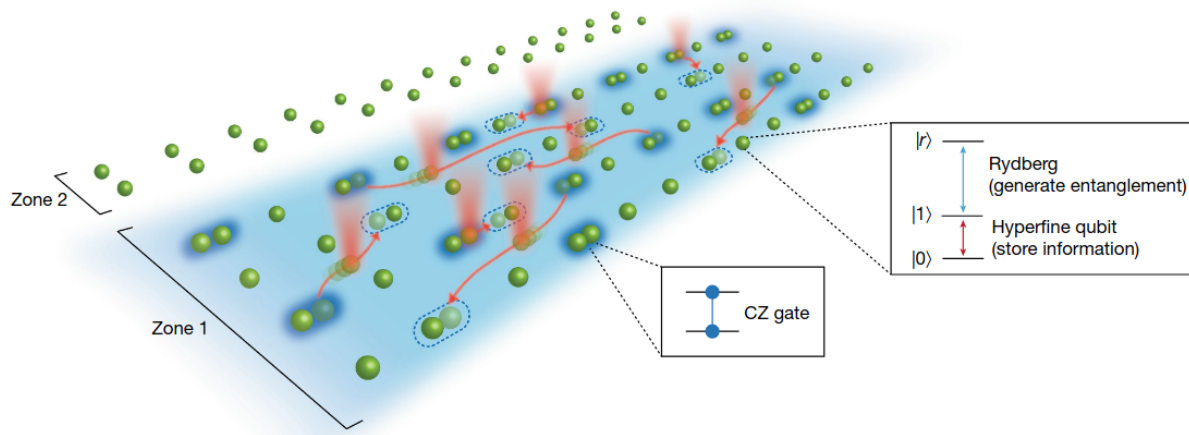
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$\rightarrow$ Implement arbitrary quantum circuits / programs

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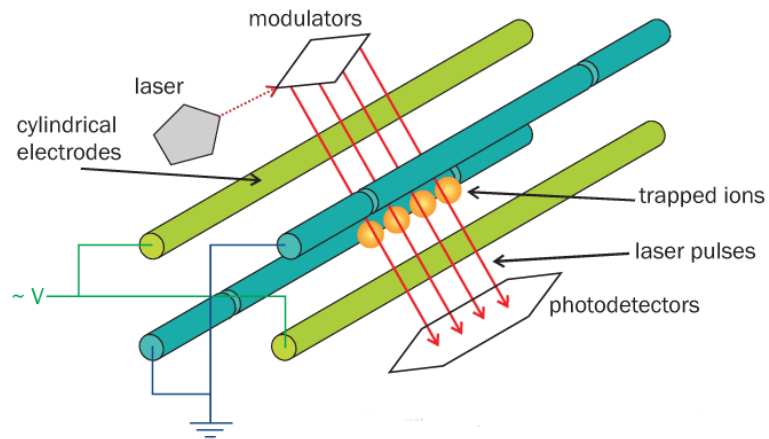
Attempts on many platforms :



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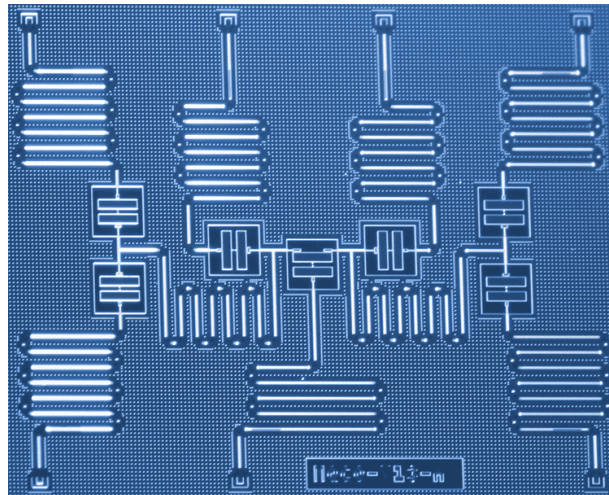
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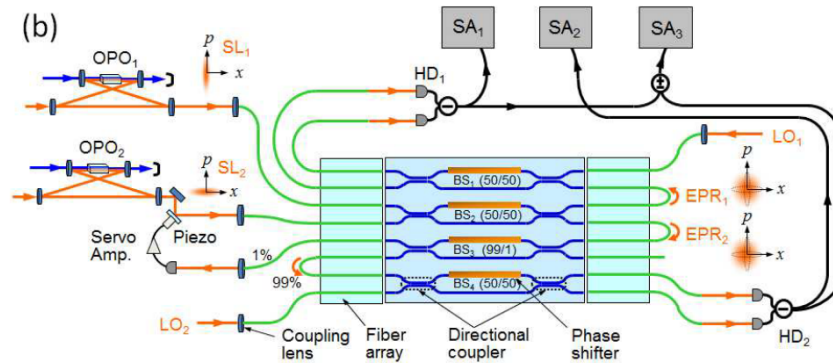
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Attempts on many platforms :



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Discrete-variable or continuous-variable quantum optics



“Natural next step” :

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Hard

“Natural next step” :

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Hard $\propto e^N$

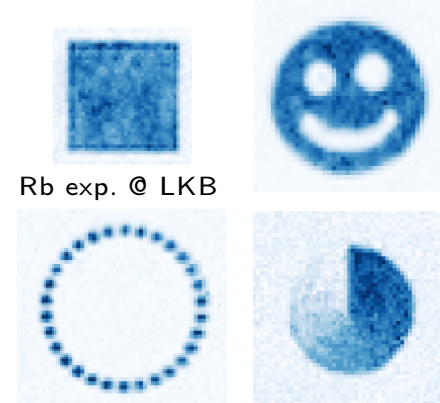
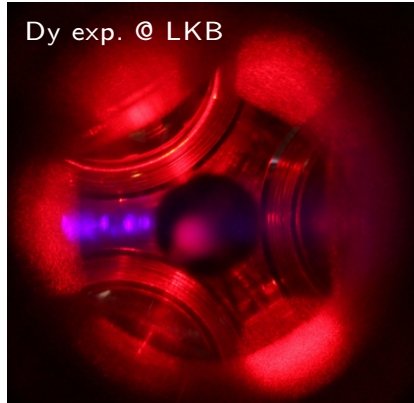
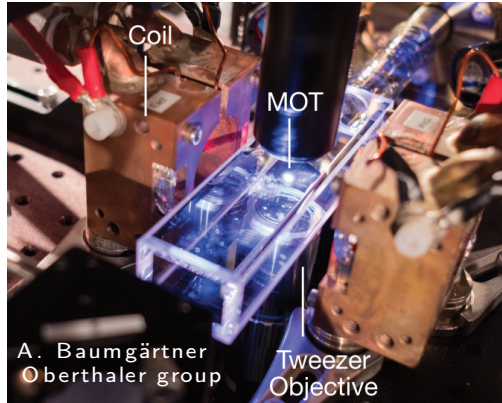
“Le problème à N corps qui se cache derrière l'ordinateur quantique”,
Xavier Waintal, Reflets de la Physique n° 70

L'ordinateur quantique est une belle aventure mais, on le comprend, il est difficile de prédire à quoi va aboutir cet effort inédit pour créer et utiliser des états quantiques macroscopiques. L'auteur peine à envisager que l'on puisse parvenir à l'ordinateur quantique de type #4 sans des ruptures conceptuelles majeures avec les approches suivies actuellement. L'ordinateur quantique souffre par ailleurs d'une différence

Difficulté	Type d'ordinateur quantique	Exemples d'applications
#1	Ordinateur analogique sans portes	Simulations quantiques
#2	Ordinateur analogique à portes, basse fidélité	Validation du système. « Suprématie quantique »
#3	Ordinateur analogique à portes, haute fidélité	Calculs variationnels de chimie quantique
#4	Ordinateur digitalisé sans mémoire quantique (calculs quasi déterministes)	Factorisation de nombres premiers Calculs exacts de chimie quantique
#5	Ordinateur digitalisé avec mémoire quantique	Intelligence artificielle, algèbre linéaire

Tableau 1. Différents types d'ordinateurs quantiques et les applications qui peuvent être envisagées.

Particles = neutral atoms in a dilute gas.

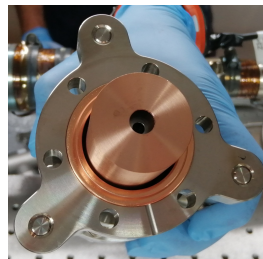


Nature's gift for controllable quantum matter :

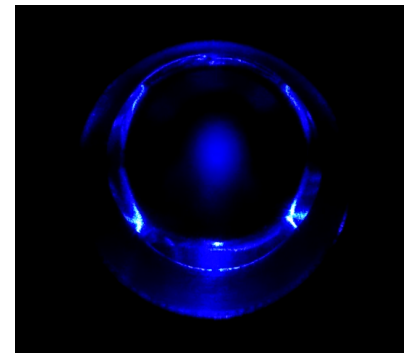
- identical particles
- stable (if dilute enough) & at equilibrium
- controllable by light, internal structure simple enough but useful enough
- can be trapped in $\pm$ arbitrary potentials (optical dipole traps / optical tweezers)
- can be cooled to degeneracy



Solid



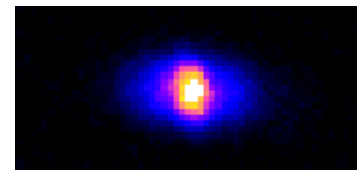
Oven



Vapor, 800 K

very low phase-space density

Cooling ↓ Compression

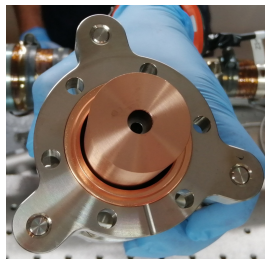


BEC, 10^{-7} K

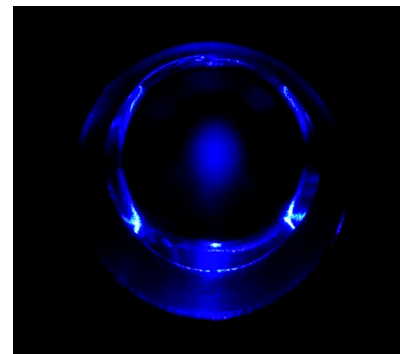
degenerate atomic gas



Solid



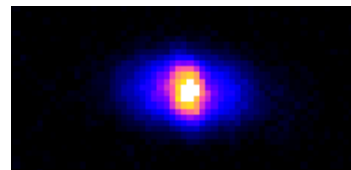
Oven



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BEC, 10^{-7} K

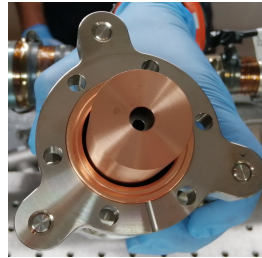
degenerate atomic gas

Timescales

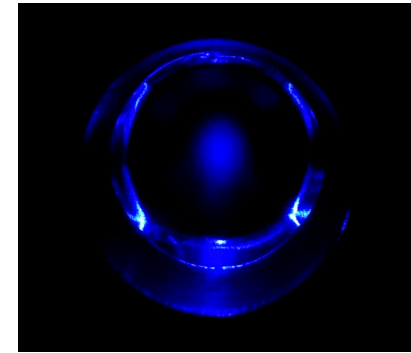
light-atom interaction	ns $\sim$ μ s
motion & atom-atom interact.	μ s $\sim$ ms $\sim$ s



Solid



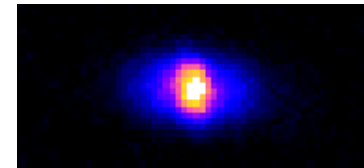
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BEC, 10^{-7} K

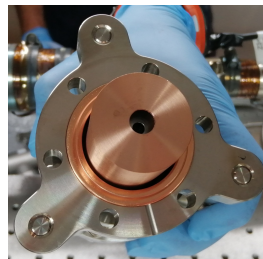
degenerate atomic gas

Timescales

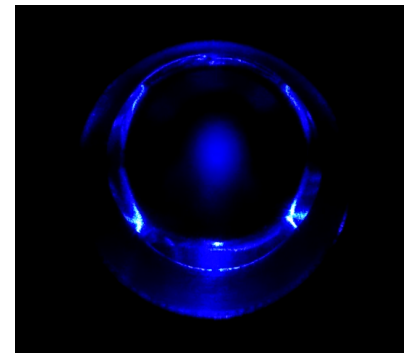
light-atom interaction	ns $\sim$ μ s
motion & atom-atom interact.	μ s $\sim$ ms $\sim$ s
degen. gas production	few s
gas lifetime	1 s $\sim$ min.



Solid



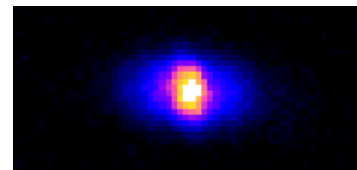
Oven



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Cooling ↓ Compression



BEC, 10^{-7} K

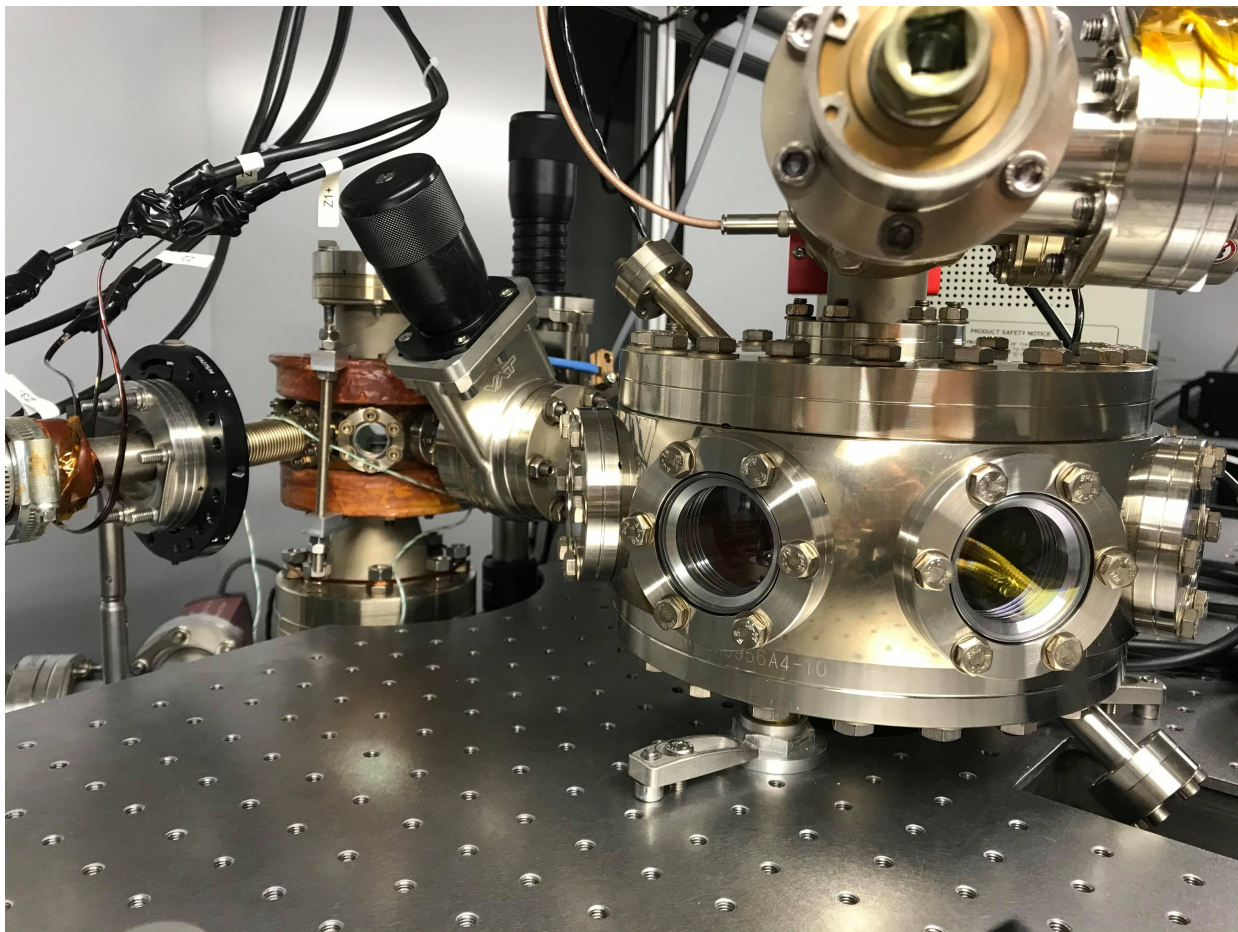
degenerate atomic gas

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3 b.
recomb.

~~2 body
inel.~~

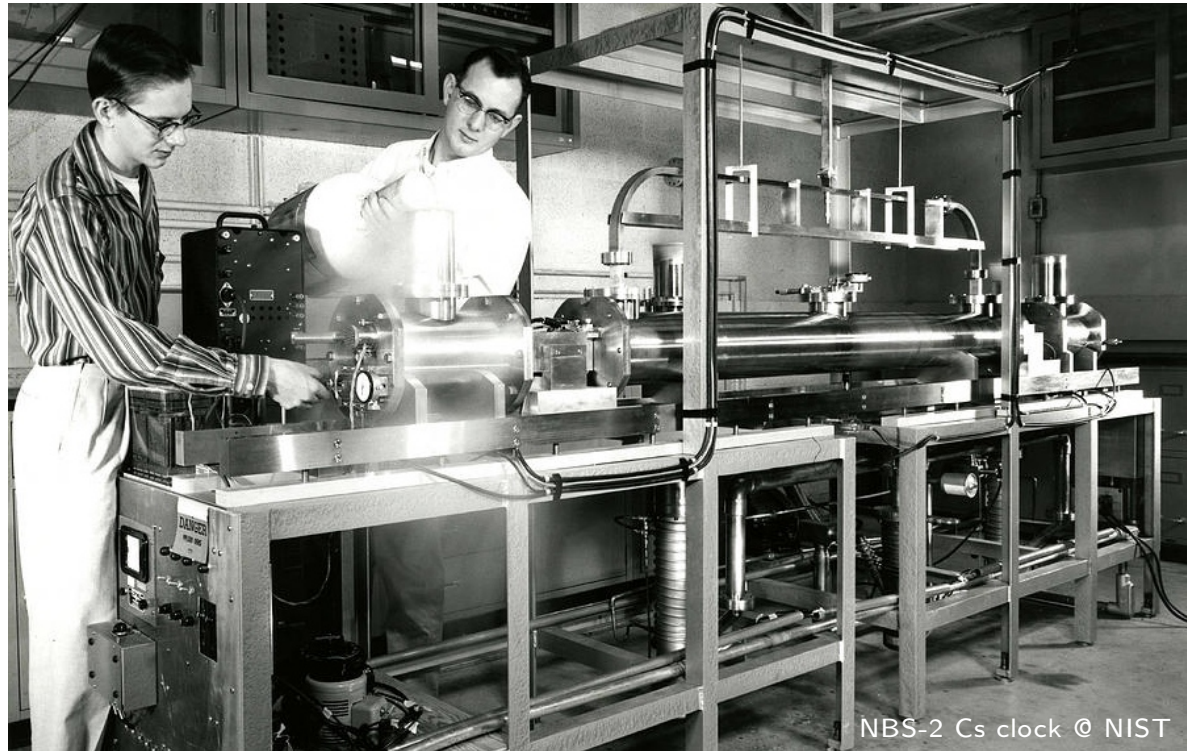


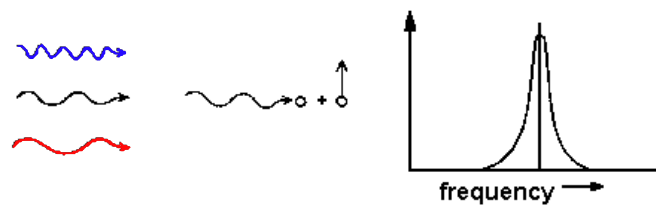
1. Degenerate atomic gases (as analogues?)

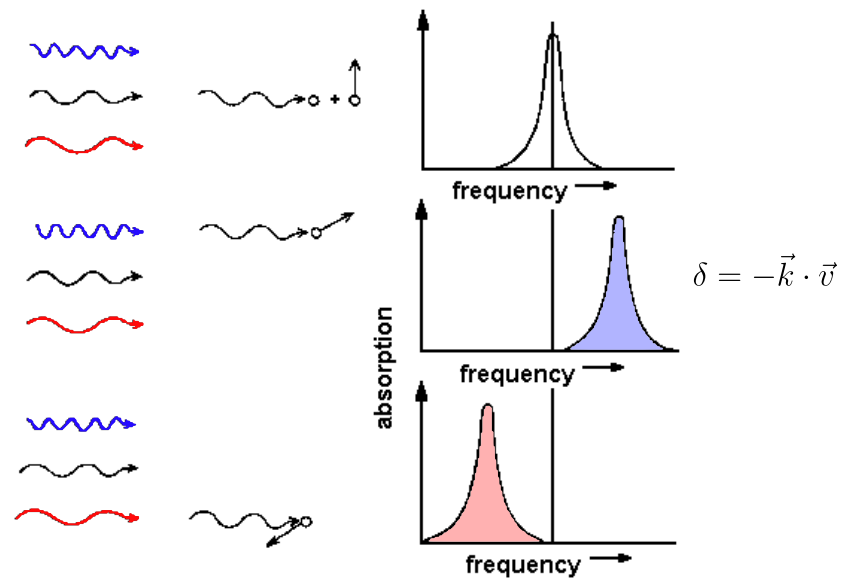
2. Laser cooling

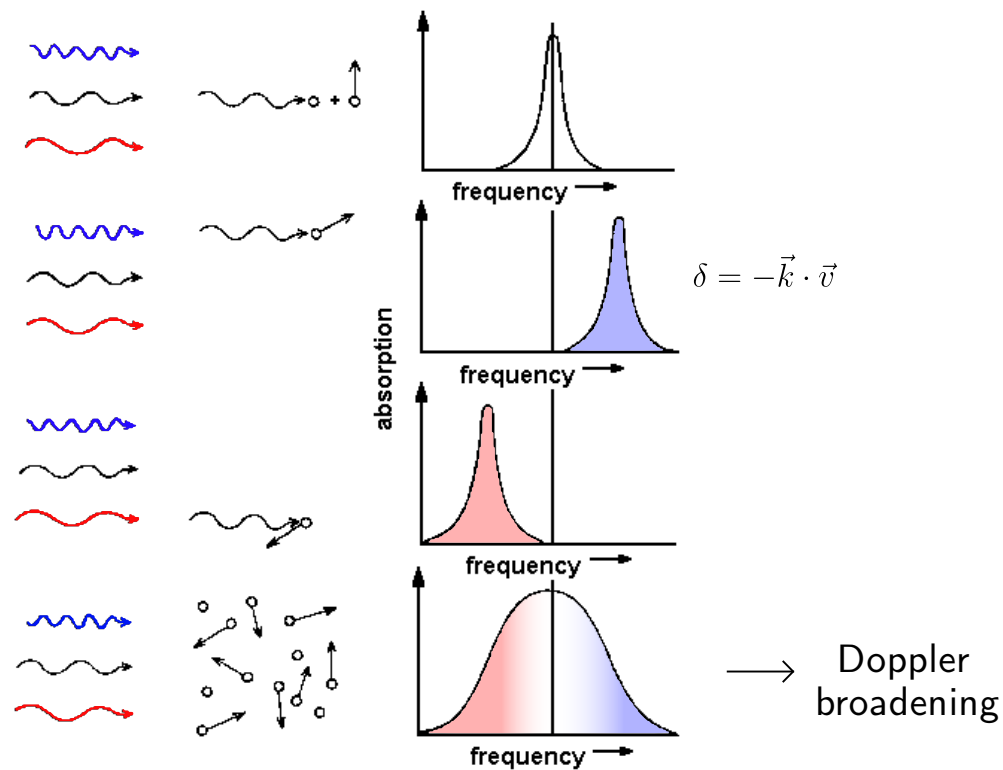
3. Evaporative cooling

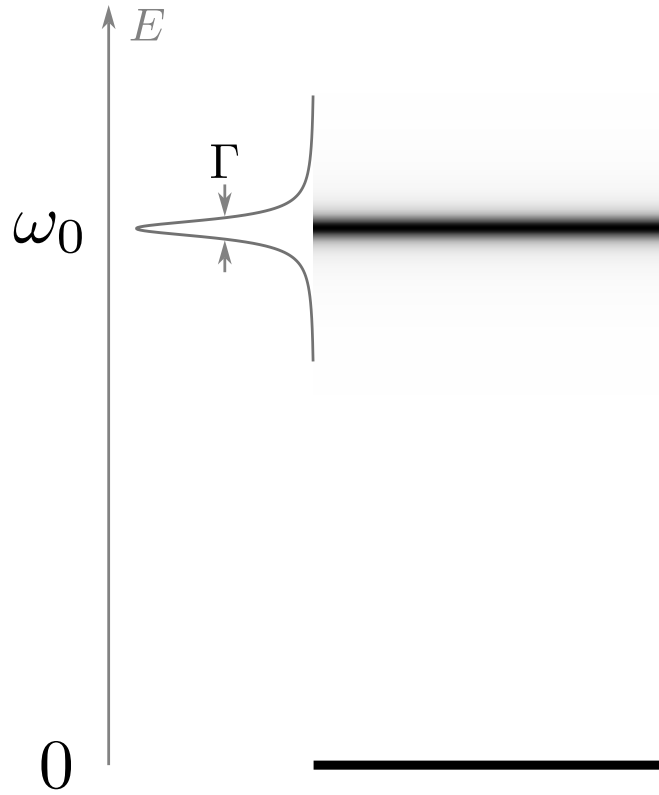
4. Bose-Hubbard physics

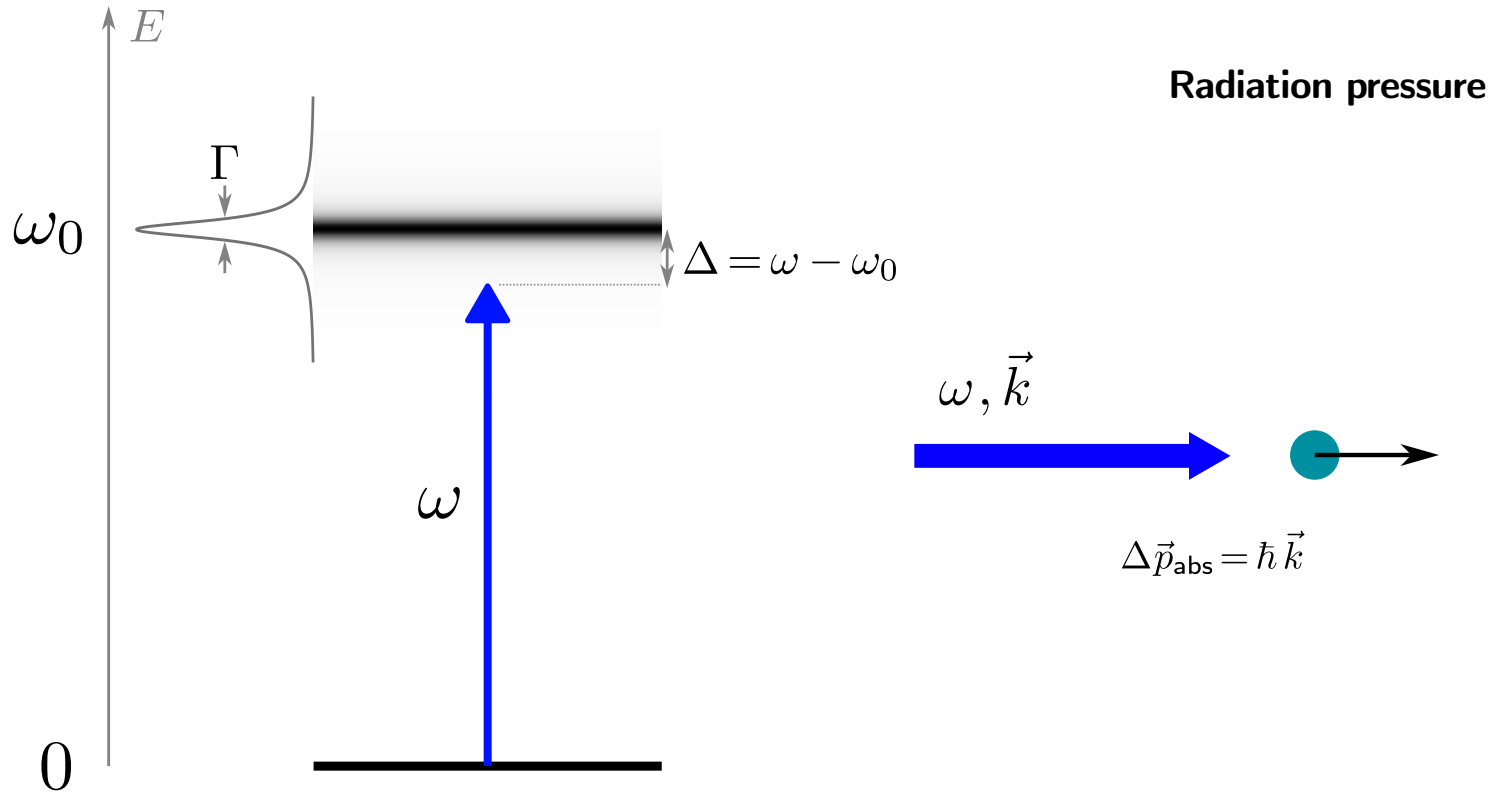


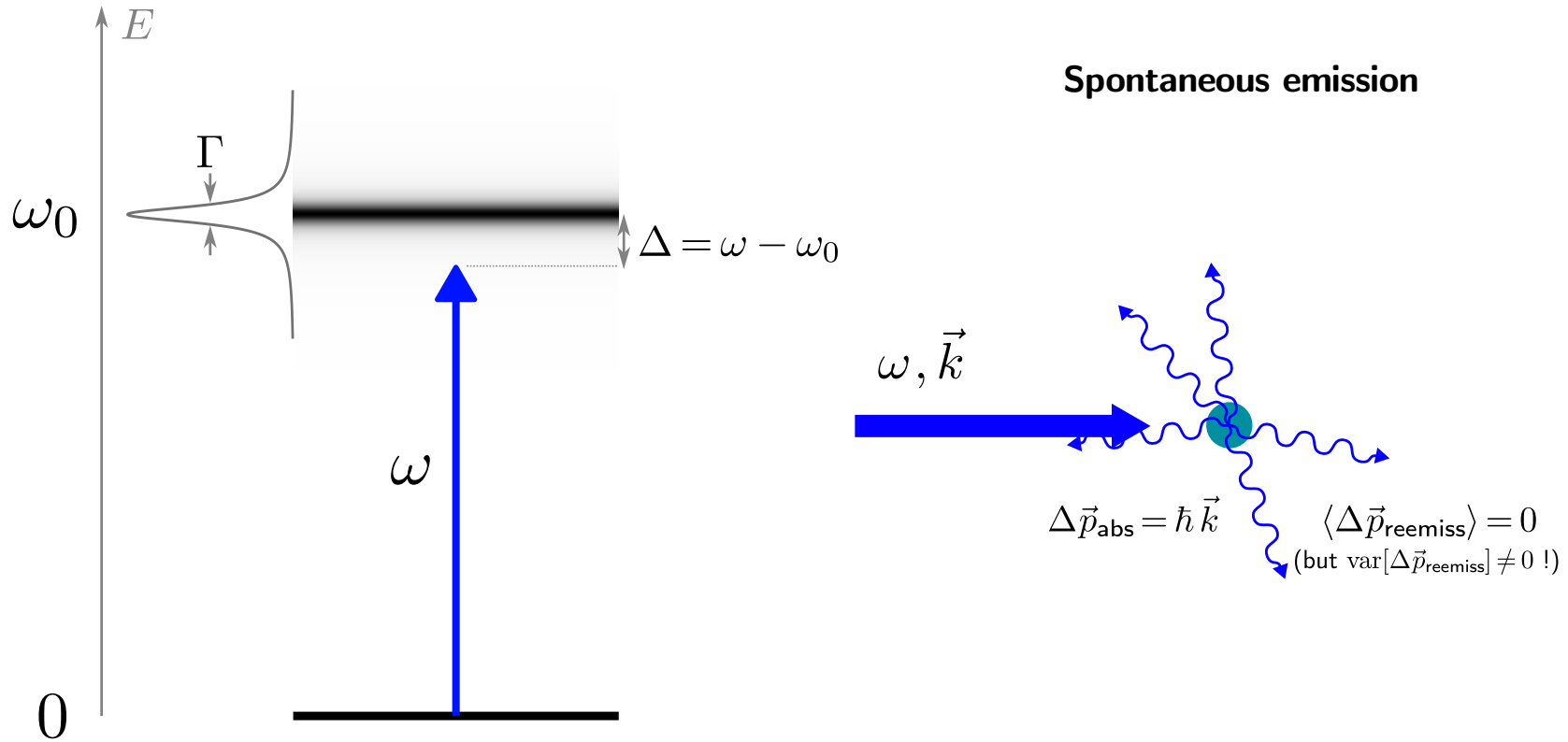


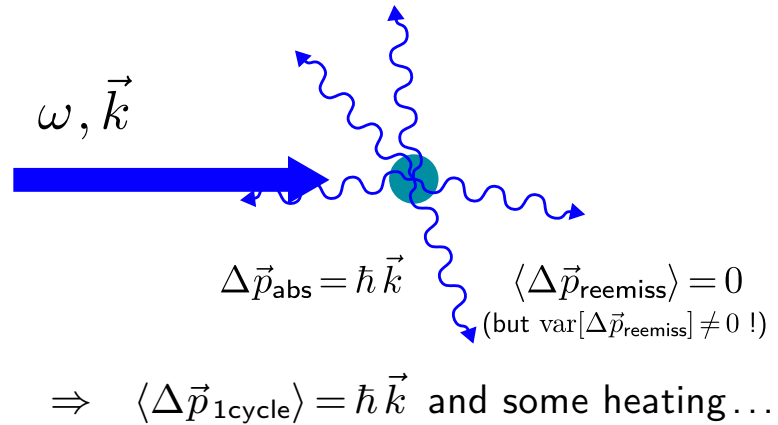
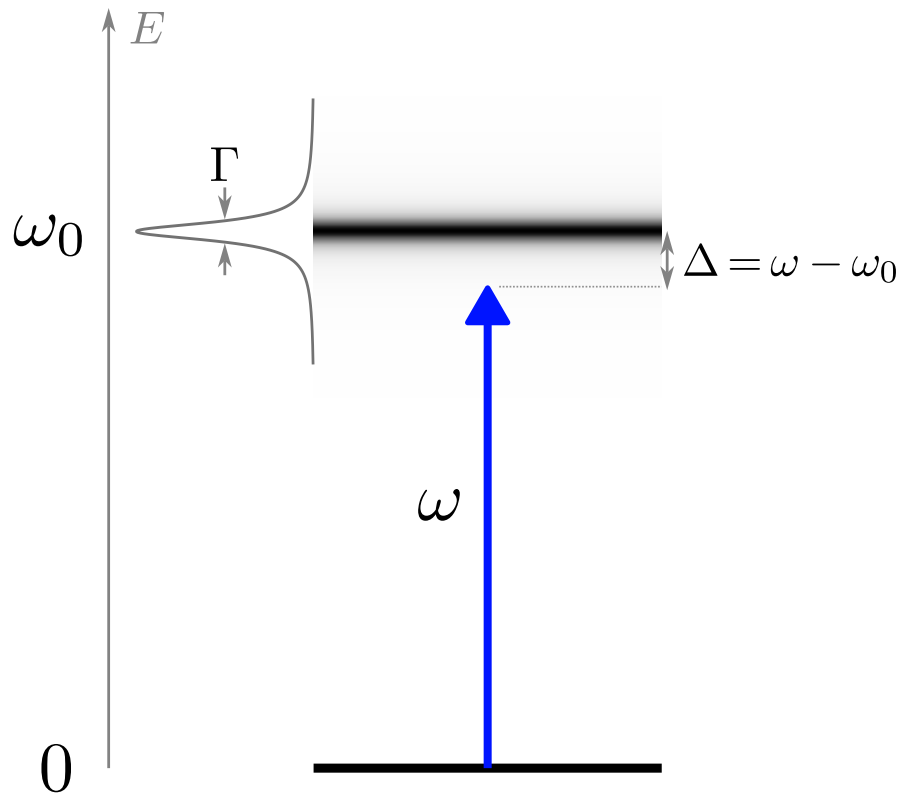


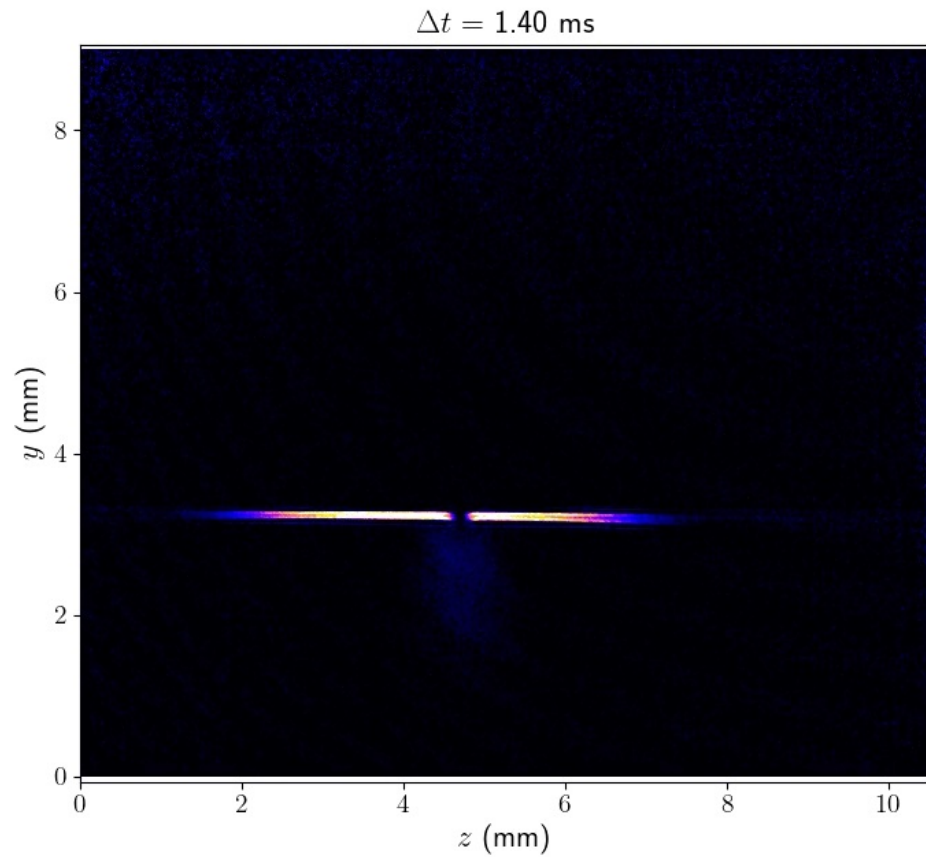


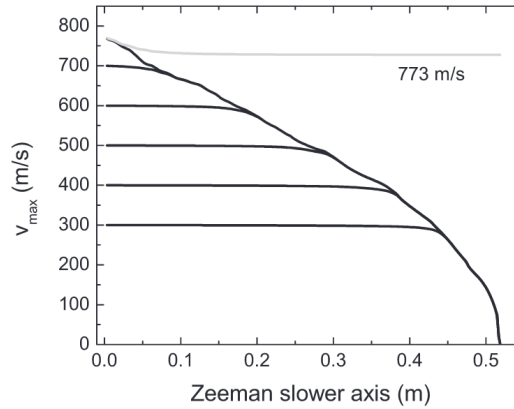
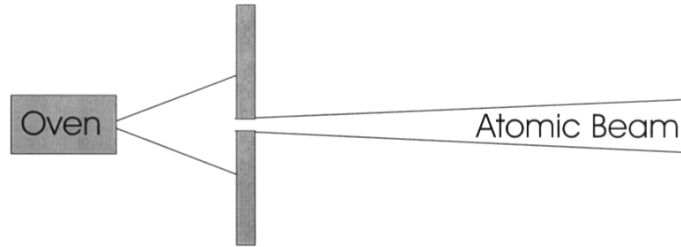


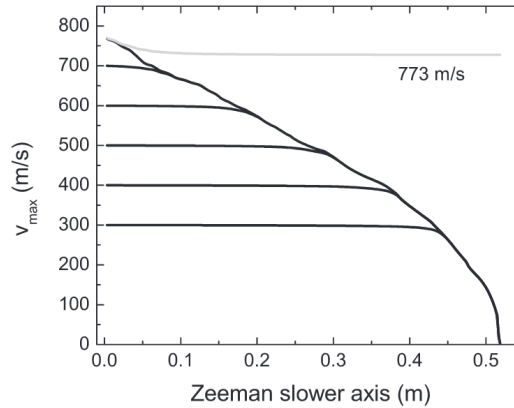
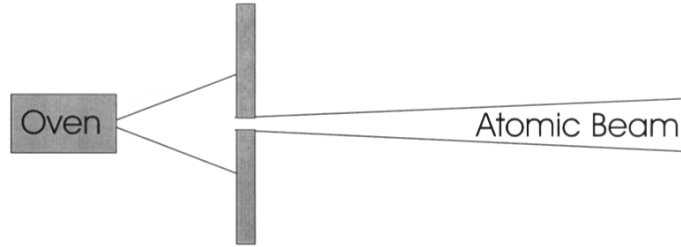




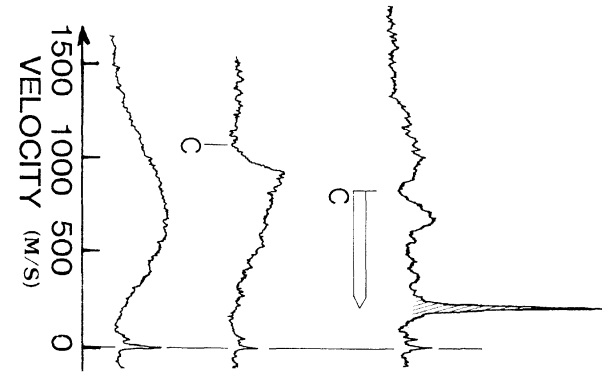






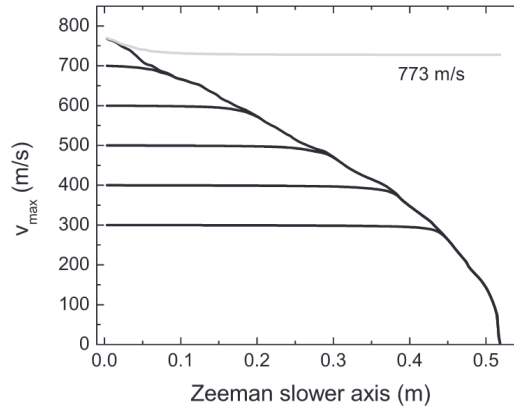
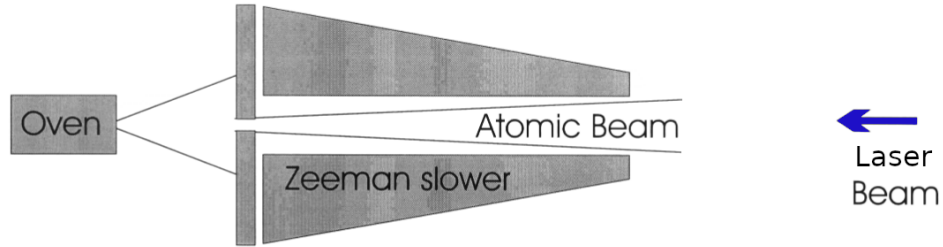


$\sim 10^5 g$!

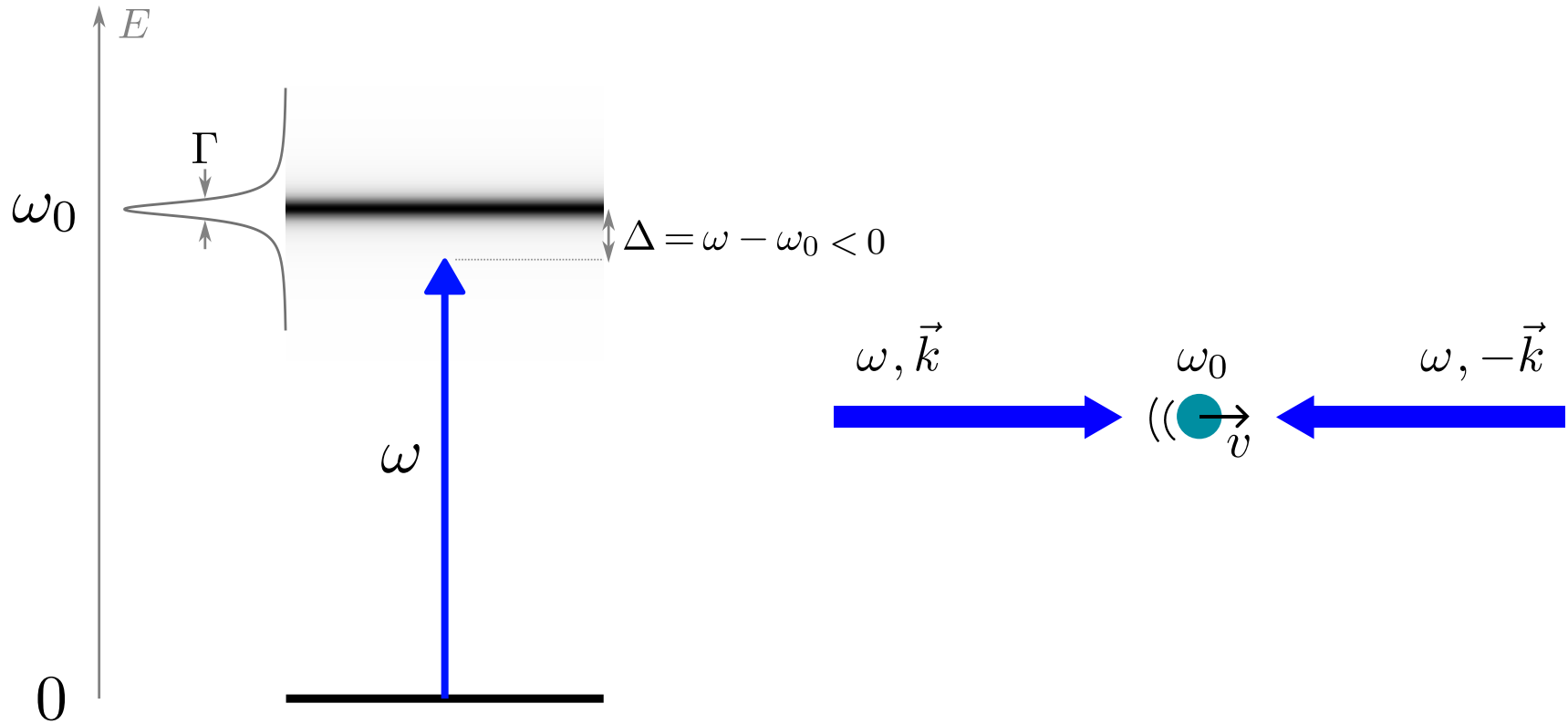


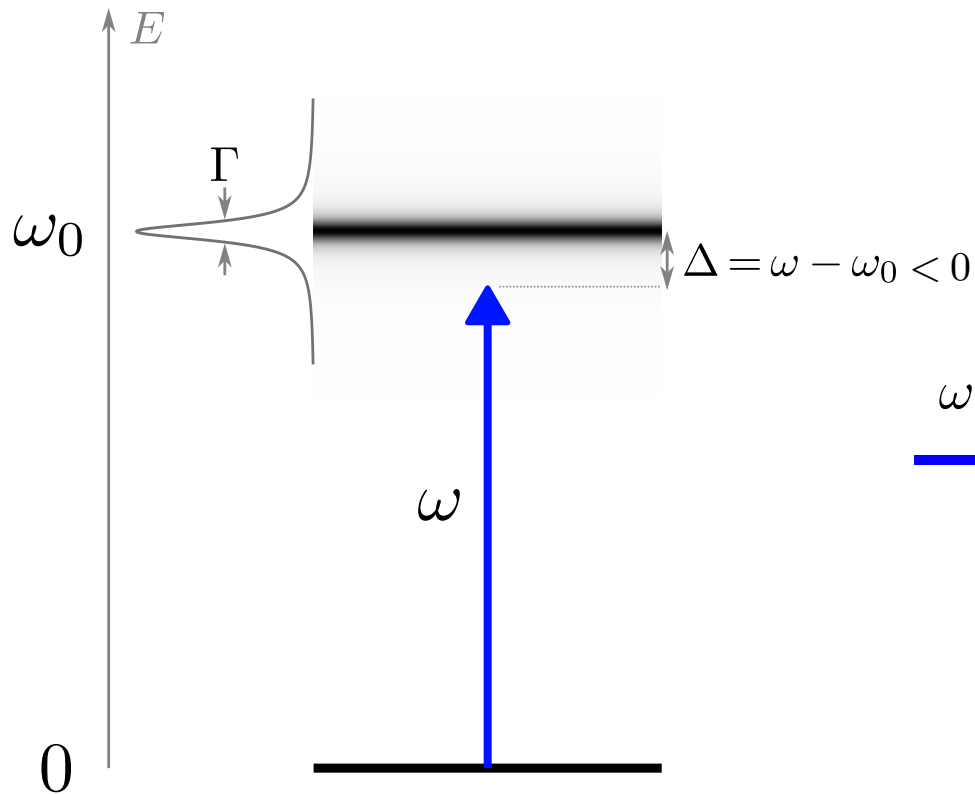
1978-84, Institute of Spectroscopy, Moscow

1984, Boulder

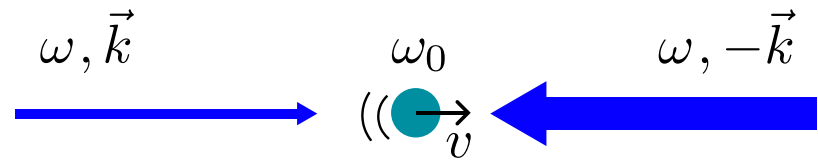


1982, NIST (Gaithersburg, USA)



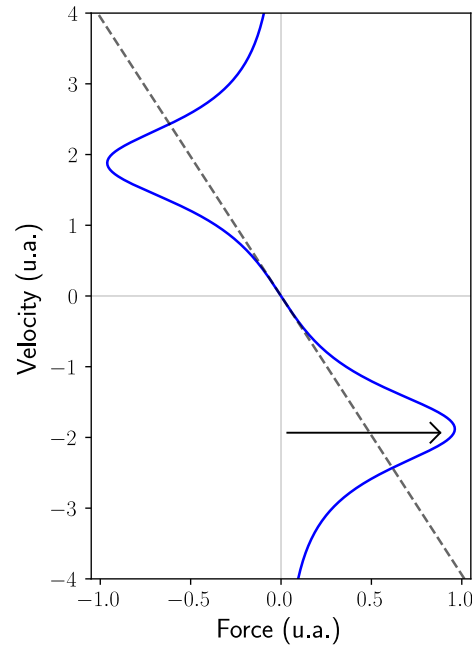
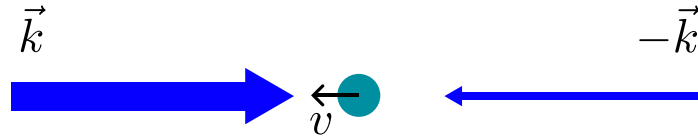


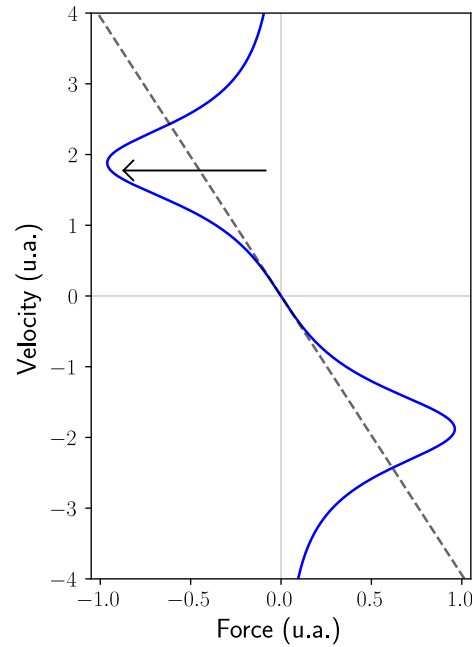
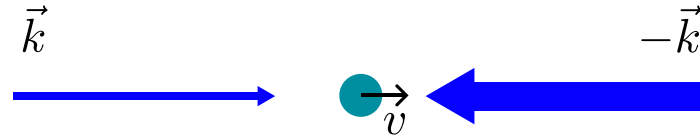
Absorption imbalance

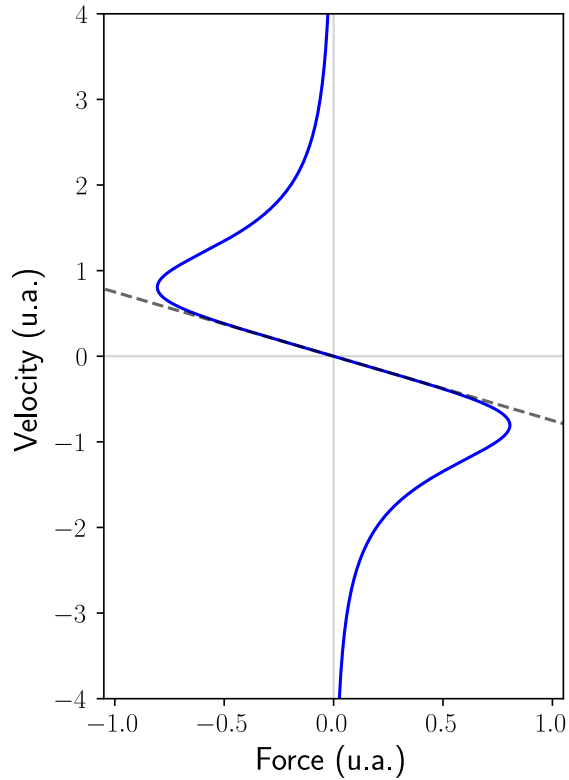


Doppler shift :

$$\Delta_{\text{seen by the atom}} = \Delta_{\text{laser}} - \vec{k} \cdot \vec{v}$$

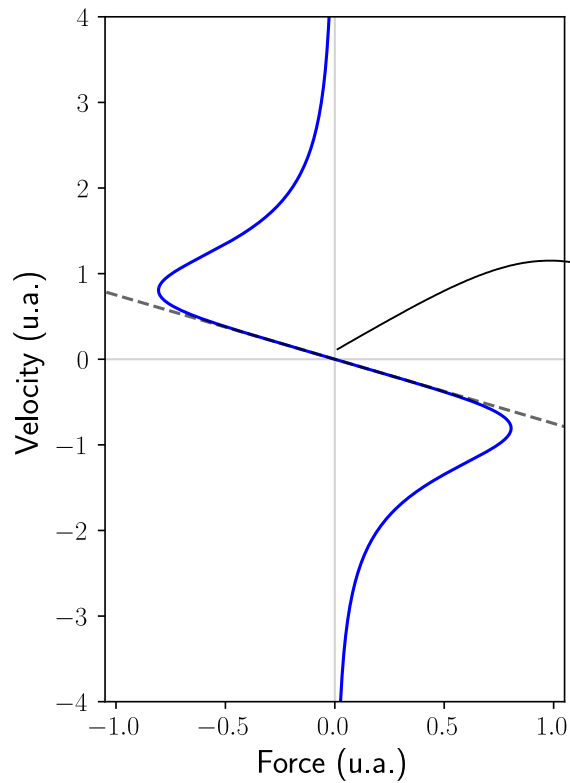






$$\Rightarrow \langle \vec{F}_{\text{molasses}} \rangle \propto -\vec{v}$$

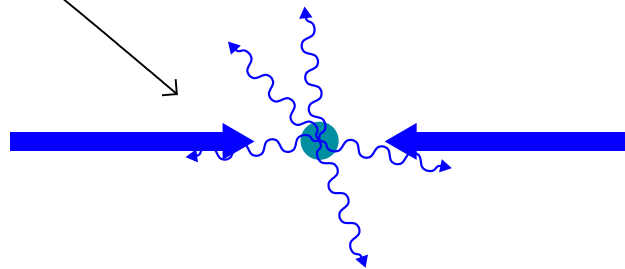
friction/damping force

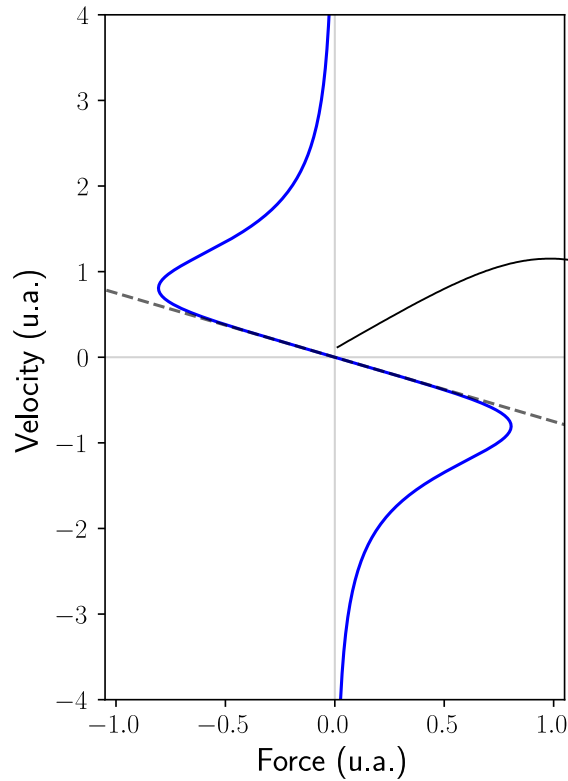


Cooling, $\langle \vec{F}_{\text{molasses}} \rangle \propto -\vec{v}$

+

Heating, even at $v = 0$

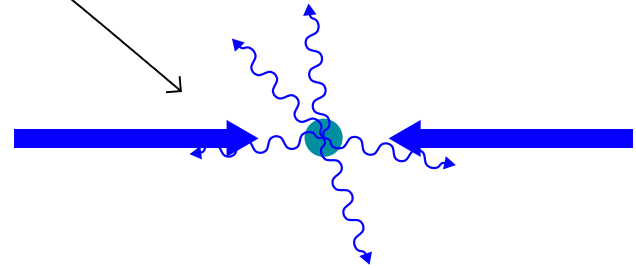




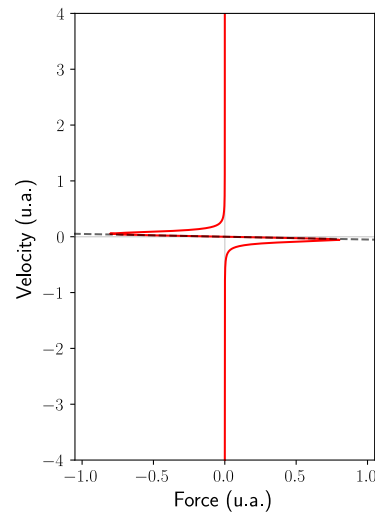
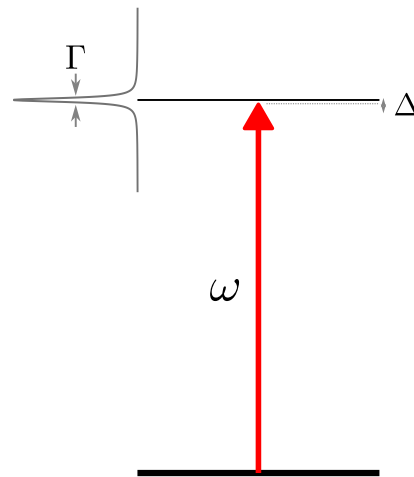
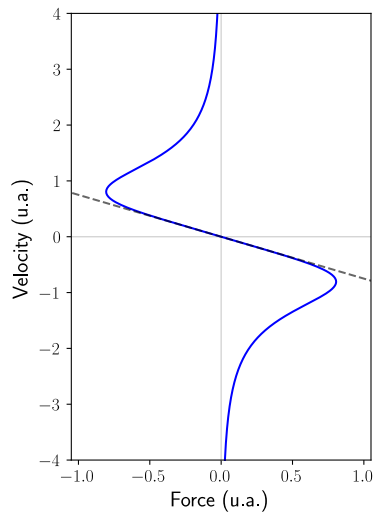
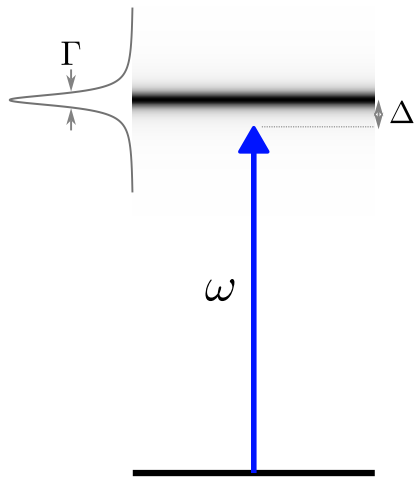
Cooling, $\langle \vec{F}_{\text{molasses}} \rangle \propto -\vec{v}$

+

Heating, even at $v = 0$



$\Rightarrow$ non-zero equilibrium avg. velocity



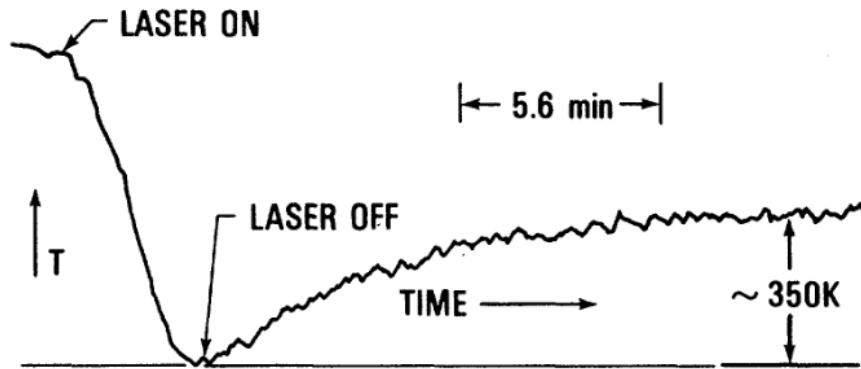
small linewidth Γ $\iff$ selective in frequency $\xleftrightarrow{\text{Doppler effect}}$ selective in velocity $\implies$ better $\frac{\text{damping}}{\text{heating}}$ $\implies \searrow v$'s

$$k_B T_{\min} = \frac{\hbar \Gamma}{2}$$

Idea : **1974**, Hänsch & Schawlow

First Doppler/sideband cooling on trapped ions : **1978**,

Wineland @ Boulder



Dehmelt @ Heidelberg

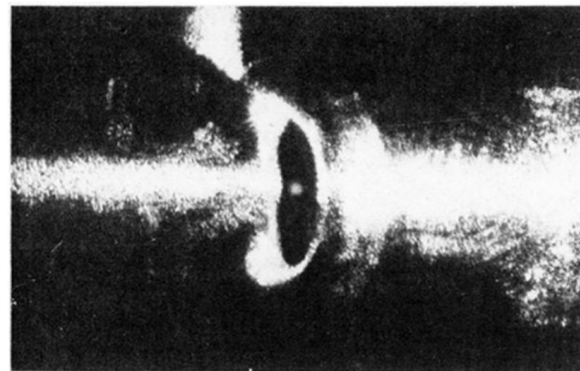


FIG. 2. Photograph of trap looking in $-x'$ direction. The Ba^+ cloud is visible in the center.

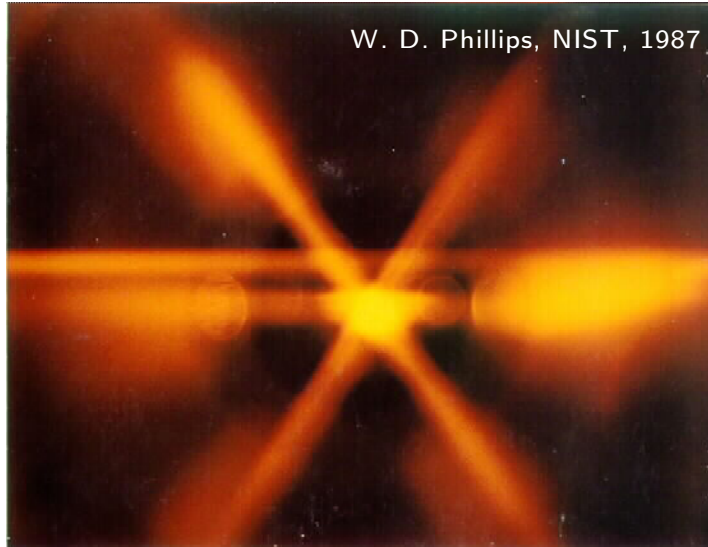
2D molasses (atomic beam) : **1984**, Letokhov & Minogin, Institute of Spectroscopy, Moscow

→ 3.5 mK

3D molasses : **1985**, S. Chu @ Bell Labs

→ 240 μ K

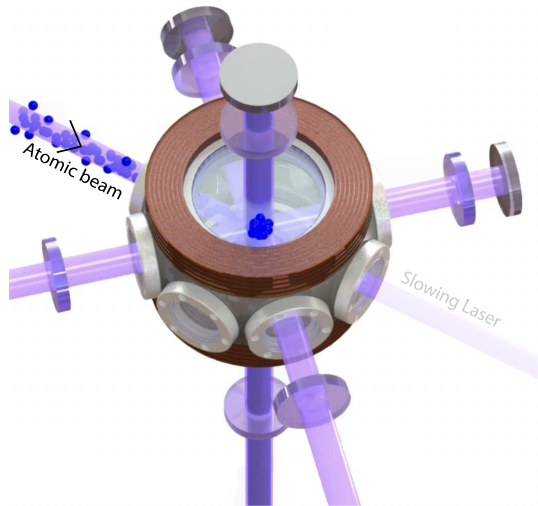
Then ENS, NIST, JILA...



3D molasses + restoring force $\Rightarrow$ Cooling *and trapping*

$$\langle \vec{F}_{\text{molasses}} \rangle \propto -\vec{v}$$

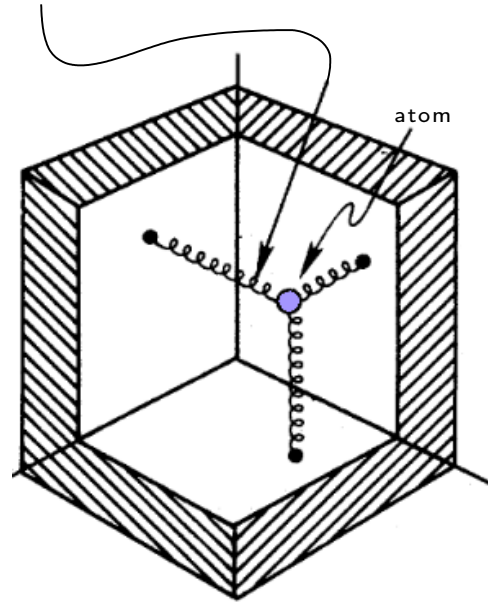
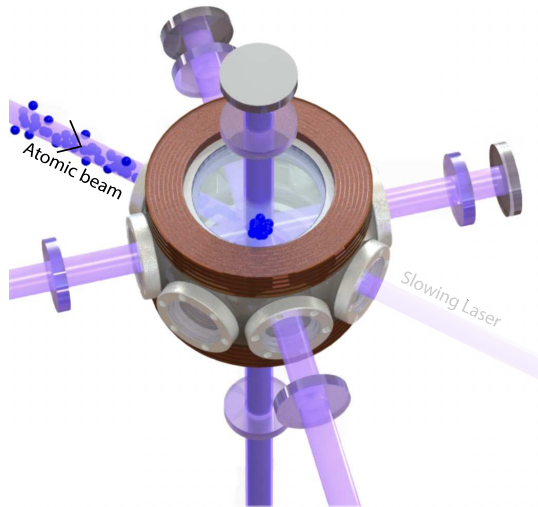
$$\langle \vec{F}_{\text{restoring}} \rangle \propto -\vec{r}$$



3D molasses + restoring force $\Rightarrow$ Cooling *and* trapping

$$\langle \vec{F}_{\text{molasses}} \rangle \propto -\vec{v}$$

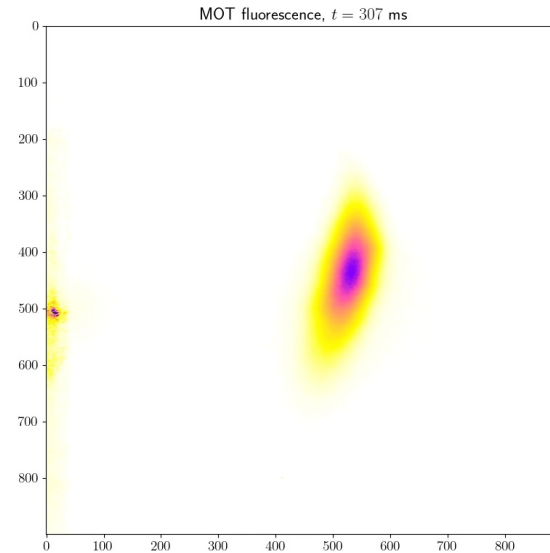
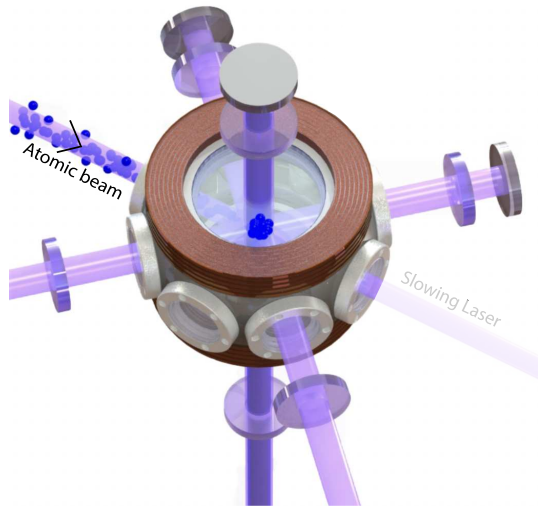
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3D molasses + restoring force $\Rightarrow$ Cooling *and trapping*

$$\langle \vec{F}_{\text{molasses}} \rangle \propto -\vec{v}$$

$$\langle \vec{F}_{\text{restoring}} \rangle \propto -\vec{r}$$



First magneto-optical trap : **1985**, Raab, S. Chu, Prichard @ Bell Labs
+ ideas of J. Dalibard

Typ. maximum MOT PSD : 10^{-4} (alkali elements)

Confirmation of sub-Doppler cooling : 1988

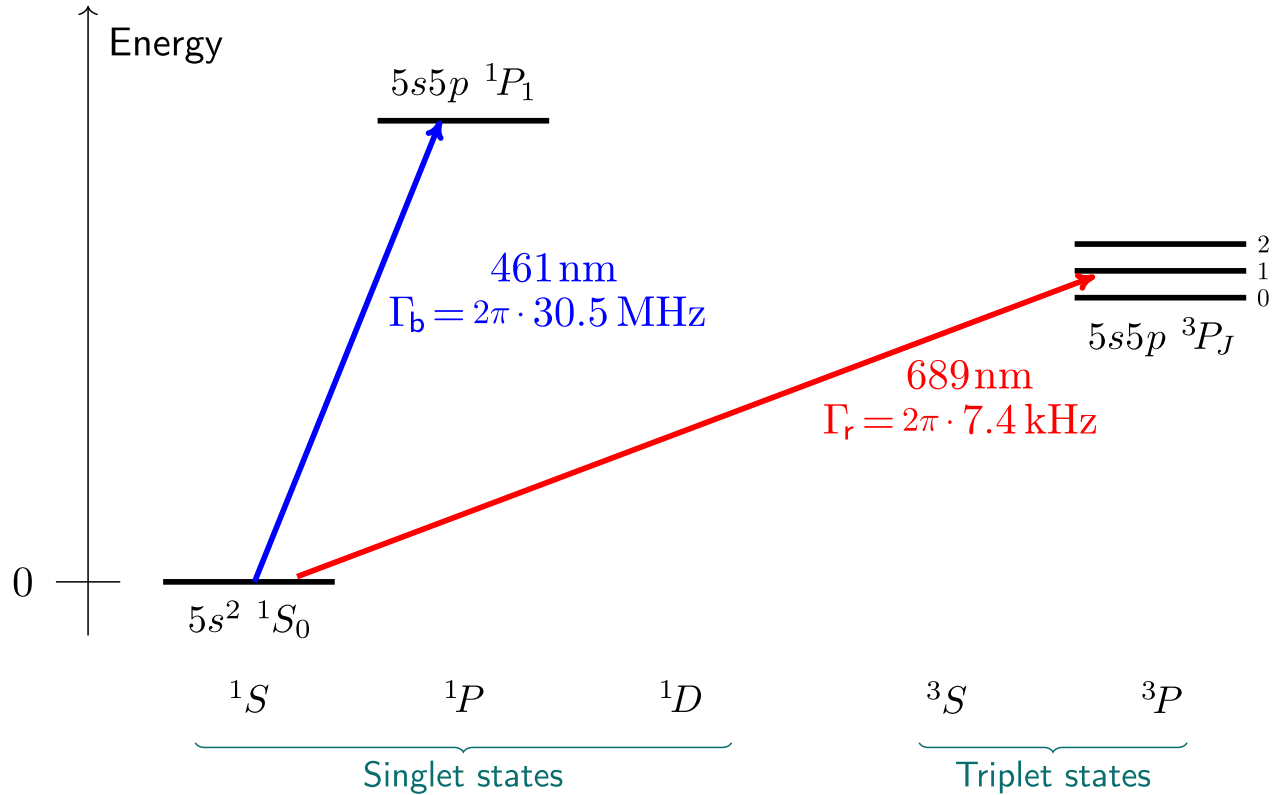
Nobel prize for C. Cohen-Tannoudji, S. Chu, W. D. Phillips

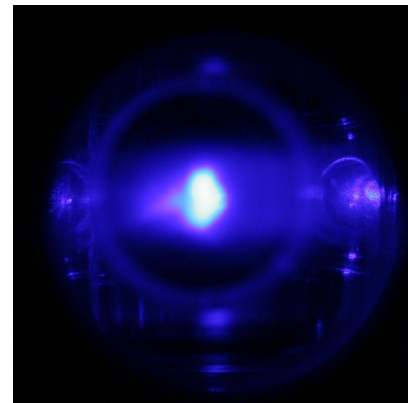
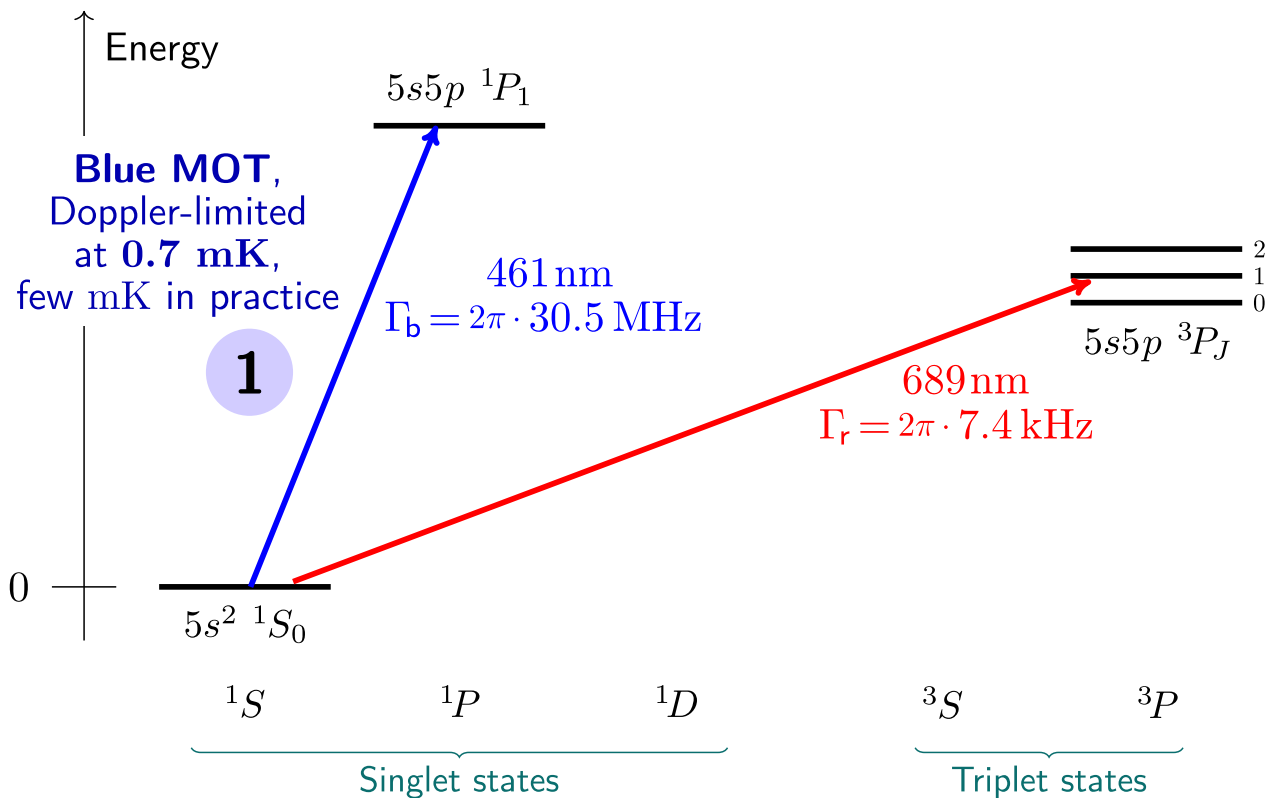


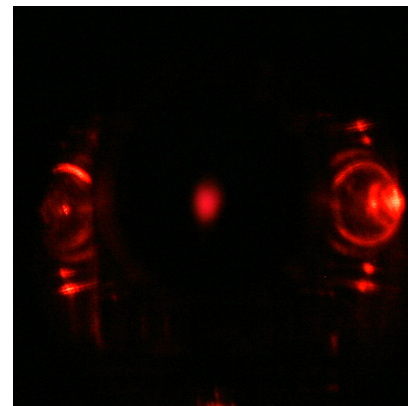
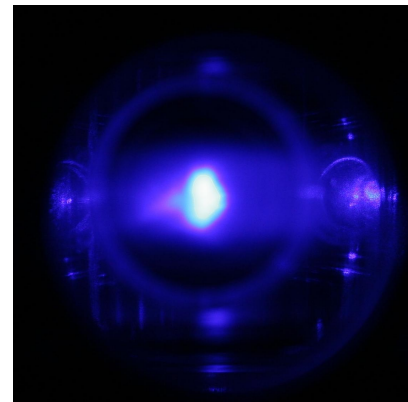
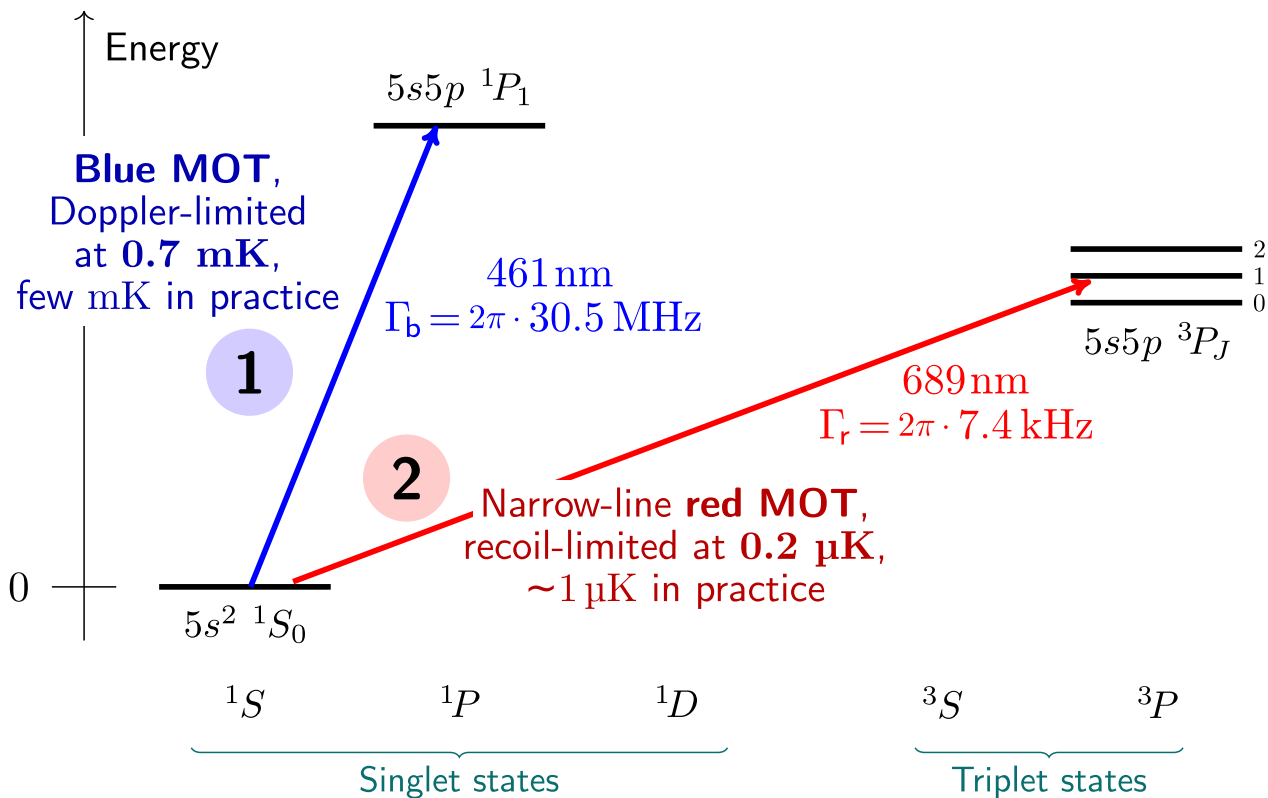
Strontium : a two-valence-electrons atom

44/89

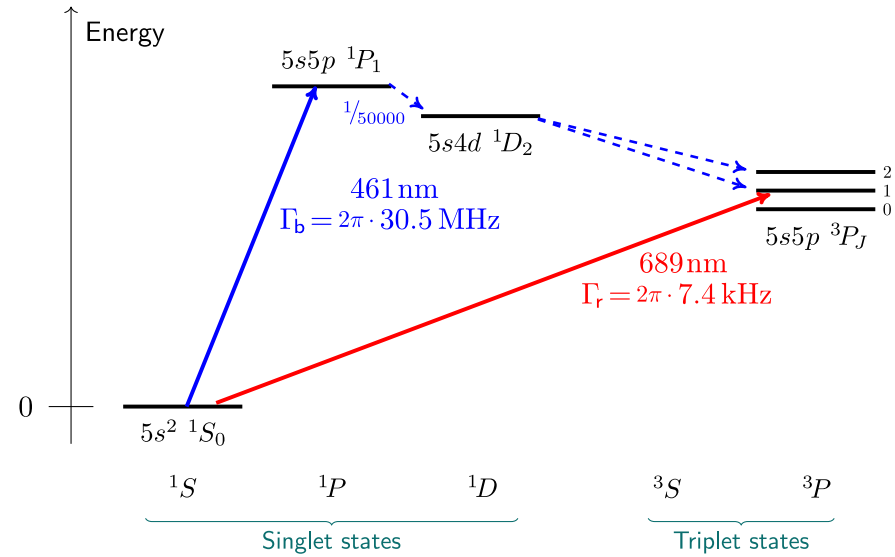
Group→	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
↓Period																		
1	1 H																	2 He
2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne
3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
6	55 Cs	56 Ba		72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
7	87 Fr	88 Ra		104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og
Lanthanides			57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu	
Actinides			89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr	







E1-forbidden : $\langle S=0, \dots | \vec{D} | S=1, \dots \rangle = 0$

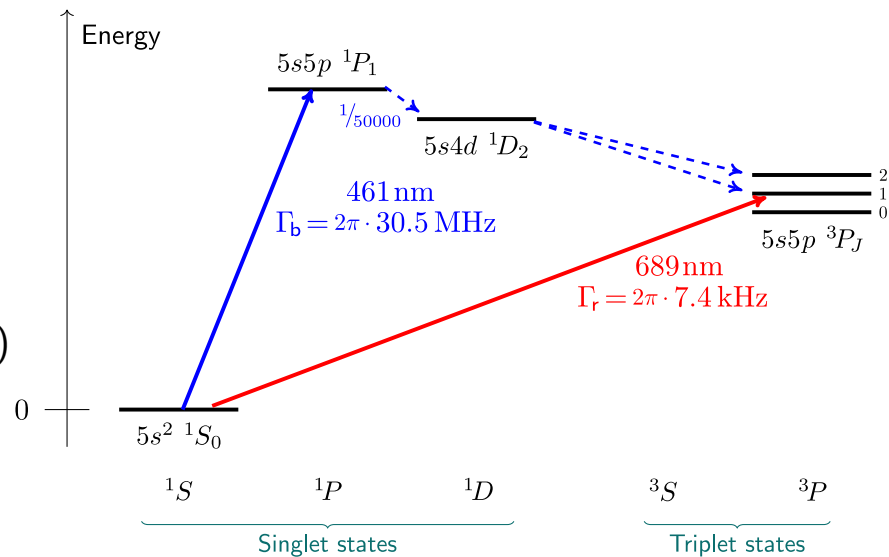


E1-forbidden : $\langle S=0, \dots | \vec{D} | S=1, \dots \rangle = 0$

Spin-orbit (not just $\vec{L} \cdot \vec{S}$ term !)

weak but non-negligible in Sr ($Z=38$).

$\rightarrow L, S$ not strictly good quantum numbers (J is)



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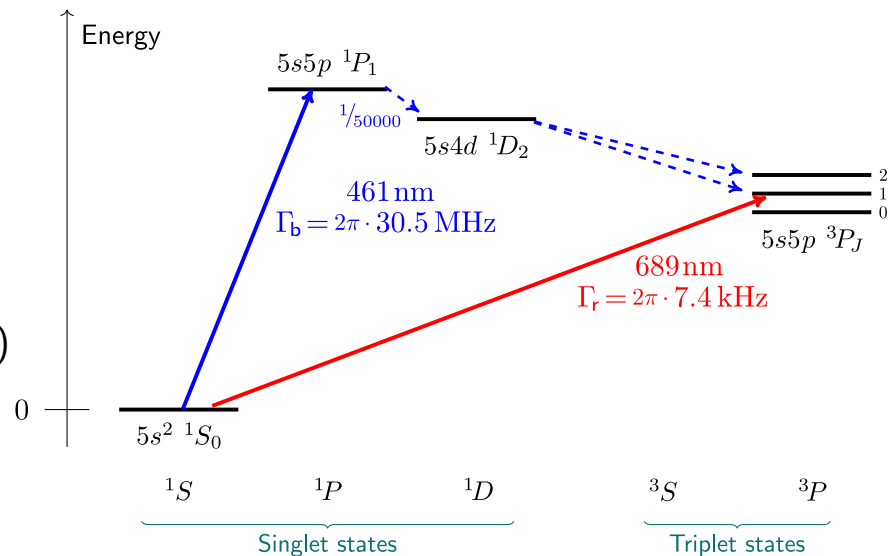
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→ Spin-orbit mixes LS terms with same J ,
and in particular

$$|5s5p\ ^3P_1\rangle = (1 - \varepsilon) |5s5p, S=1, L=1, J=1\rangle + \varepsilon |5s5p, S=0, L=1, J=1\rangle + \dots$$

$\uparrow$
 $\uparrow$



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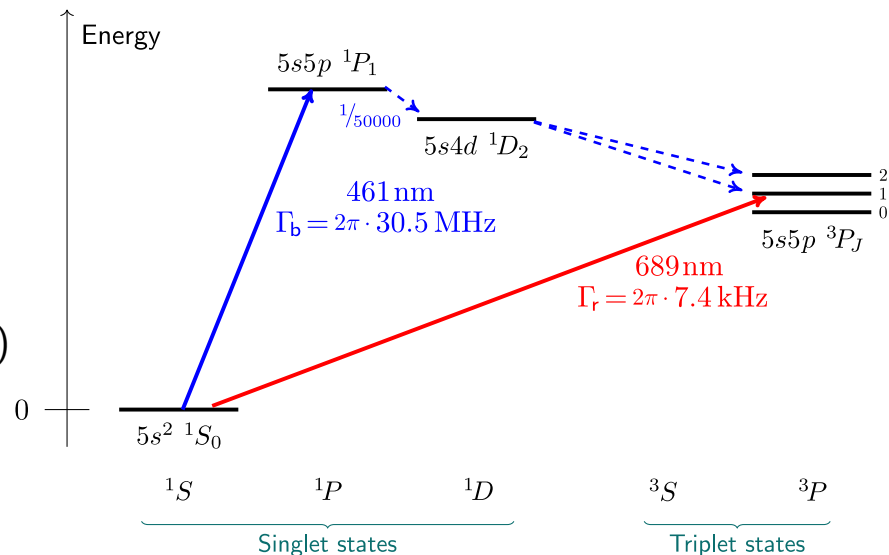
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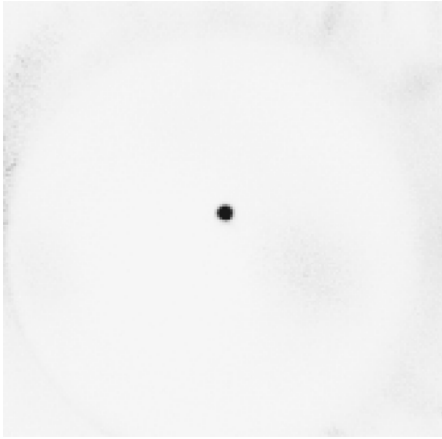
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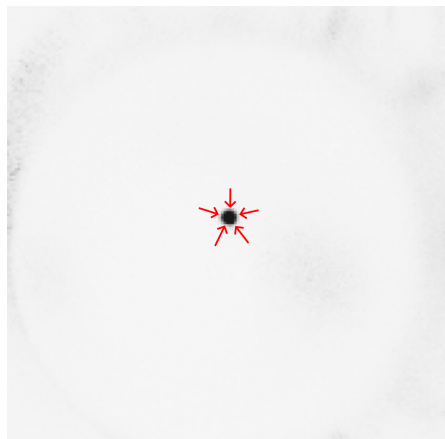
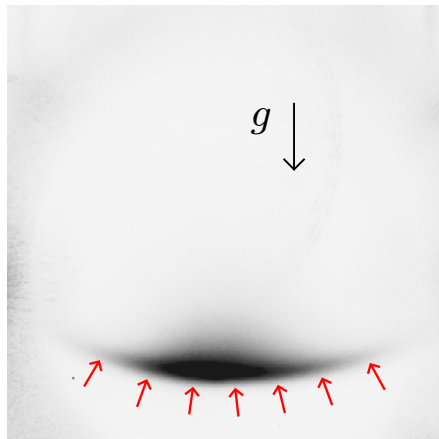
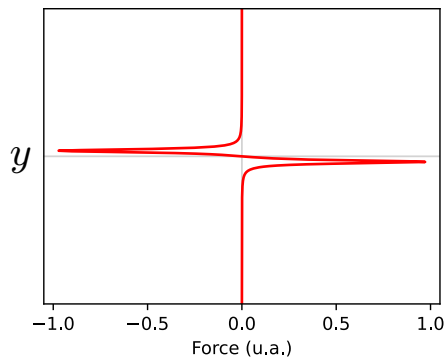
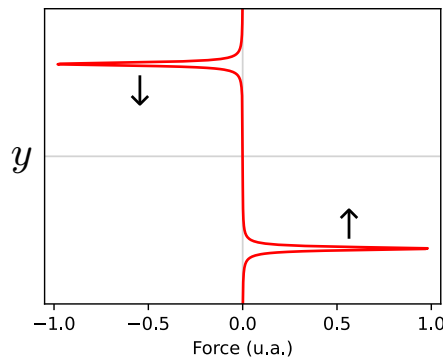
↑

↑

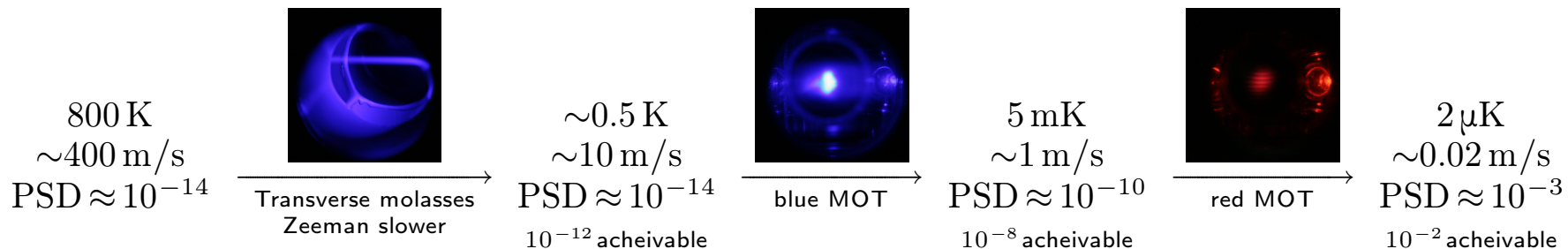
$$\Rightarrow \langle ^1S_0 | \vec{D} | ^3P_1 \rangle \neq 0 \quad (\propto \varepsilon) \quad \Rightarrow \text{finite (long) lifetime, E1 decay}$$






 $\Delta = -\text{few } \Gamma$

 $\Delta = -300 \Gamma$

 $\Delta = -10 \Gamma$
 $T_{\min} = 0.2 \mu\text{K}$
 $1 \sim 2 \mu\text{K}$ in practice

 $\sim 50 \cdot 10^6$ at in $\sim (100 \mu\text{m})^3$
 $\text{PSD} \approx 10^{-2} !$



1. Oven $\rightarrow$ atomic beam
2. Transverse cooling
3. Zeeman slower
4. Blue MOT ($\sim 1 \text{ s}$ for loading 10^8 atoms)
5. Broadened red MOT ($\sim 0.1 \text{ s}$)
6. Narrow-line red MOT ($\sim 0.1 \text{ s}$)
7. ...we're not there yet !

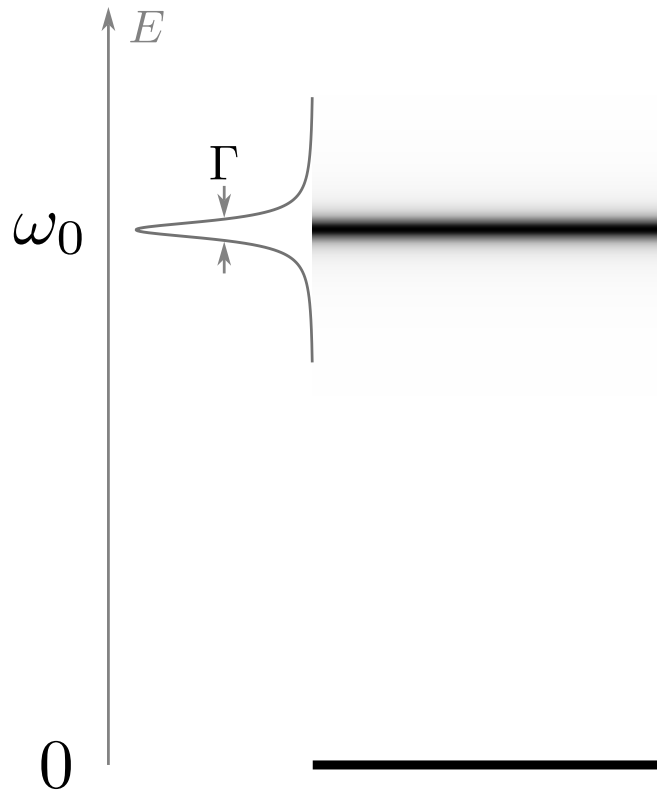
1. Degenerate atomic gases (as analogues?)
2. Laser cooling
3. **Evaporative cooling**
4. Bose-Hubbard physics

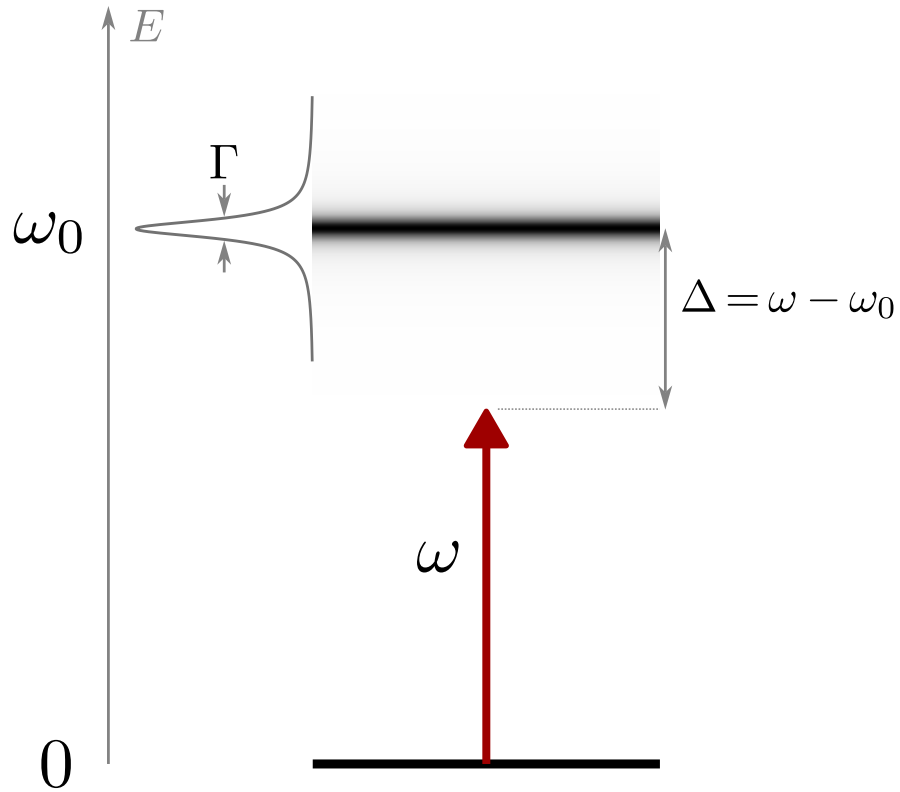
Cannot really use resonant light / dissipative cooling : residual random motion + losses

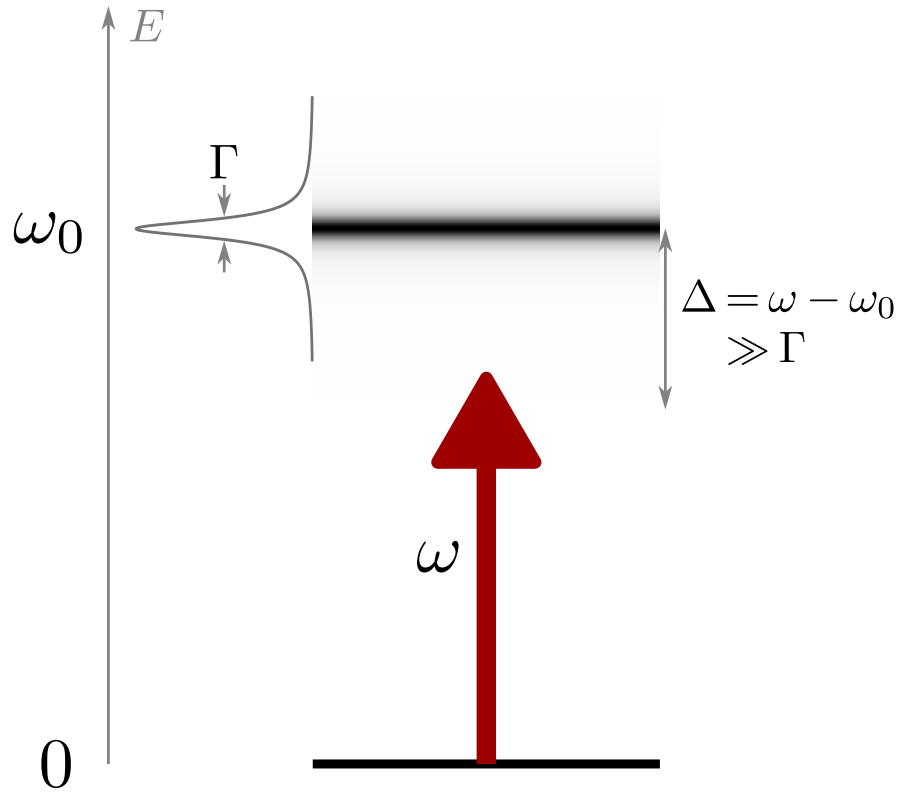
⇒ Conservative potentials

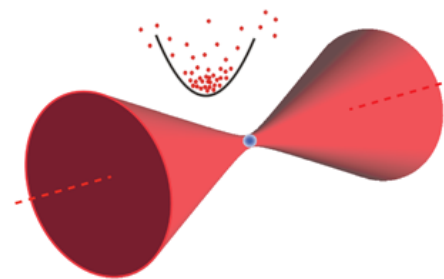
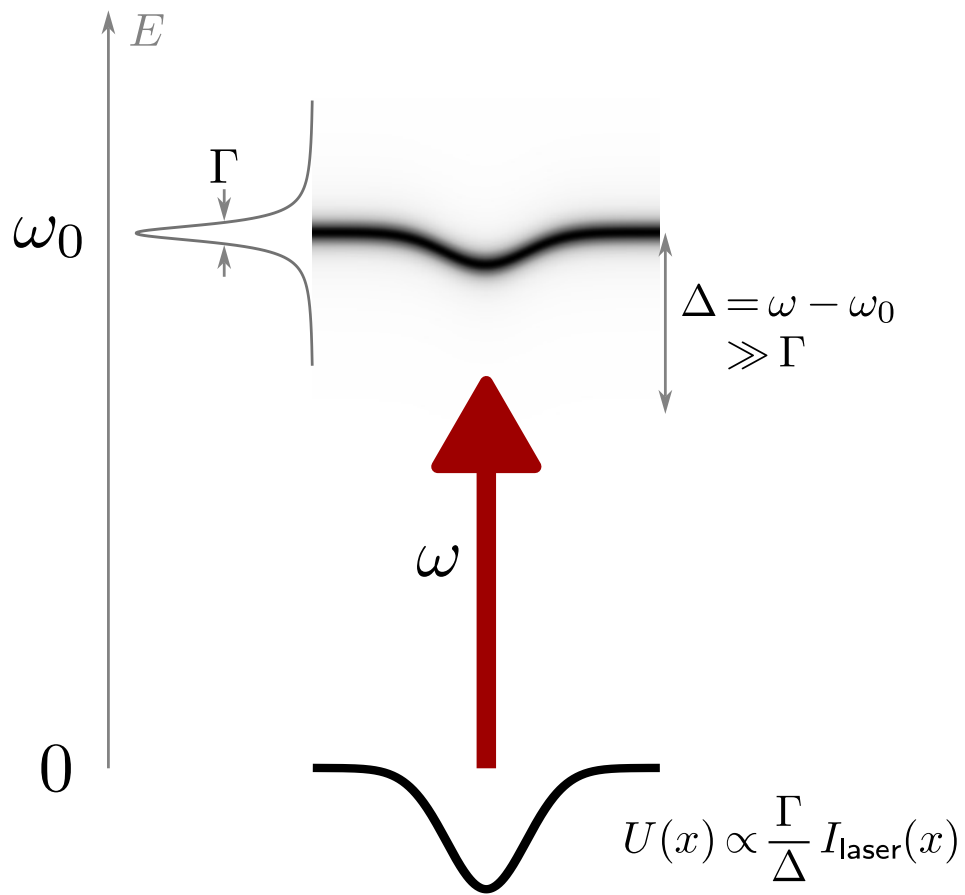
→ Magnetic traps

→ Optical traps

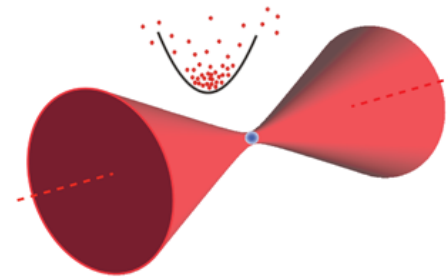
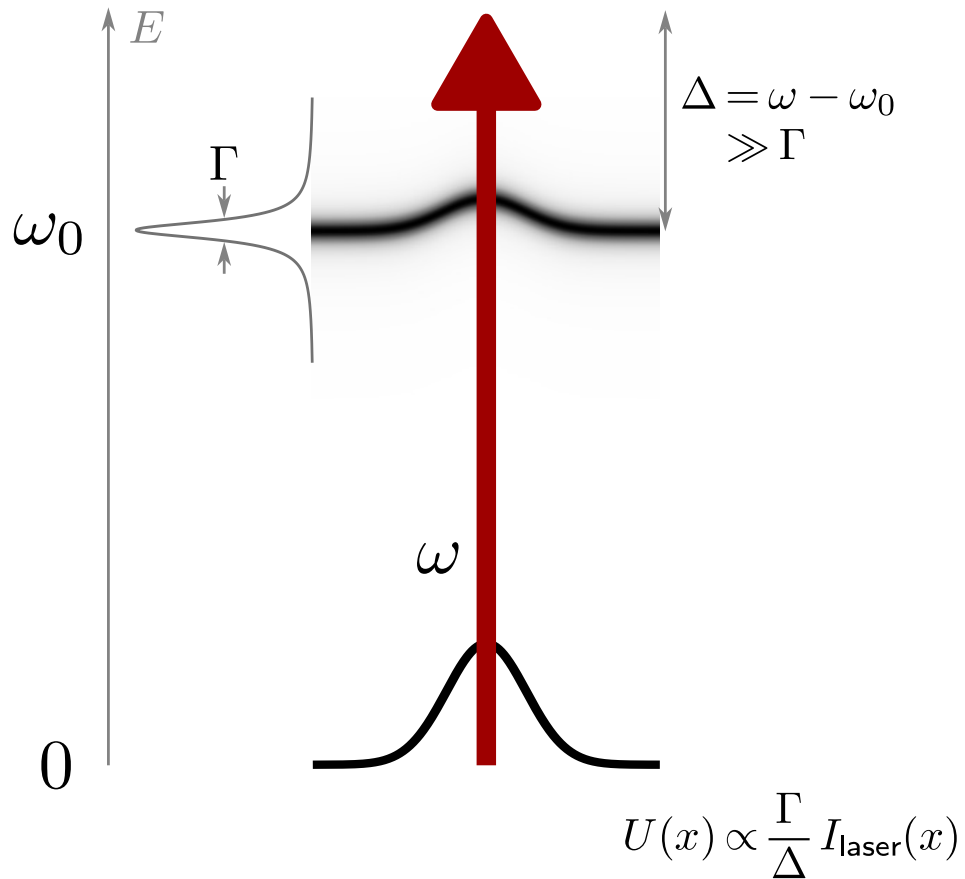




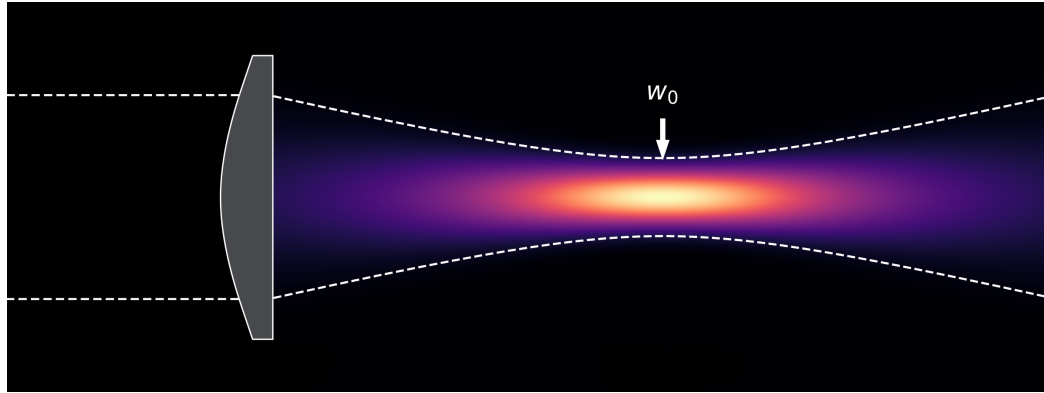




eg. gaussian beam



eg. gaussian beam



$$\text{potential}(\vec{x}) \propto -\text{intensity}(\vec{x})$$

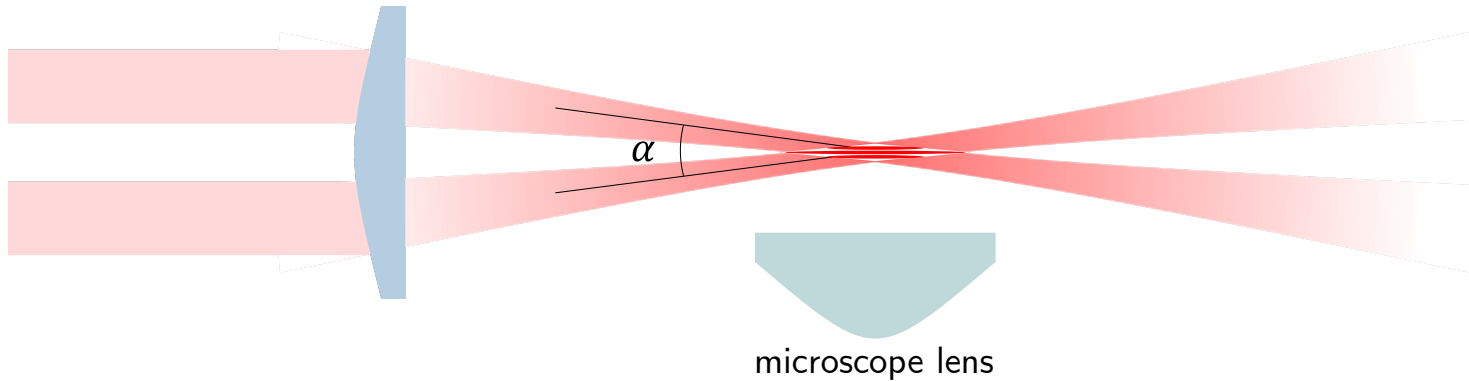
We want to study a 2D gas

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→ we need to **freeze vertical motion** (while keeping a large system horizontally)

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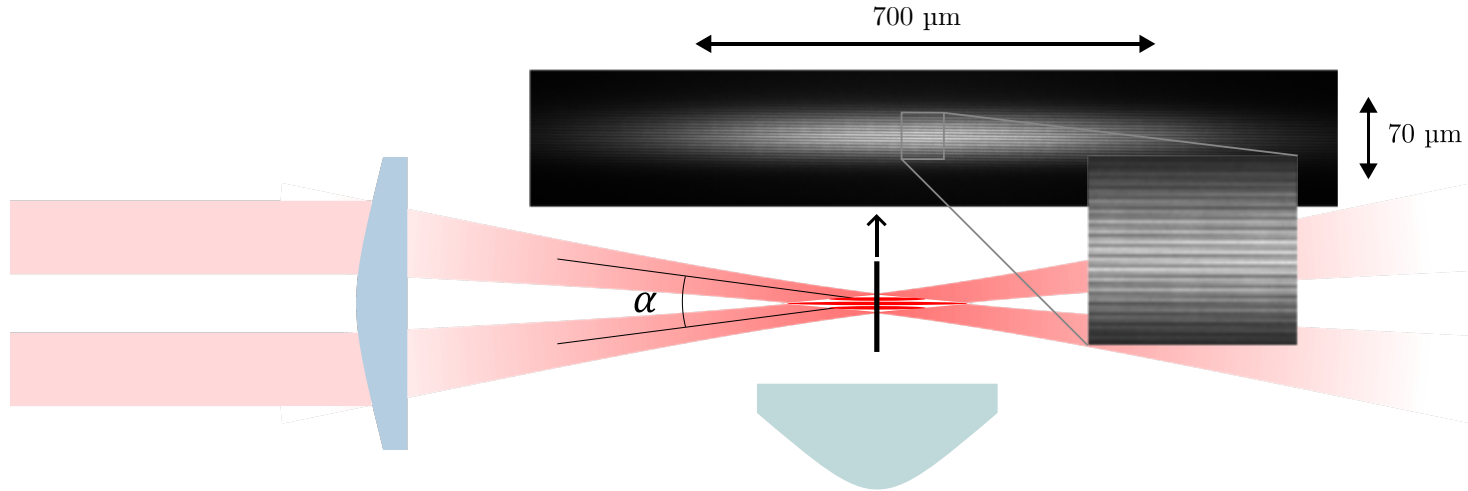
→ we need to **freeze vertical motion** (while keeping a large system horizontally)



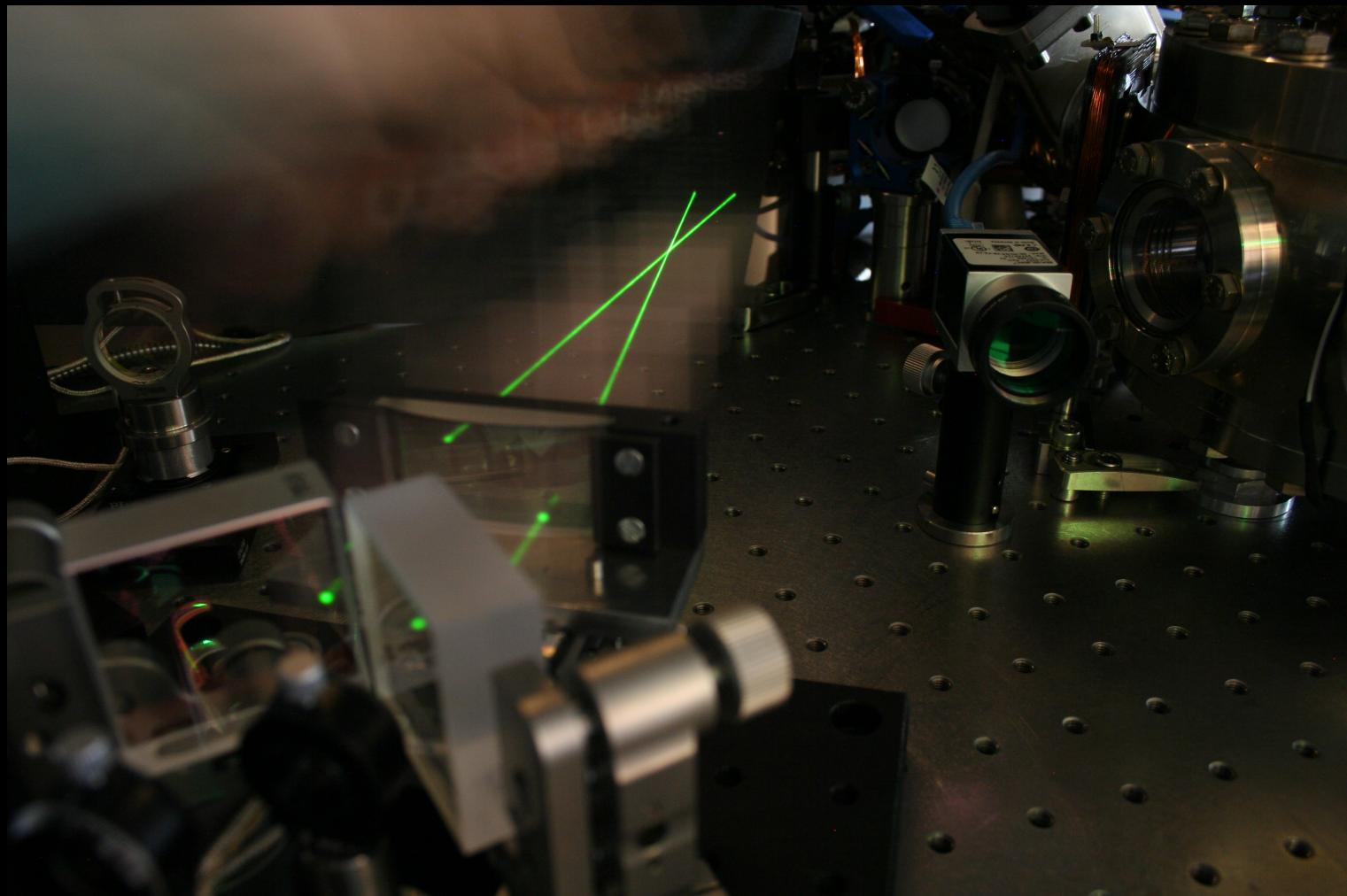
$$\alpha = 12^\circ \rightarrow 5 \mu\text{m fringe-to-fringe}$$

We want to study a 2D gas

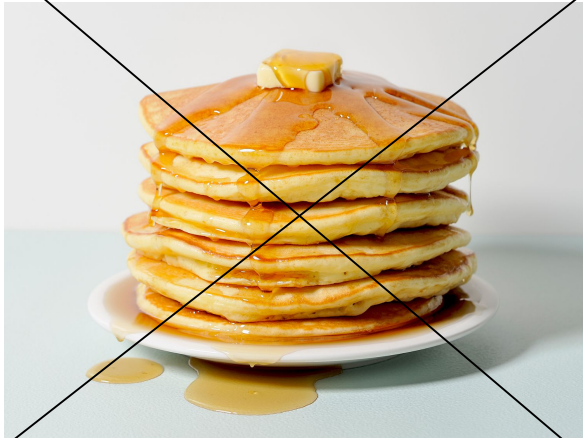
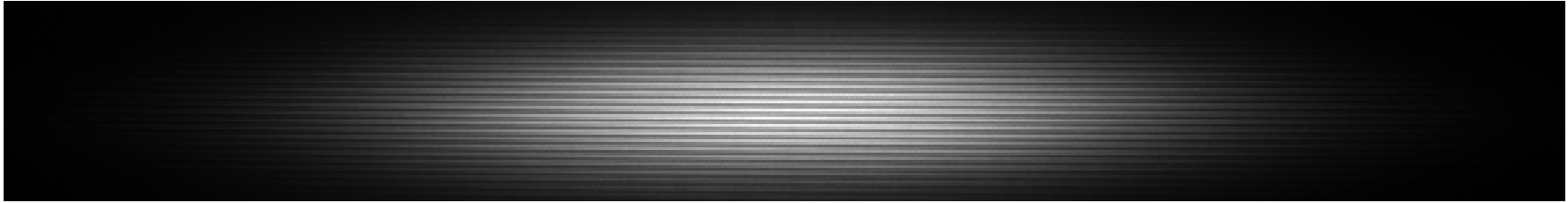
→ we need to **freeze vertical motion** (while keeping a large system horizontally)



$$\alpha = 12^\circ \rightarrow 5\ \mu\text{m} \text{ fringe-to-fringe}$$

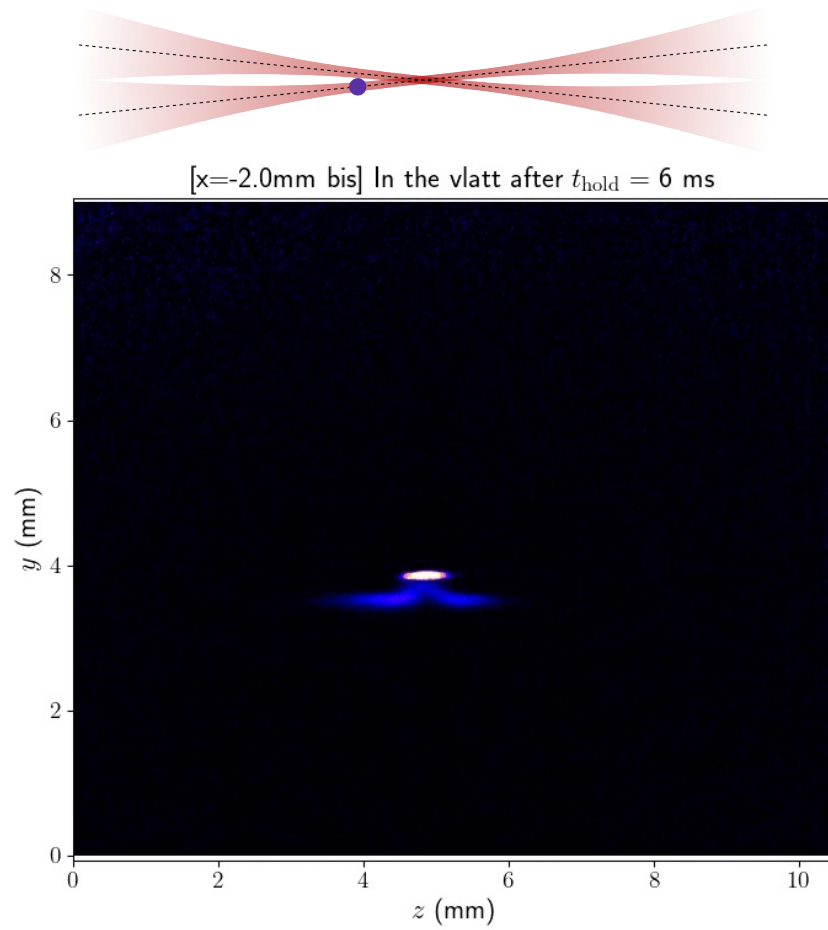


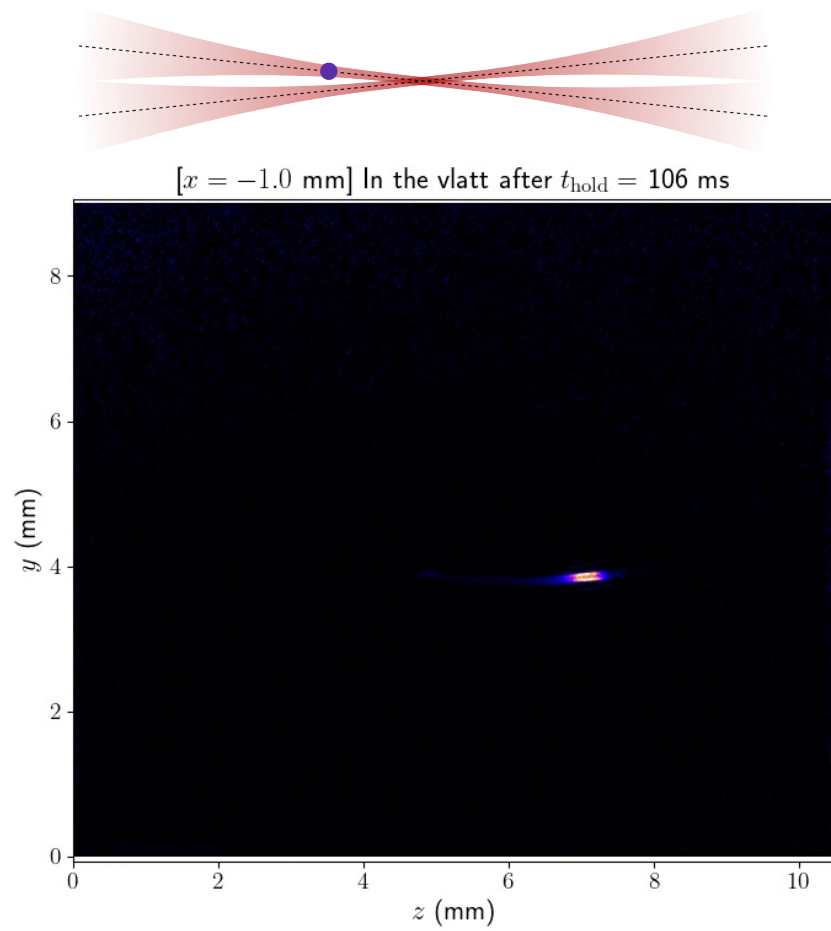
Challenge :



bad for the microscope







Cloud tightly trapped : denser ($n \nearrow$), but also hotter ($\lambda_T \searrow$) $\rightarrow$ same PSD $= n \lambda_T^3$

More laser cooling ?

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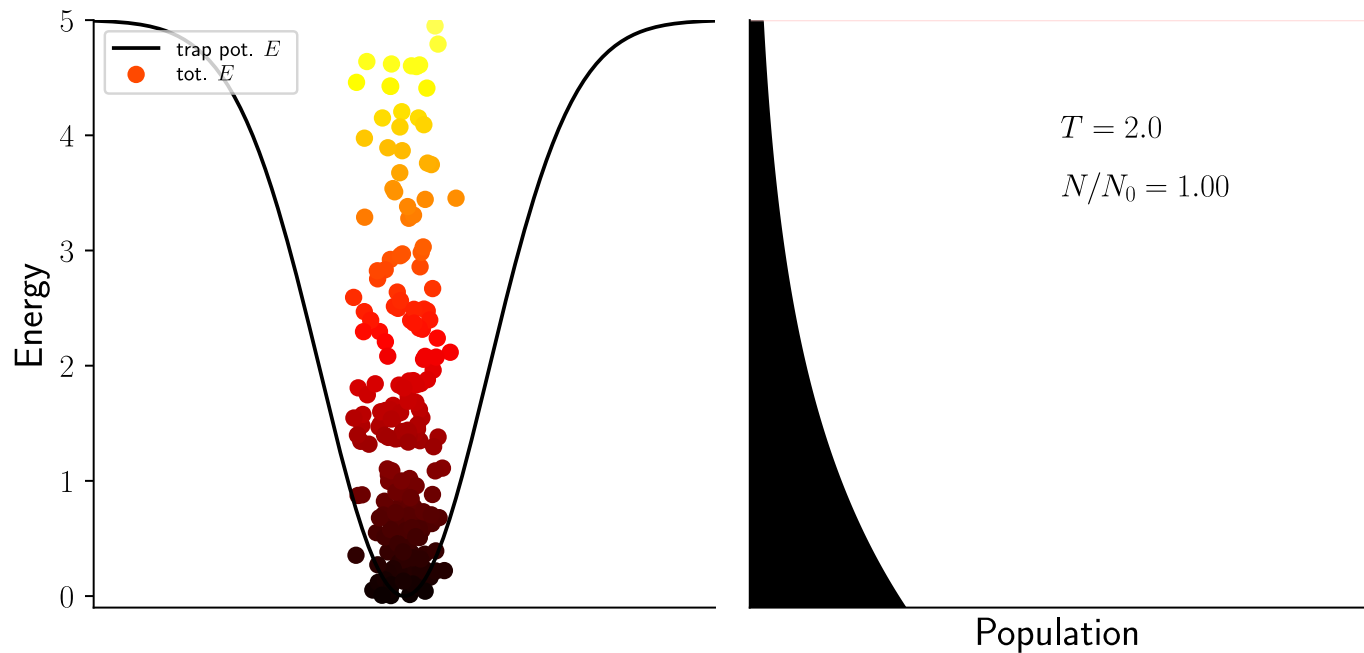
No : lossy, and not quite enough ($1 \sim 2 \mu\text{K}$ min.)

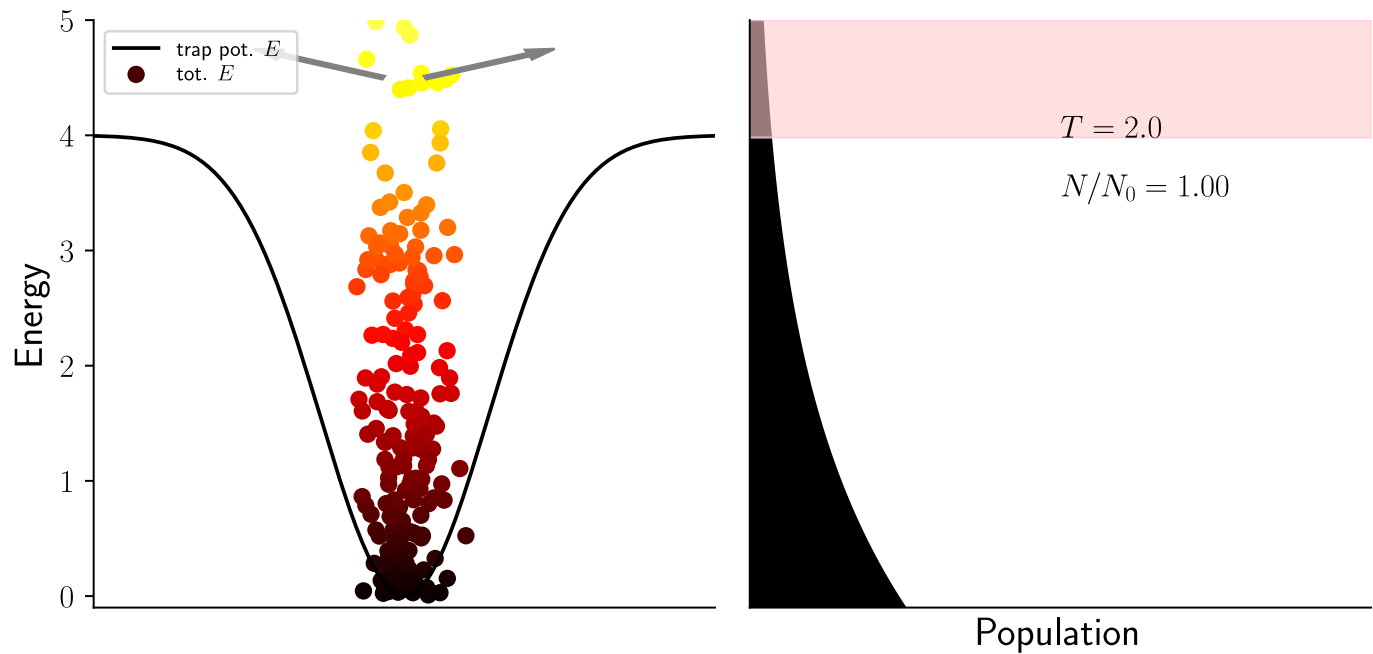
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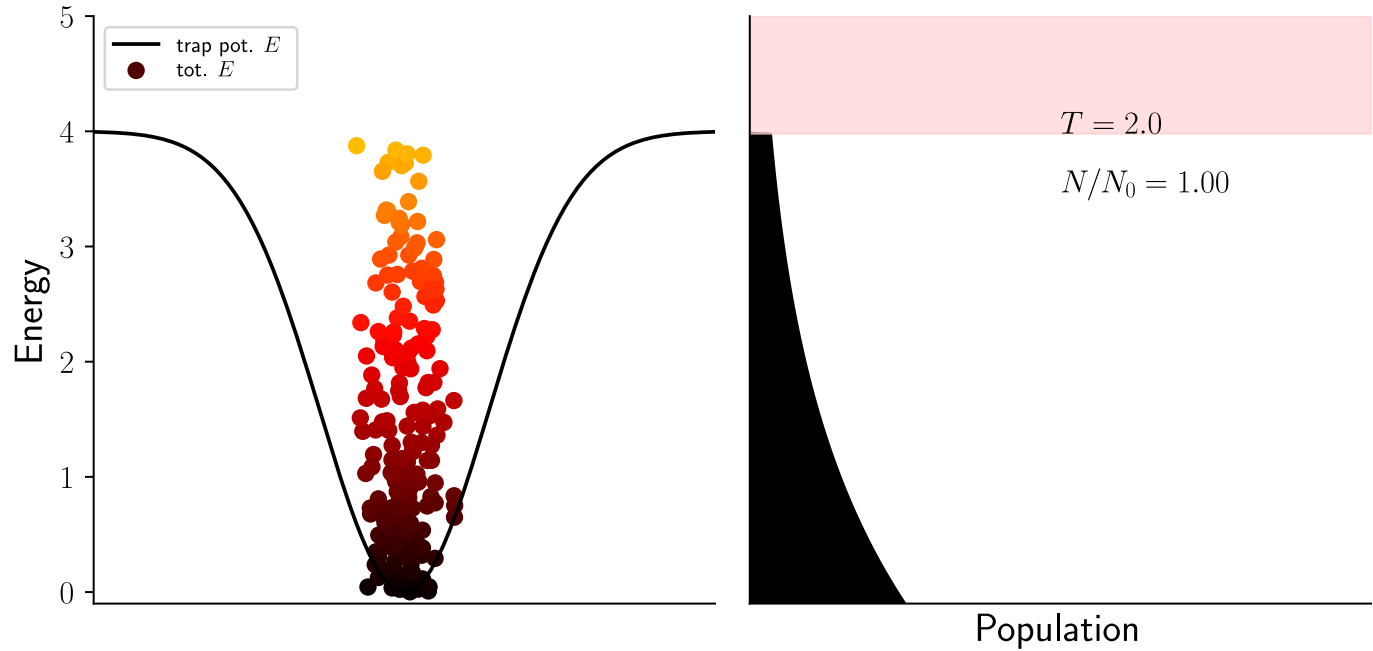
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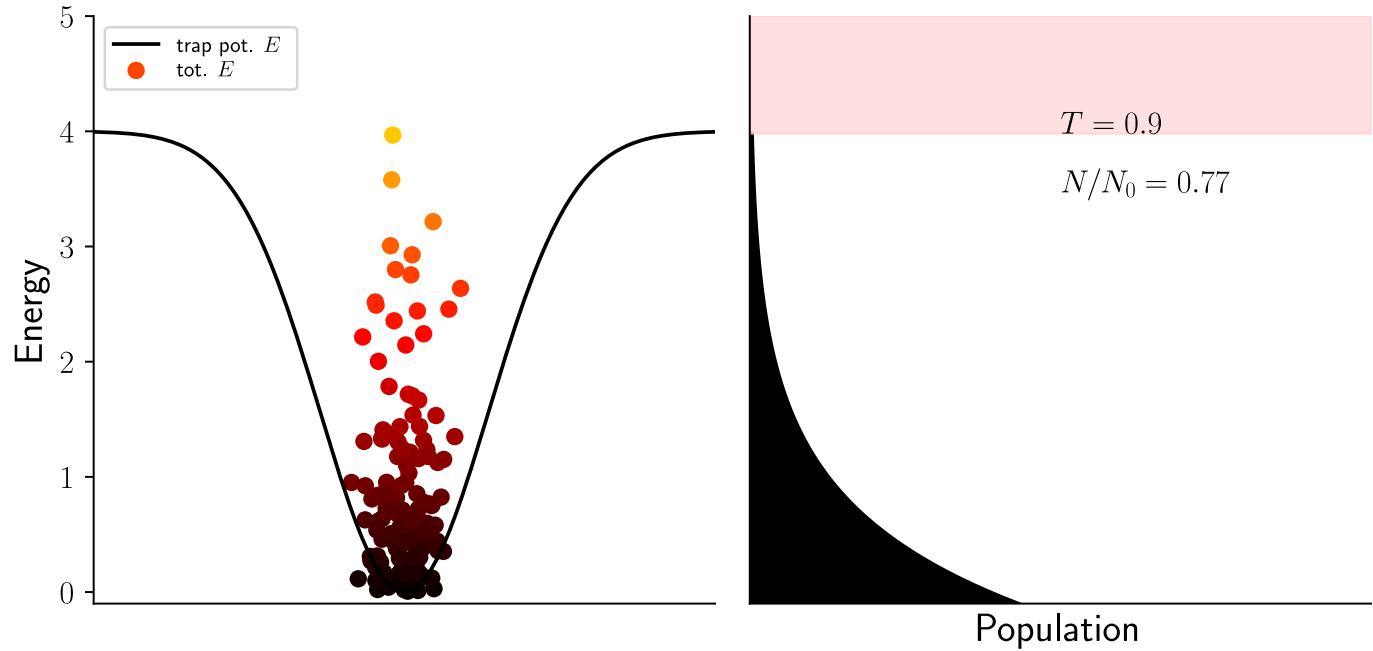
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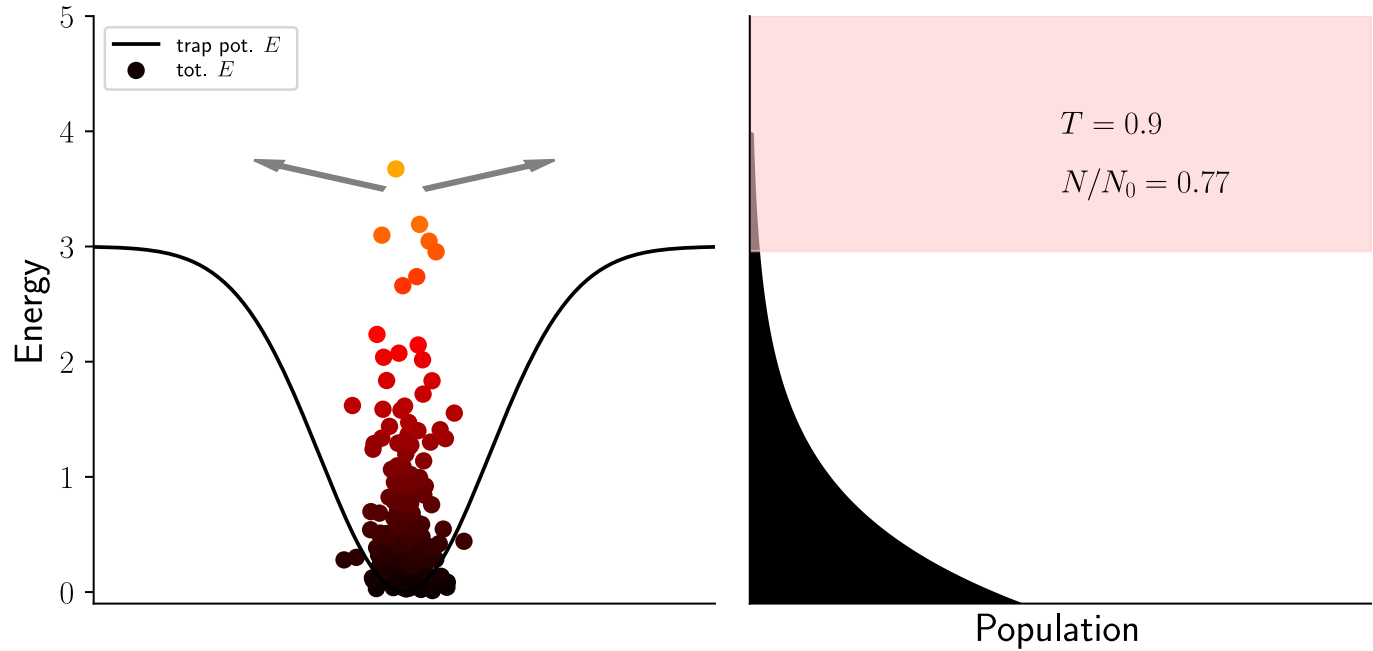
Remove hot atoms $\rightarrow$ **evaporative cooling**.

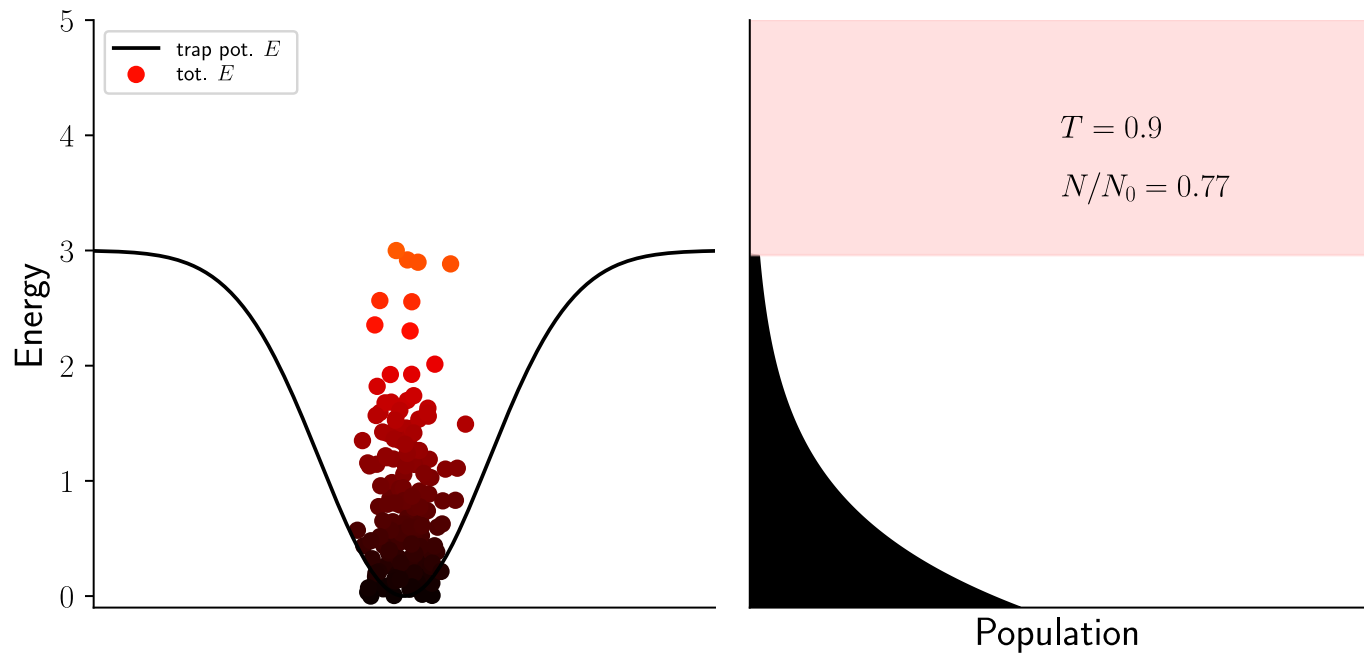


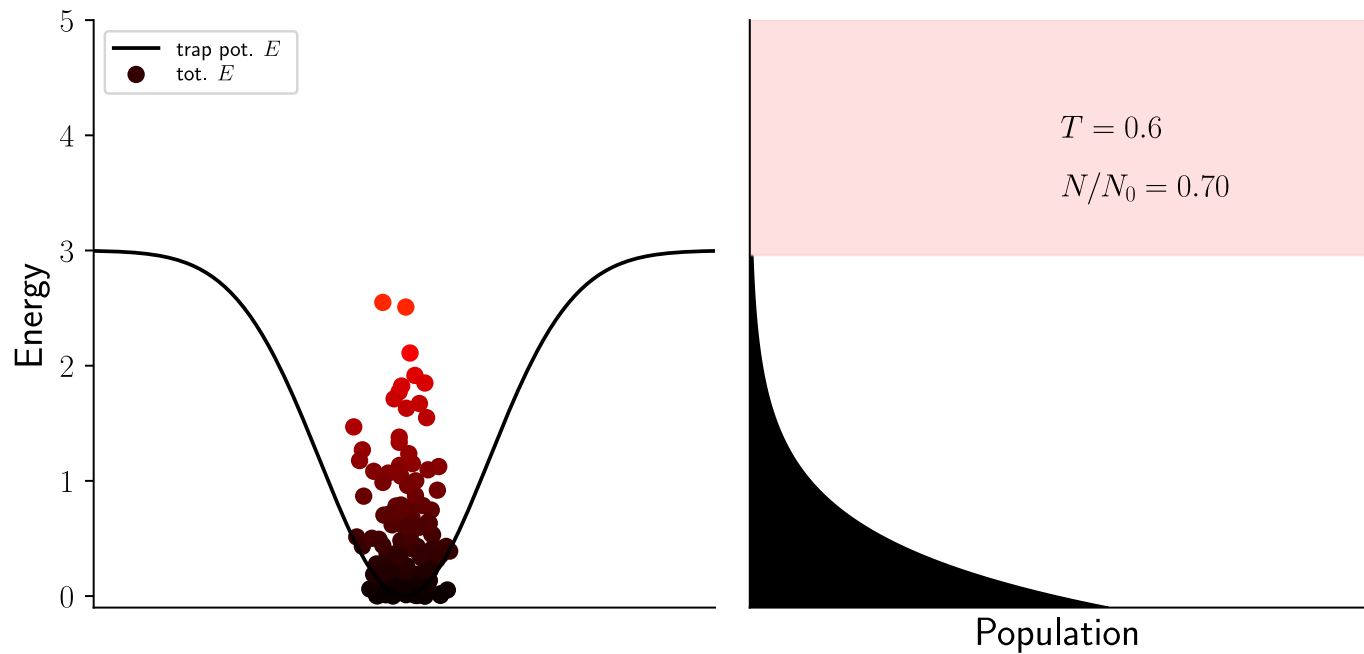


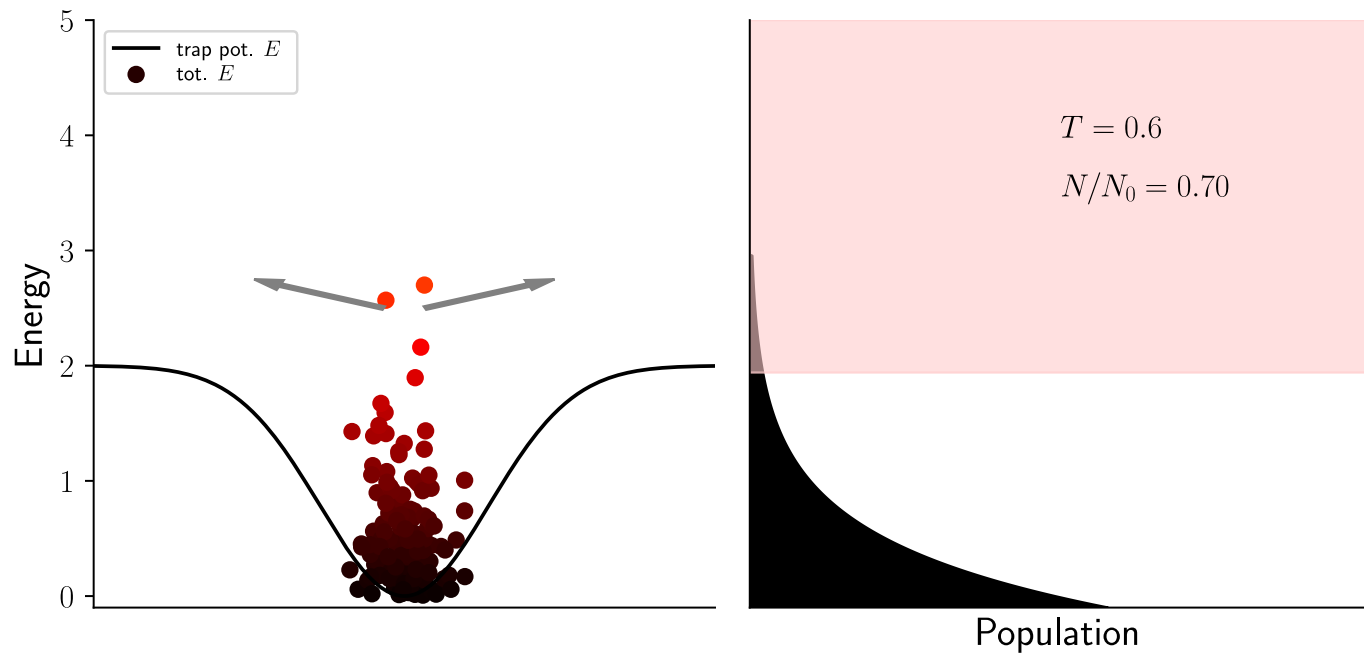


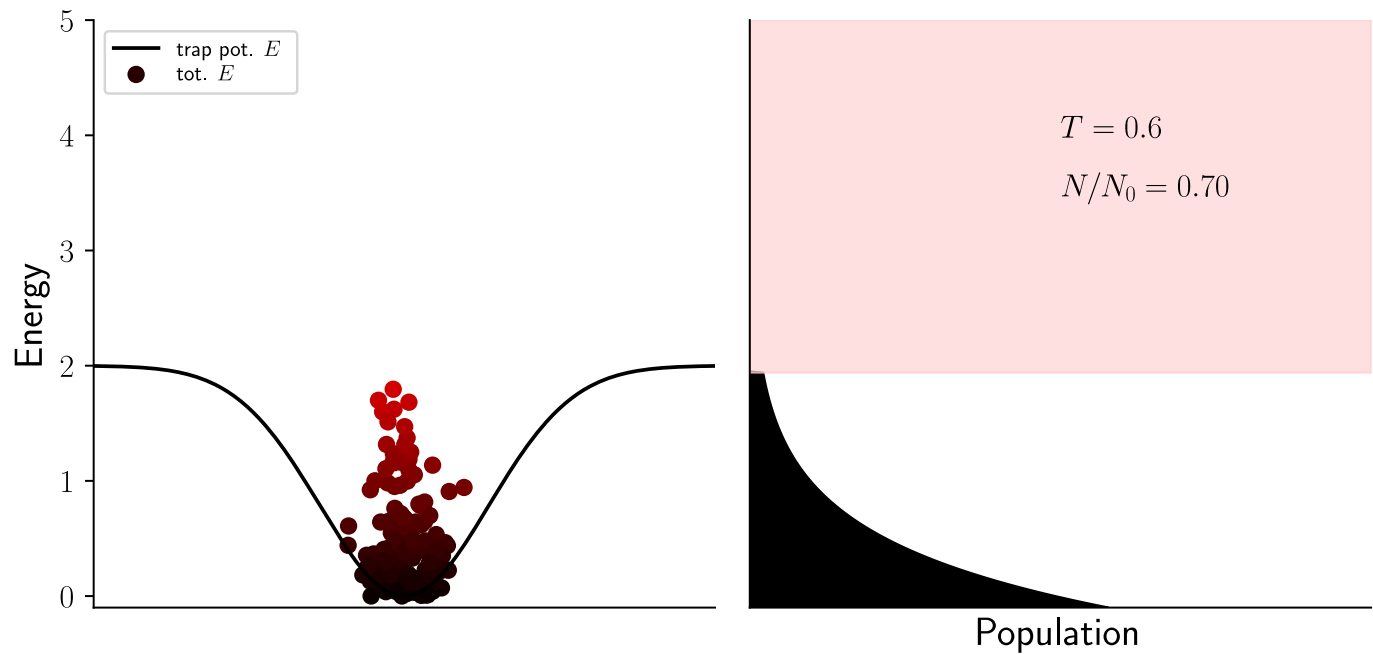


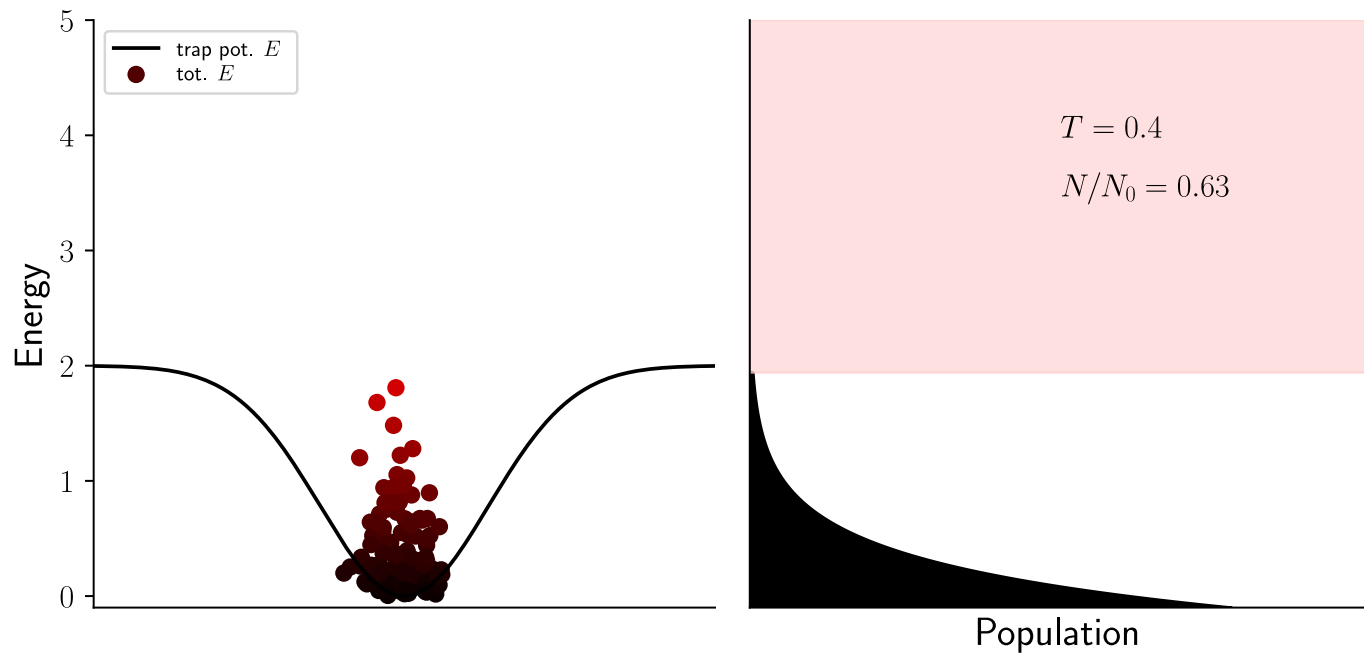


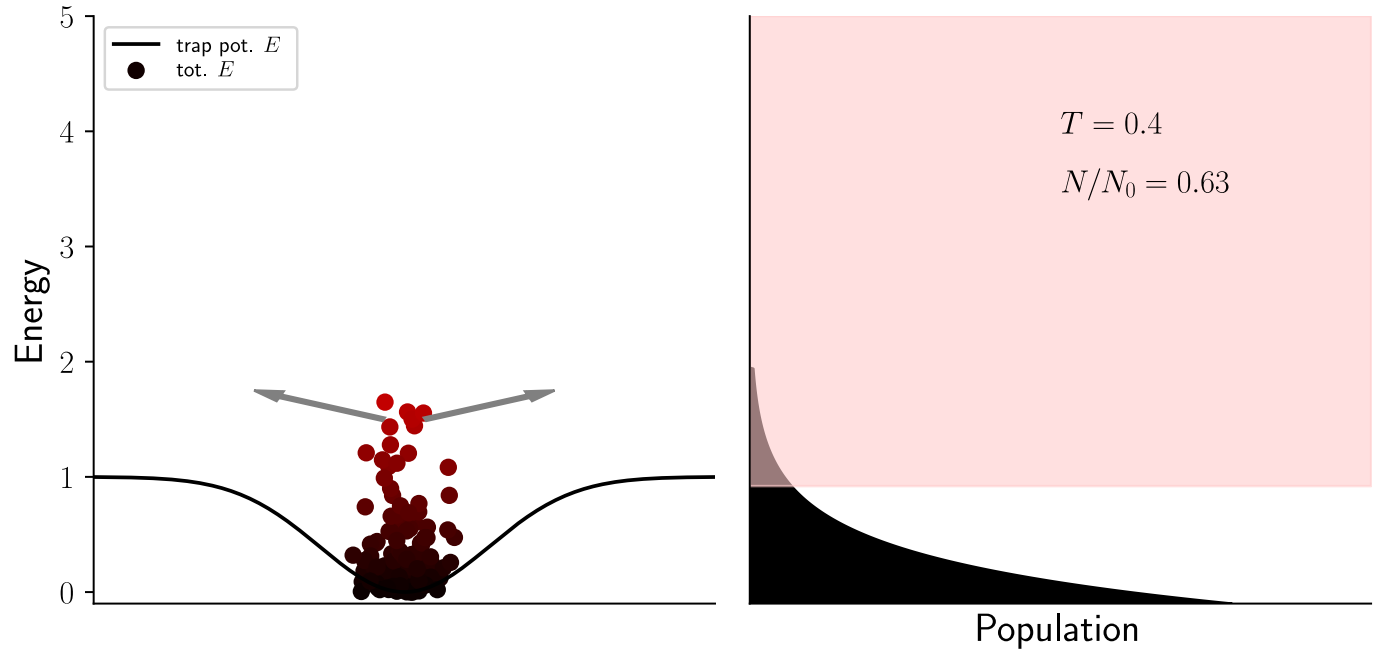


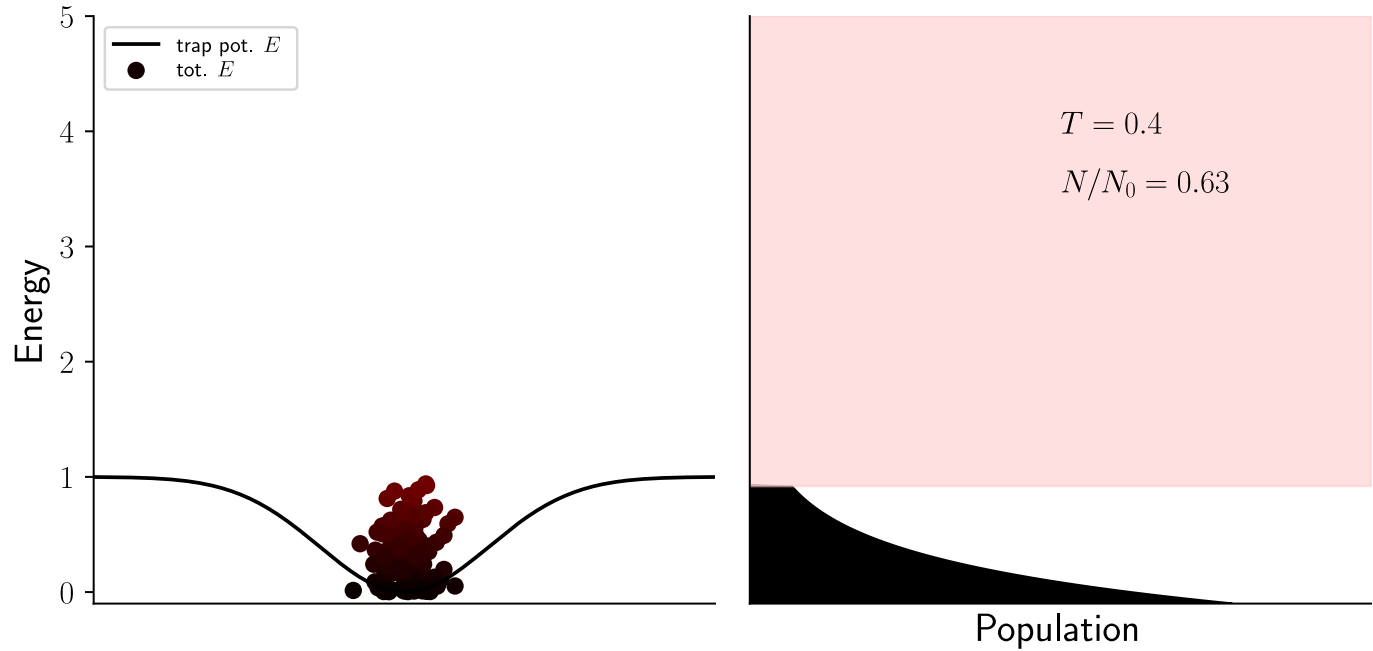


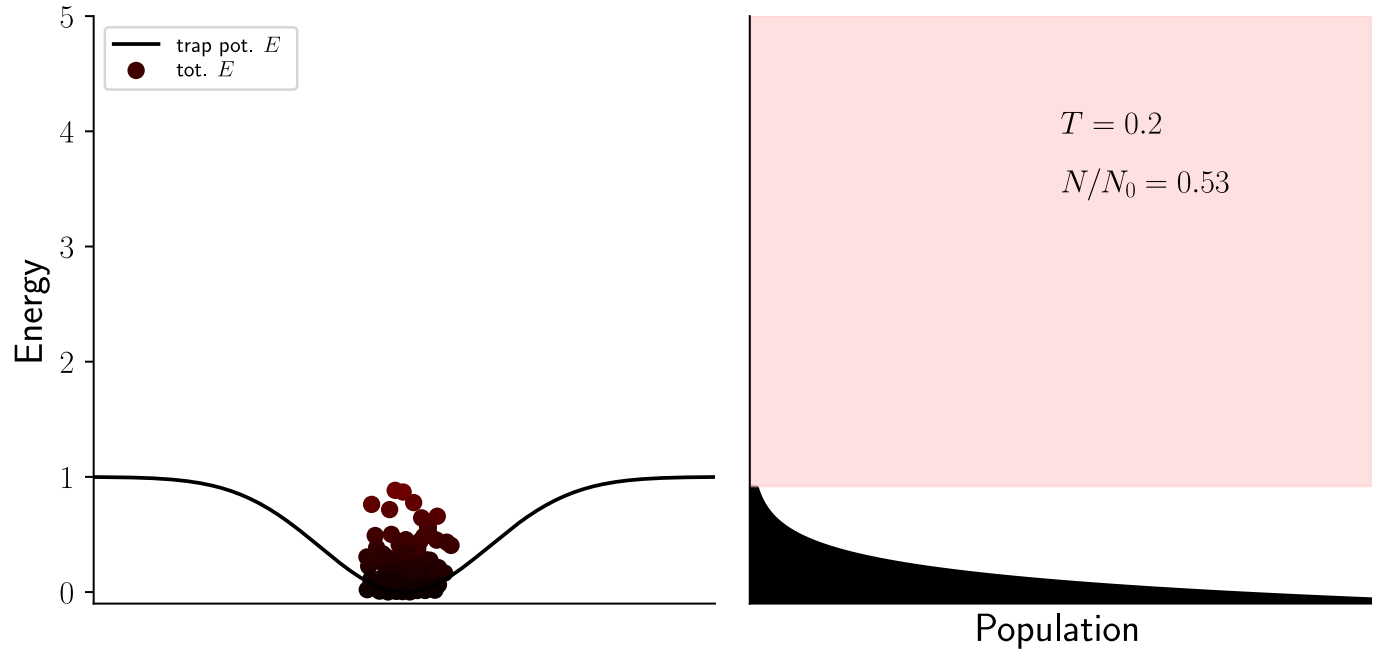












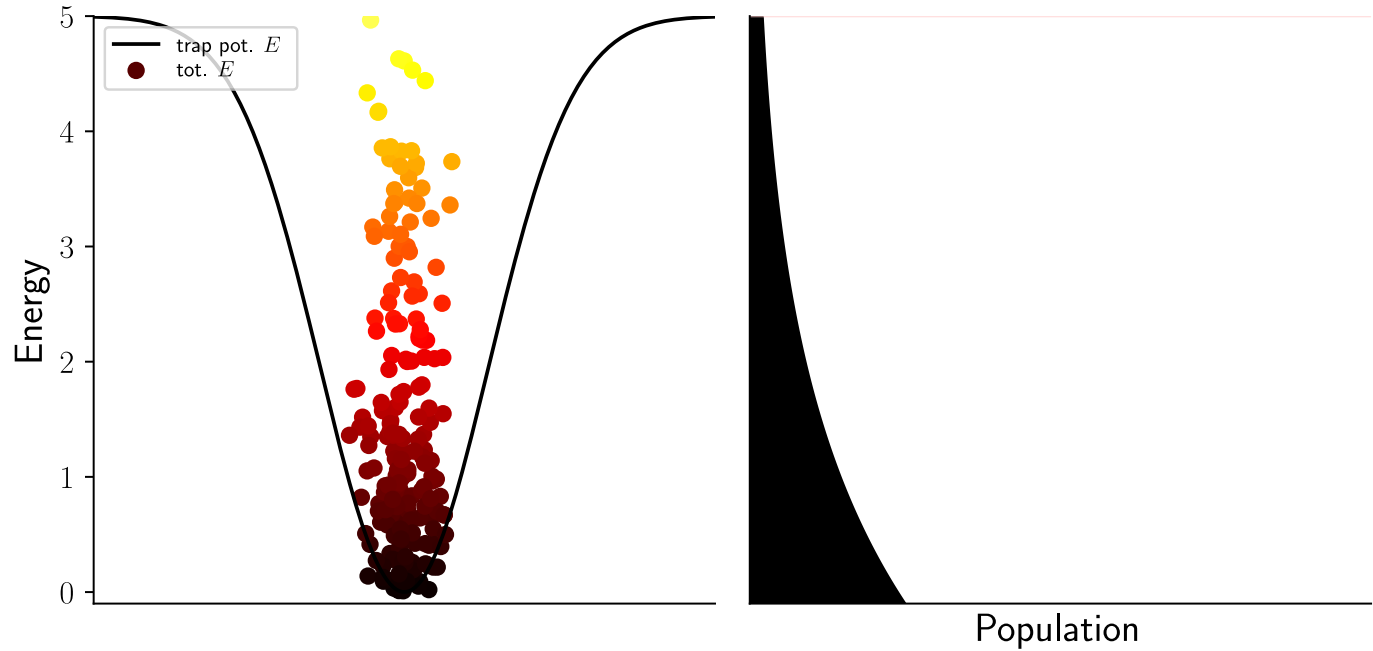
⇒ factor 10 on the temperature, factor 2 on N only !

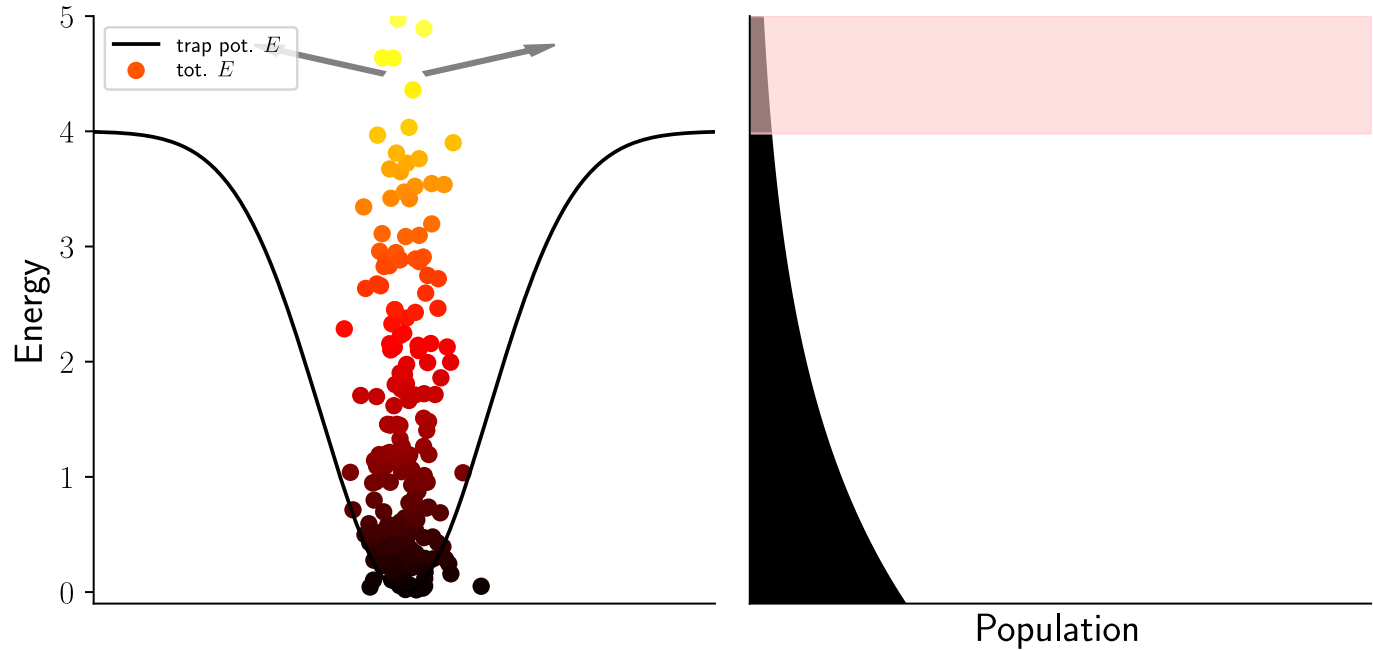
⇒ increase in phase space density

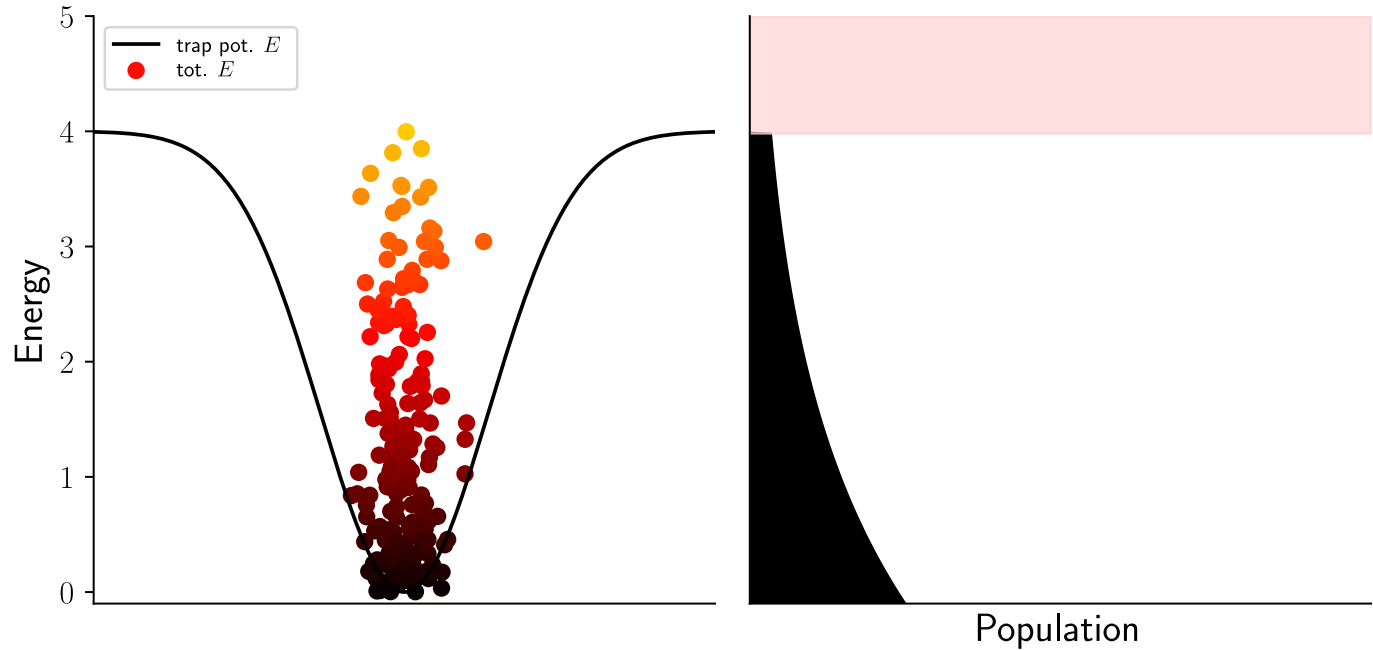
Elastic collisions must be frequent

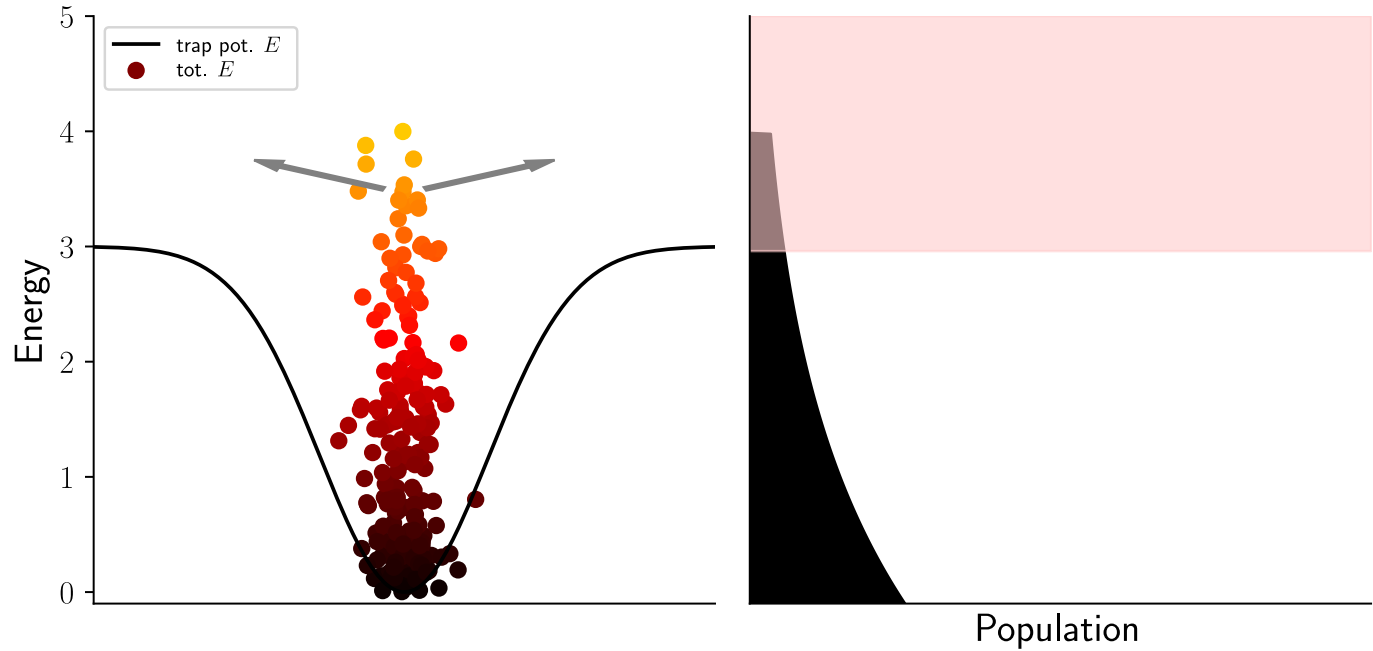
Elastic collisions must be frequent $\leftarrow$ density must be high

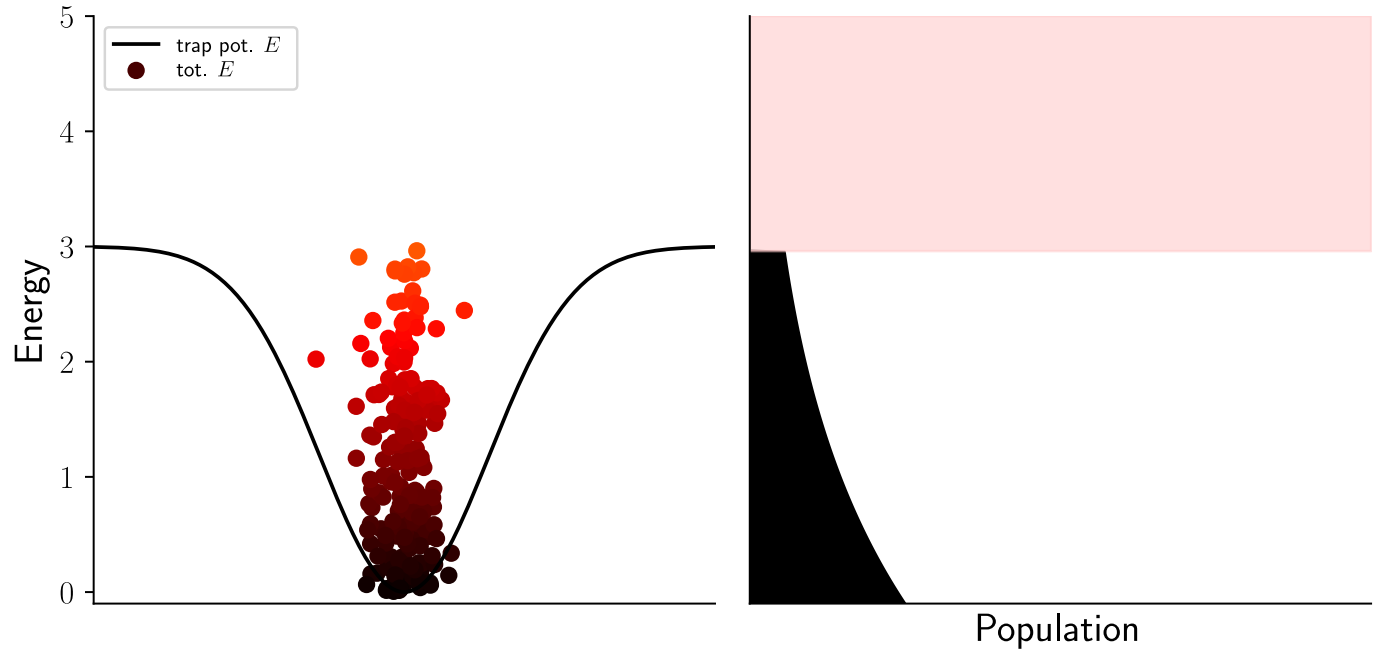
Elastic collisions must be frequent $\leftarrow$ density must be high $\leftarrow$ gas must be squeezed in a small trap

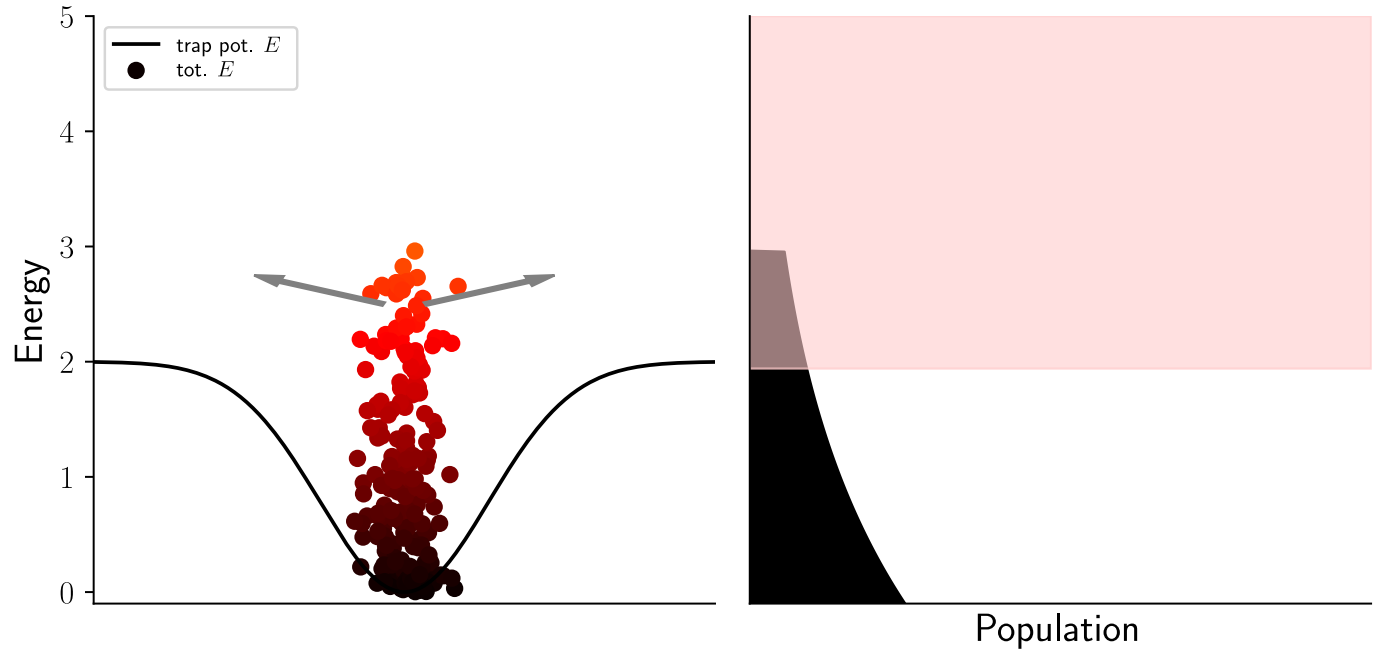


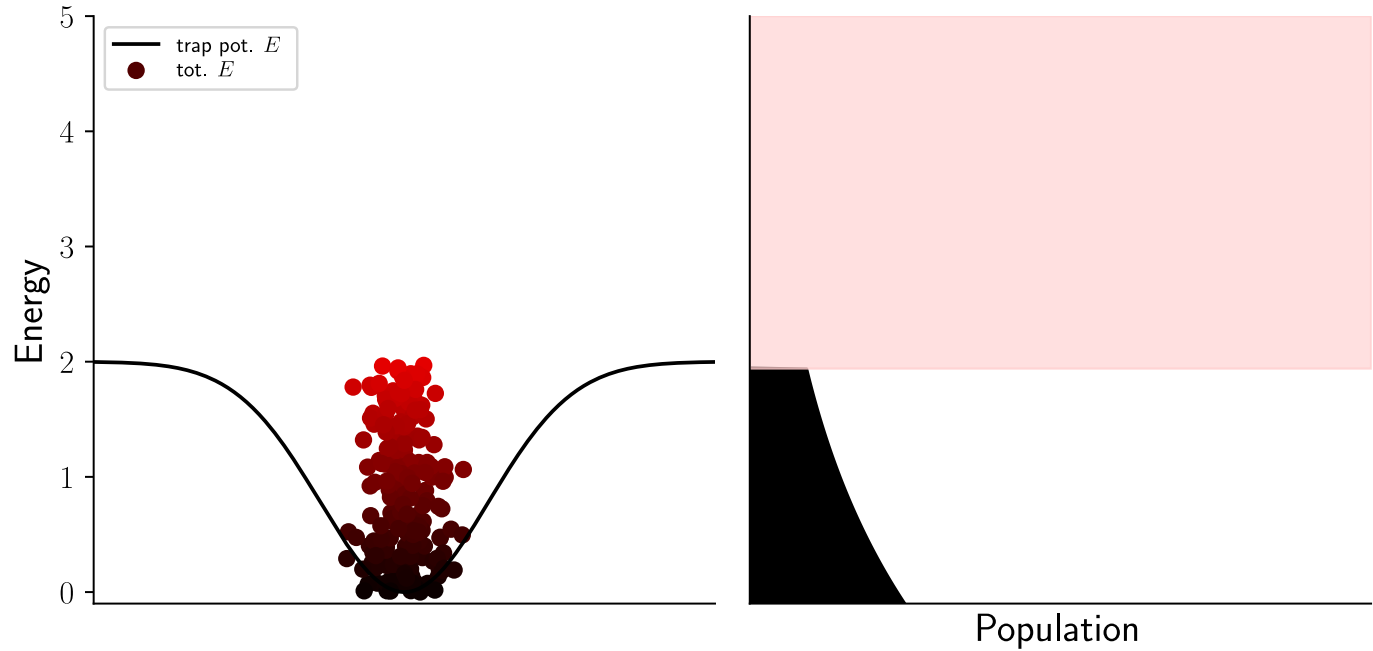


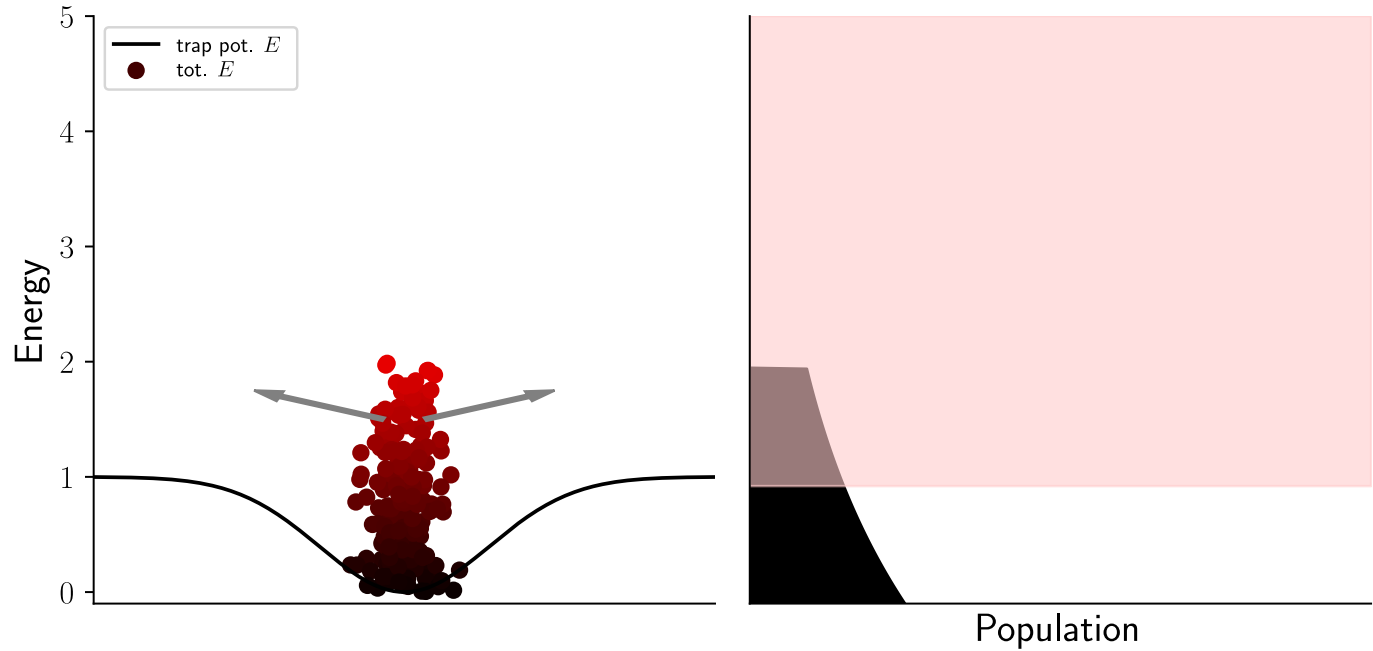


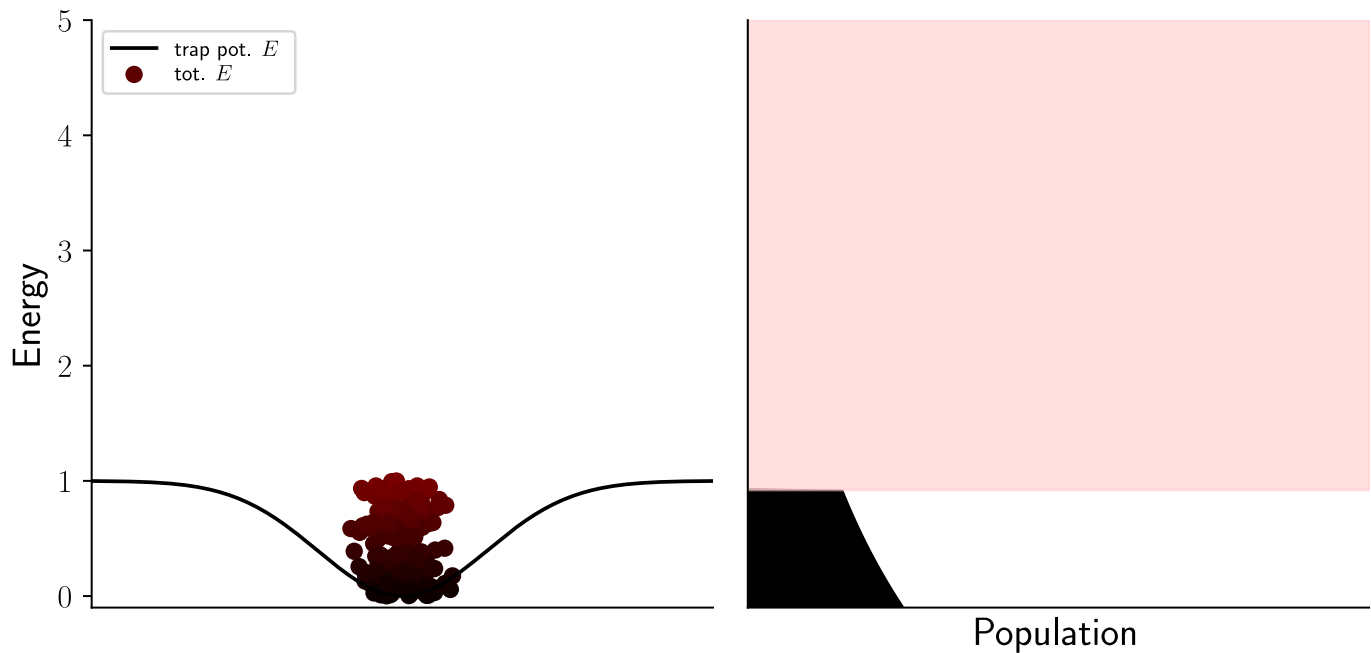












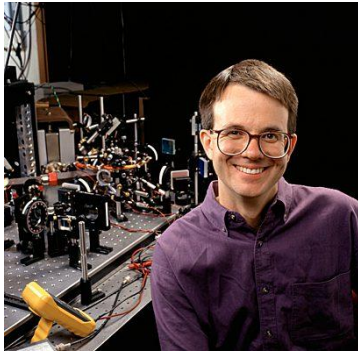
$\bar{E} \searrow$ but $n \searrow \Rightarrow$ **no** increase in phase space density

Initial works in *magnetic* traps rather than *optical* traps.

Work on evaporative cooling in the 90's, borrowed from the hydrogen community.

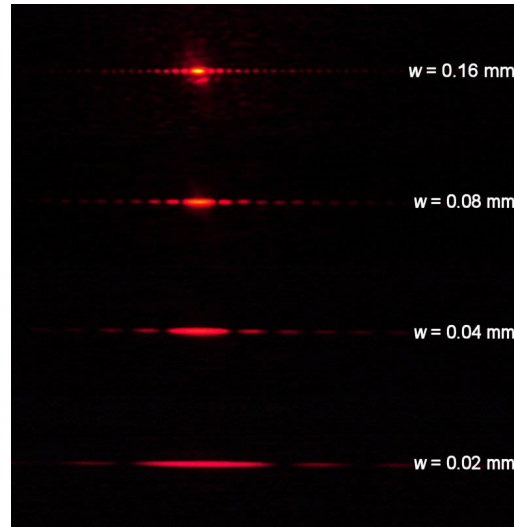
Mid. **1995** : *Bose-Einstein condensate* @ JILA, MIT and Rice within a few month (Na, Rb, Li)

Nobel prize for E. Cornell, W. Ketterle, C. Wieman



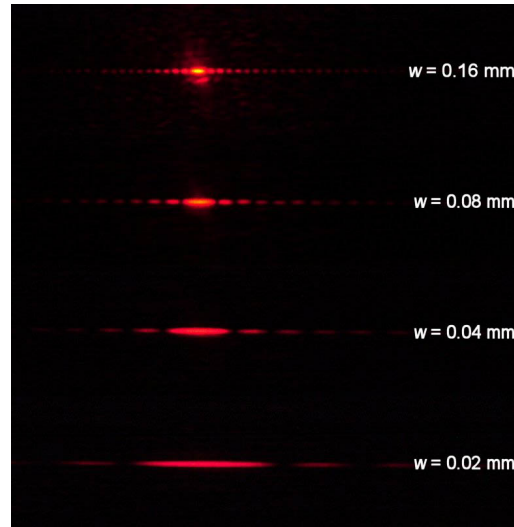
1999 : Degenerate Fermi gas (^{40}K), D. S. Jin @ JILA

Optics : slit in far field :



The **narrower** the slit, the **larger** the **far-field** diffraction pattern.

Optics : slit in far field :



*The **narrower** the slit, the **larger** the **far-field** diffraction pattern.*

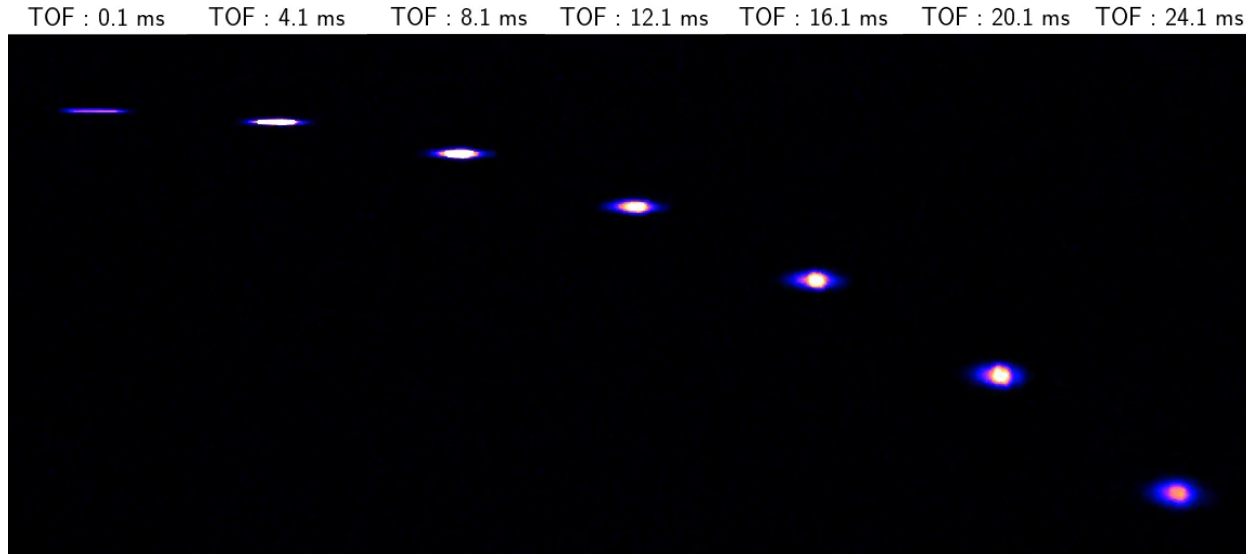
Atoms : far field = momentum-space distribution $n(\vec{p}) =$ imaging after **time-of-flight** (long enough).

→ BEC will do the same... but not thermal gases

Imaging after a time-of-flight :

$$n_{\text{after ToF}}(\vec{r}') = n_{\text{cloud}}\left(\vec{p} = m \frac{\vec{r}'}{t_{\text{ToF}}}\right)$$

($r' \gg \text{cloud size}$)



- **BEC** (not interacting $\rightarrow$ harmonic oscillator ground state) :

$$\psi_0^{1D}(x) \propto \exp\left(-\frac{m \omega x^2}{2 \hbar}\right) \quad ; \quad \text{must obey } \boxed{\Delta x \Delta p \geq \hbar/2}$$

$$\omega_x \neq \omega_y \neq \omega_z \quad \Rightarrow \quad \text{anisotropic } n(\vec{p})$$

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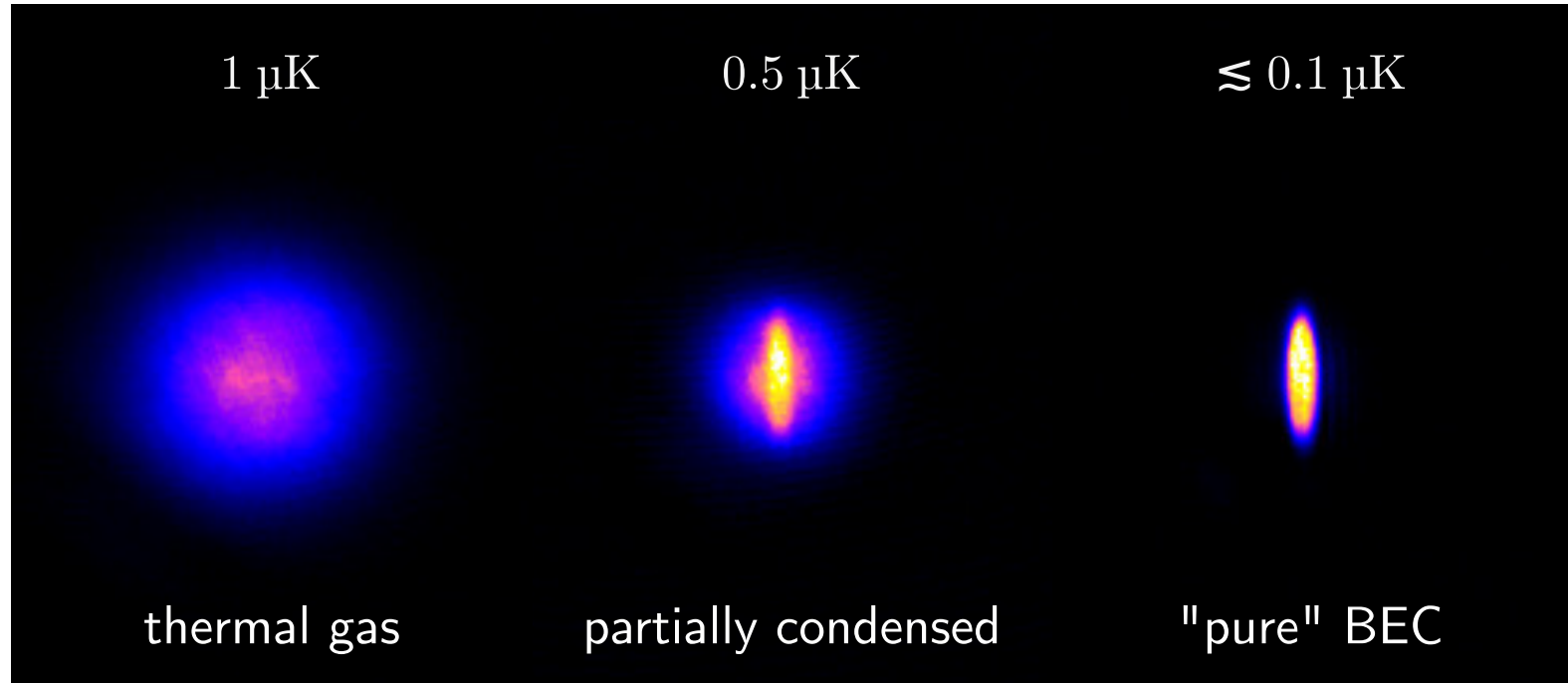
$$\omega_x \neq \omega_y \neq \omega_z \Rightarrow \text{anisotropic } n(\vec{p})$$

- **Thermal cloud** in harmonic potential (Boltzmann distrib. approx.) :

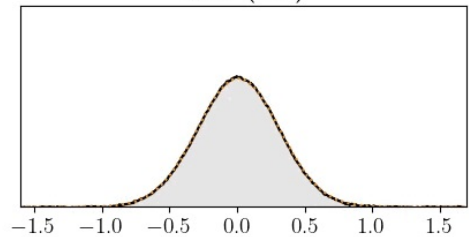
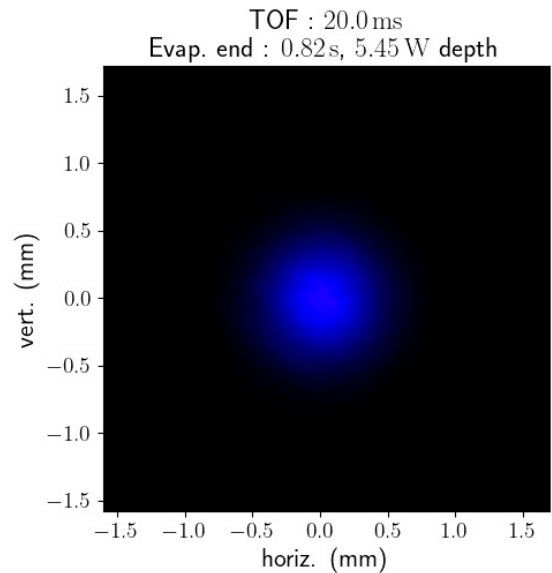
$$H = \frac{1}{2m} p^2 + \frac{m \omega^2}{2} x^2 \Rightarrow n(\vec{x}, \vec{p}) \propto e^{-H(x,p)/k_B T} \Rightarrow \boxed{n(\vec{p}) \propto \exp\left(-\frac{p^2}{2 m k_B T}\right)}$$

... does not depend on the confinement ω , **same along x , y , z .**

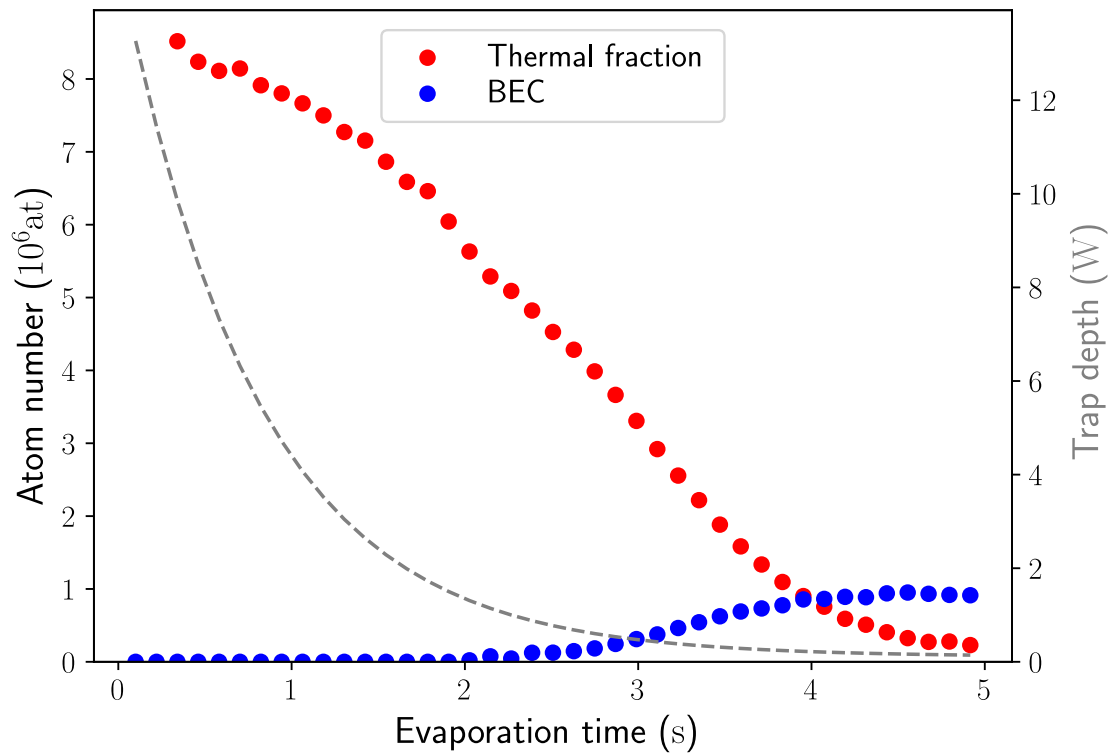
Thermal gas	BEC
$\Delta p_i \propto T$	$\Delta p_i \propto \frac{1}{\Delta x_i} \propto \text{confinement along } i$

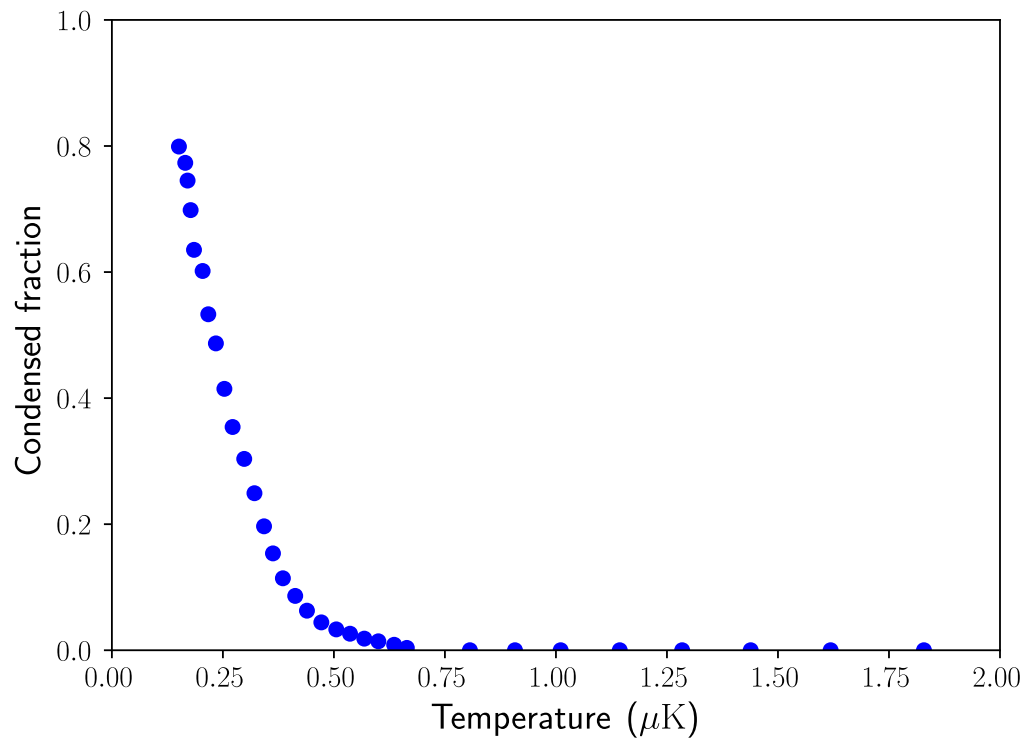


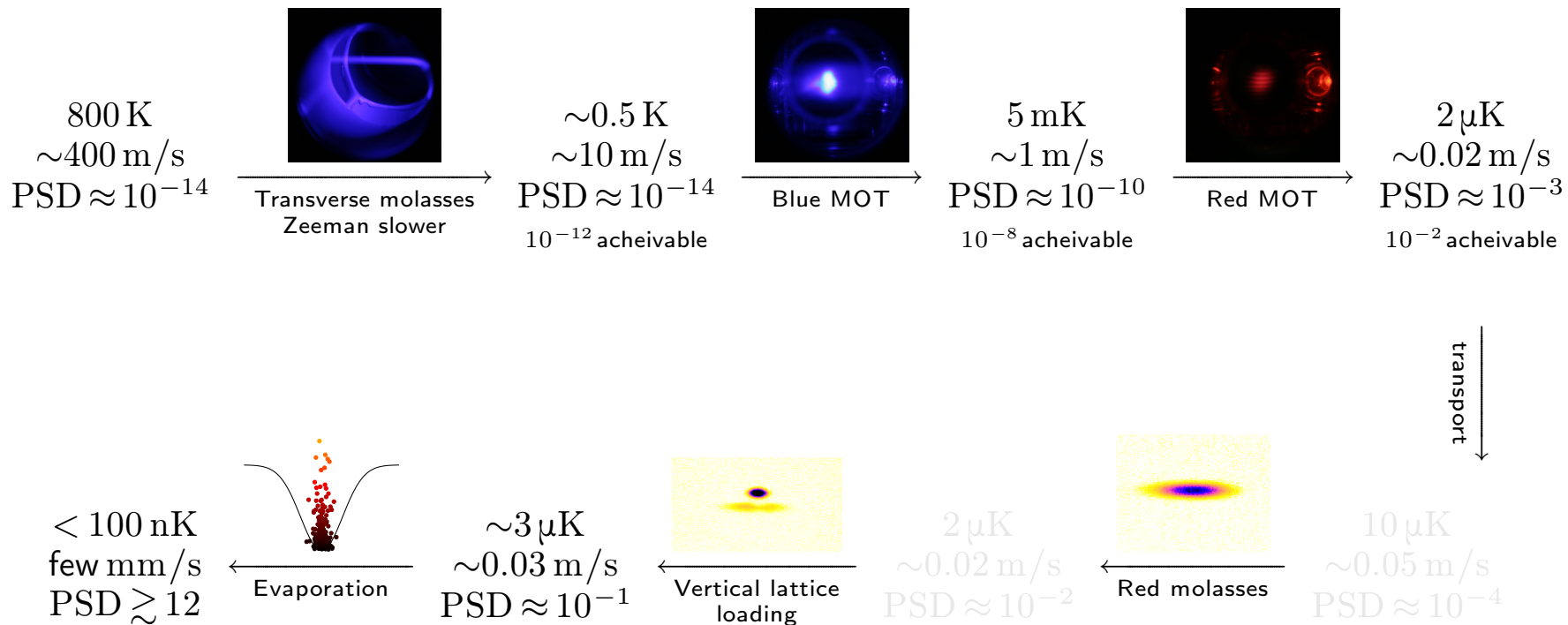
After TOF : $n(p)$ $\longrightarrow$



momentum
space
really

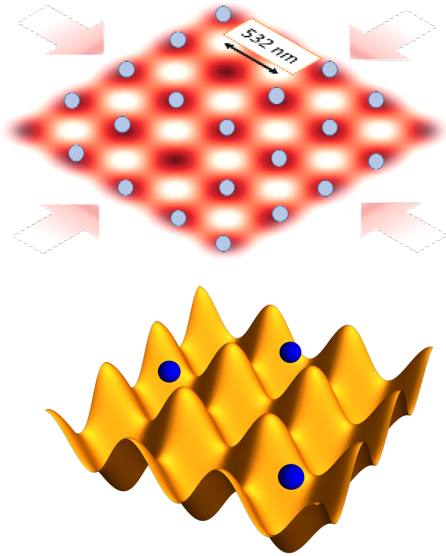


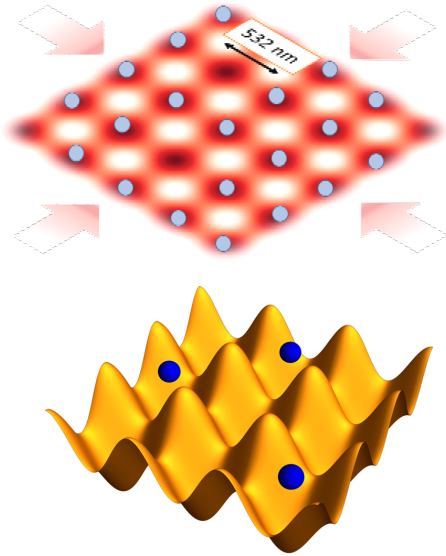




1. Degenerate atomic gases (as analogues?)
2. Laser cooling
3. Evaporative cooling
4. **Bose-Hubbard physics**

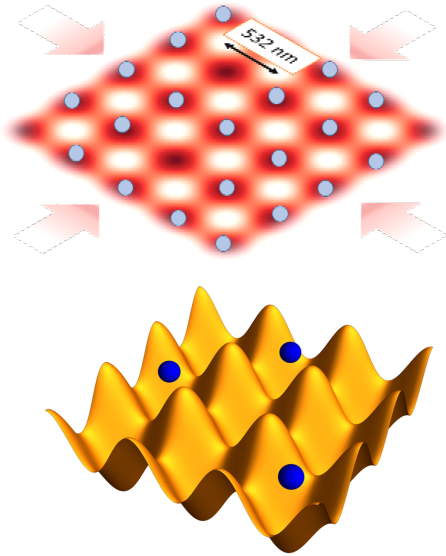
Put the 2D condensate in a periodic potential (**square optical lattice**)





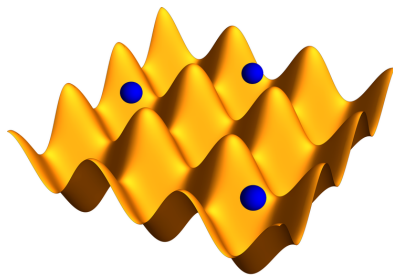
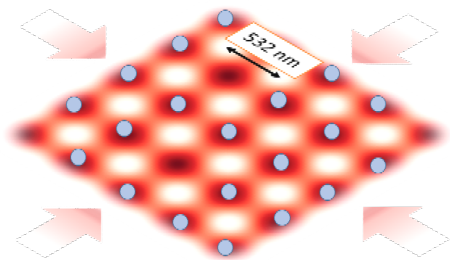
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 → **Bose-Hubbard model**

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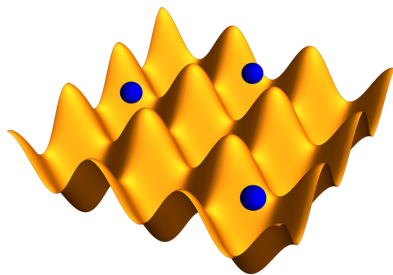
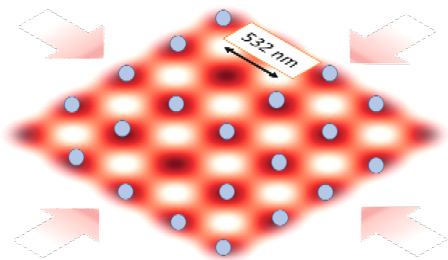
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delocalization
for kin. energy lowering



prevents
delocalization



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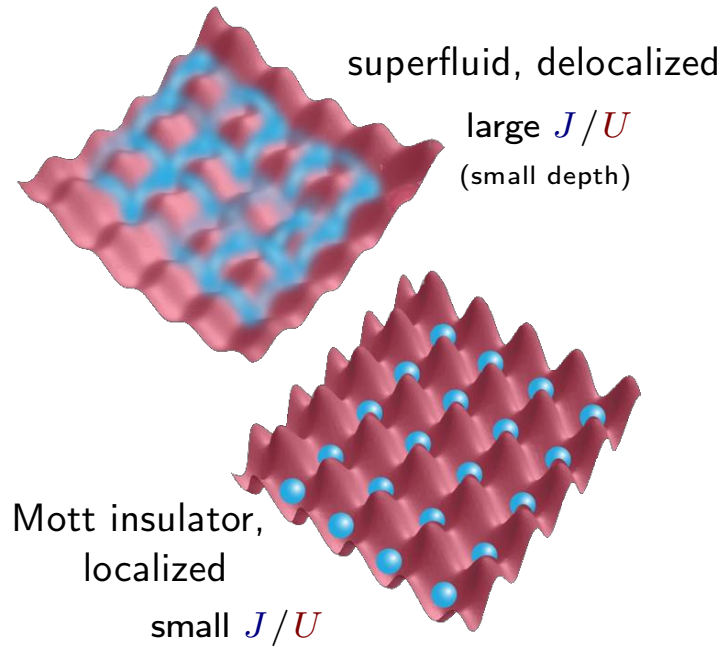
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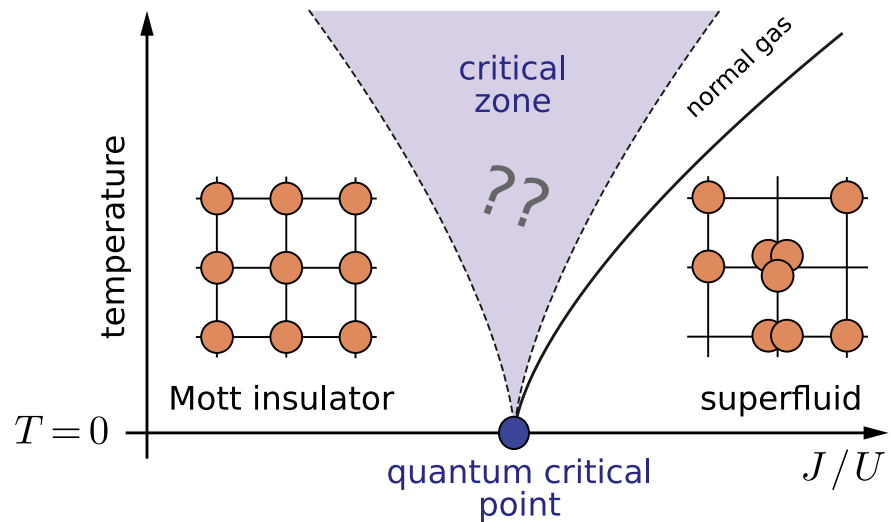
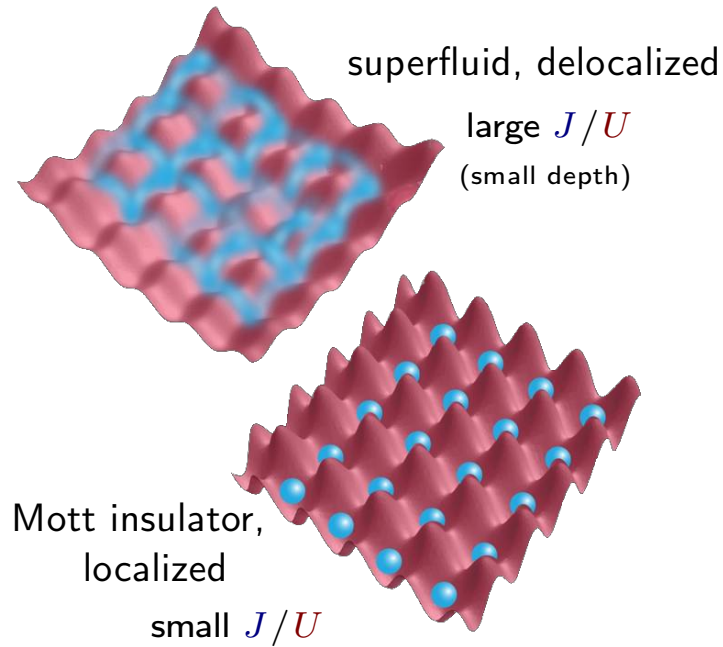


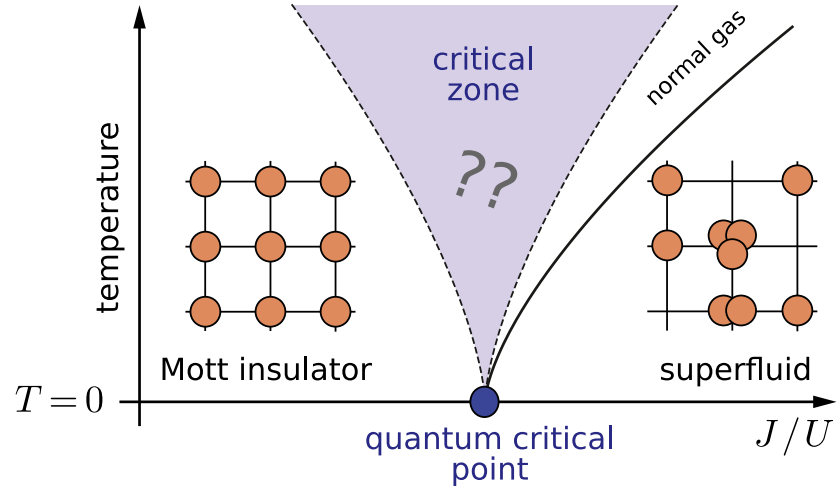
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⇒ delocalization / localization **competition**, controlled by $U/J = f(\text{lattice depth})$

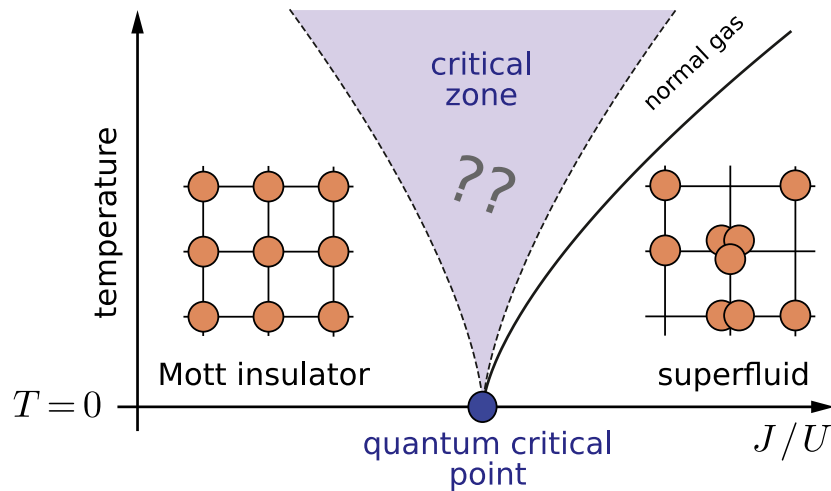
⇒ phases & quantum phase transition



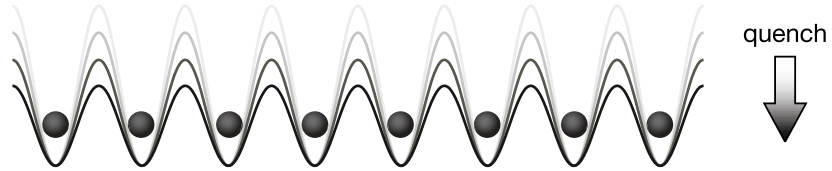


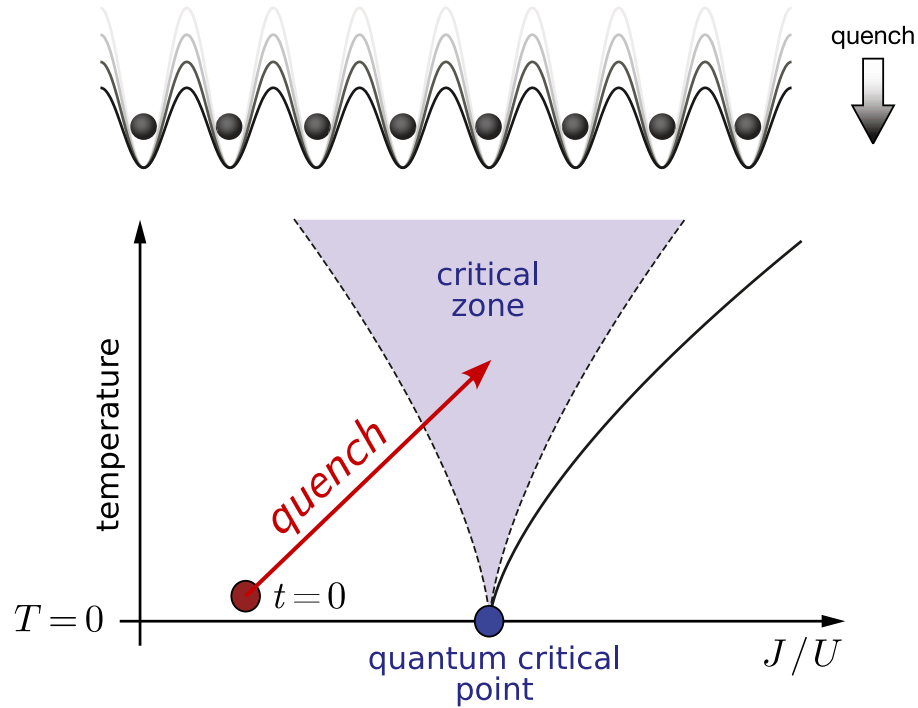


→ Outside of critical zone, **excitations = quasi-particles** (doublons-holons / phonons)



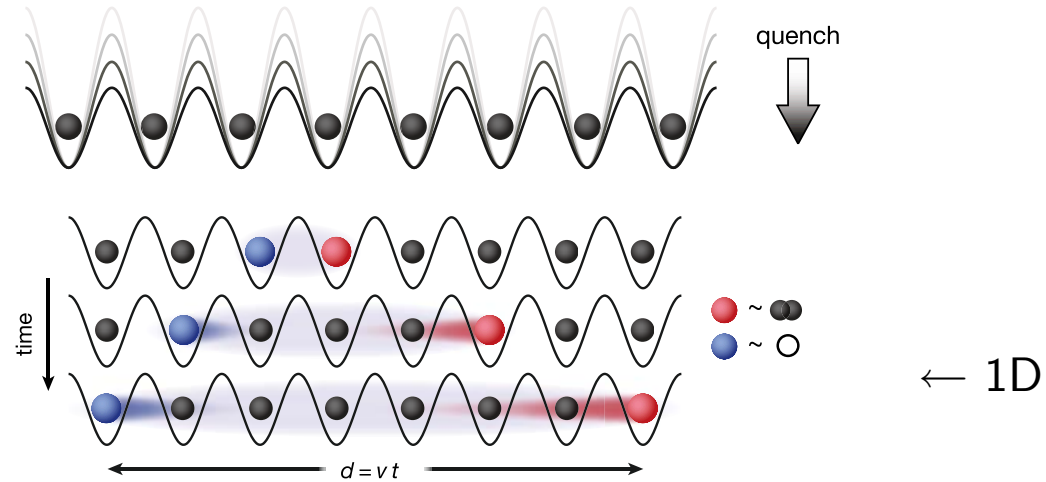
- Outside of critical zone, **excitations = quasi-particles** (doublons-holons / phonons)
- But *no long-lived quasi-particles* in the critical zone !
(2D-specific)
- What are the excitations then ?



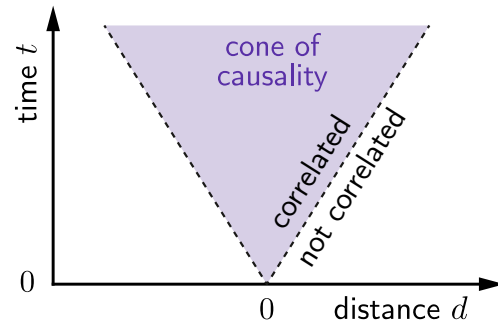
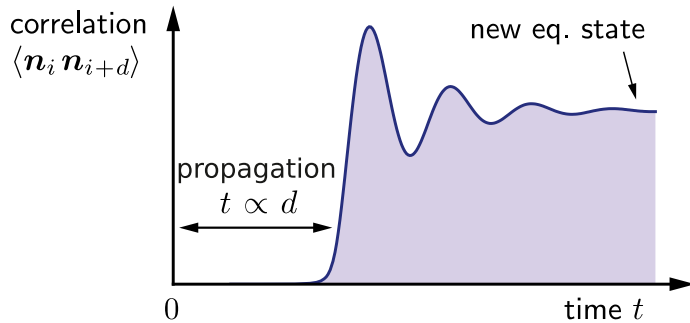
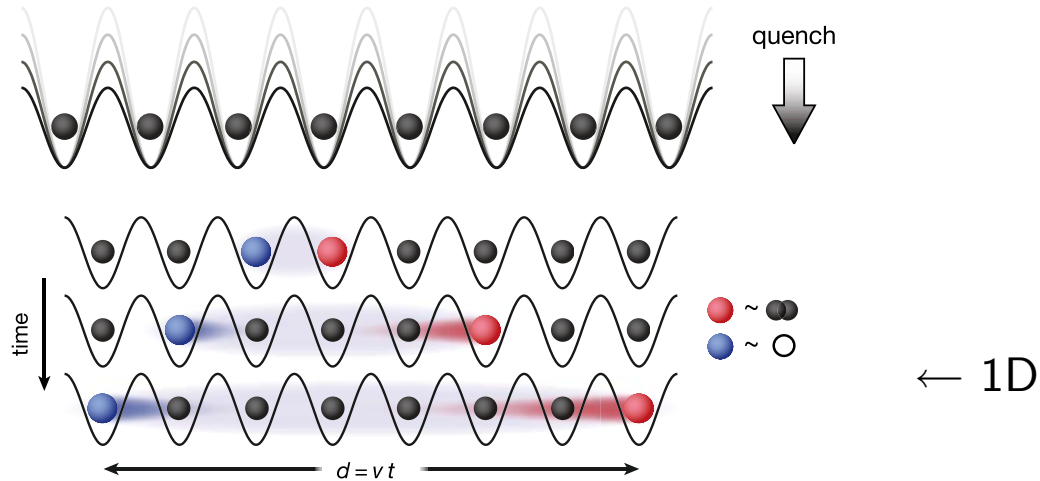


Relaxation :

Thermalization ? Final state ? How fast ?



Correlation $\langle n_i n_{i+d} \rangle$ after a delay t ?



When $\exists$ long-lived quasi-particles (eg. deep in insulator or superfluid) :

- correlation spreading = q-p propagation
 - speed = q-p group velocity

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When $\nexists$ long-lived quasi-particles (eg. critical zone) :

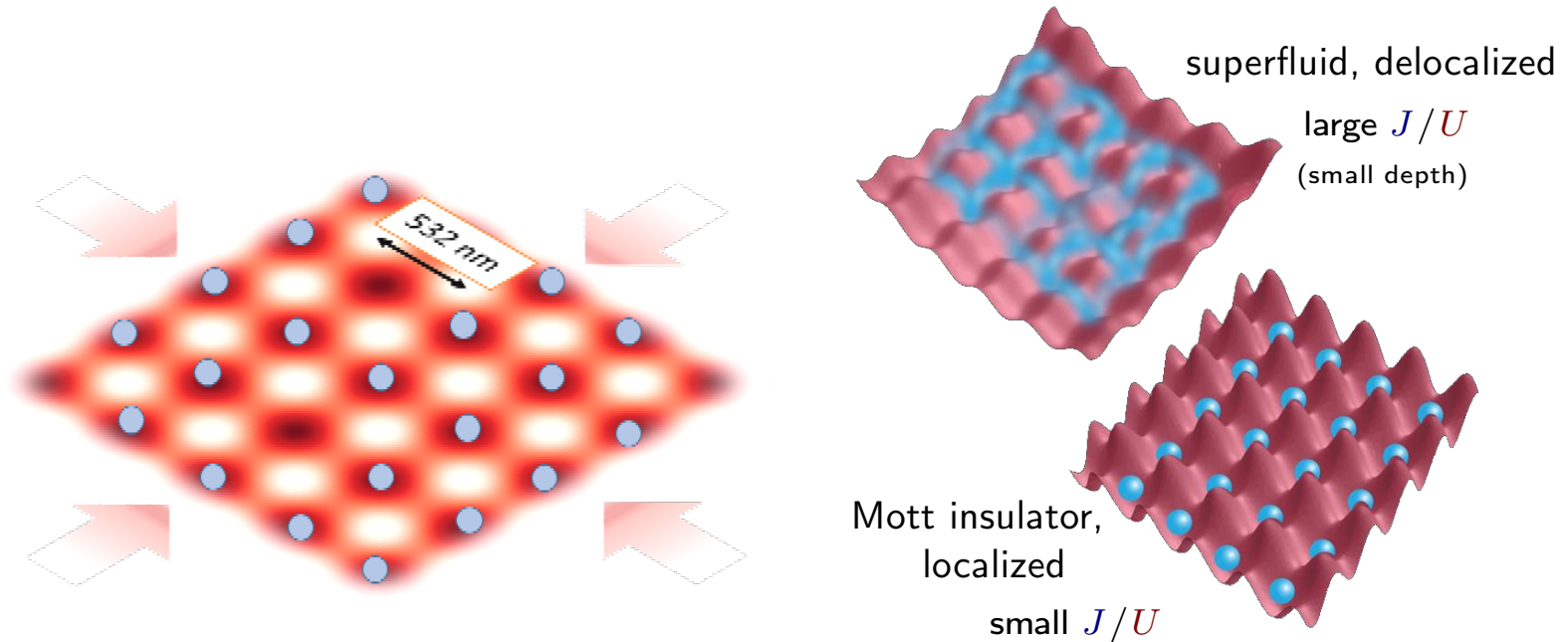
???

ballistic ? diffusive ? ...

→ let's look experimentally !

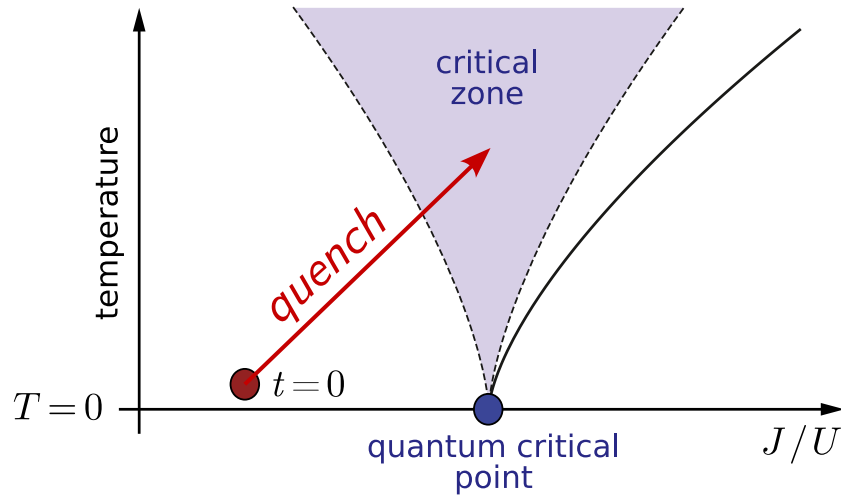
BEC : only the starting point.

1. Make it strongly interacting $\rightarrow$ optical lattice; many-body quantum system



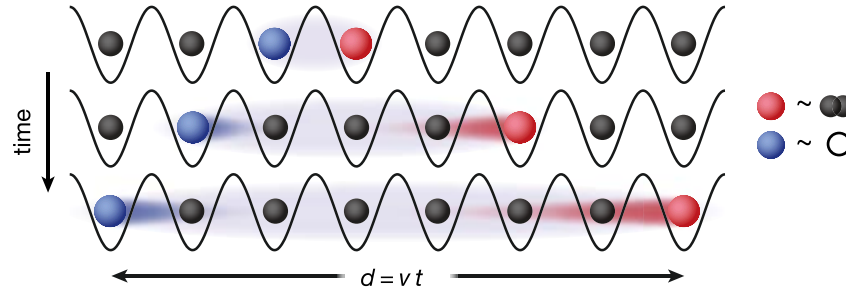
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2. Put it out-of-equilibrium $\rightarrow$ sudden change of parameter



BEC : only the starting point.

1. Make it strongly interacting $\rightarrow$ optical lattice
2. Put it out-of-equilibrium $\rightarrow$ sudden change of parameter
3. Observe how n -body correlations propagate spatially in the system

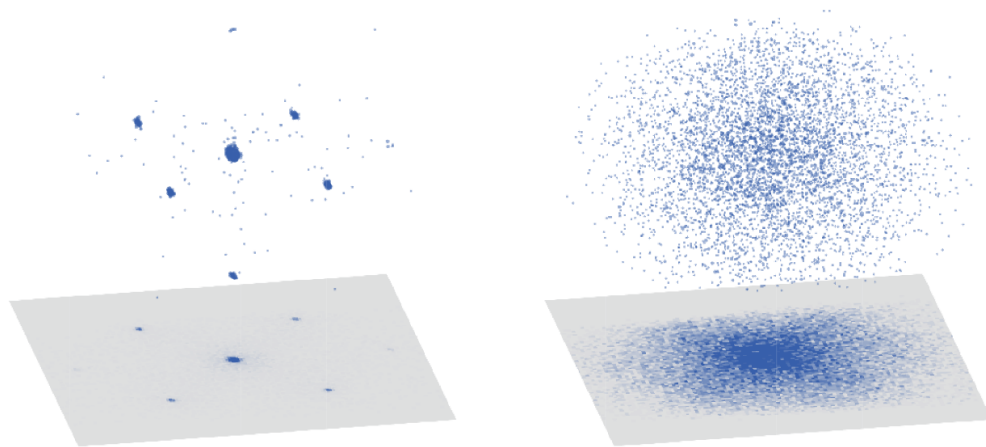


With density/momentum profiles, we can only access **1-body** correlation functions ($\langle \mathbf{n}(\vec{p}) \rangle \langle \mathbf{n}(\vec{p}') \rangle \dots$)

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We want **2-body** (or more) correlation functions ! Only possible with **single-particle detection**

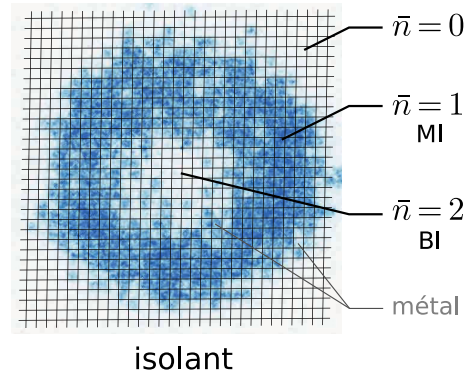
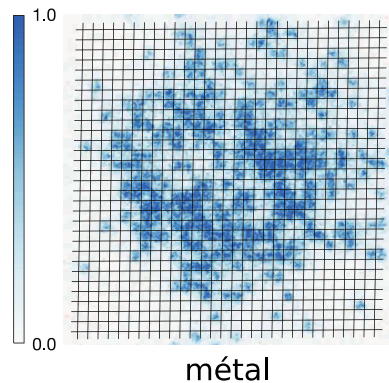
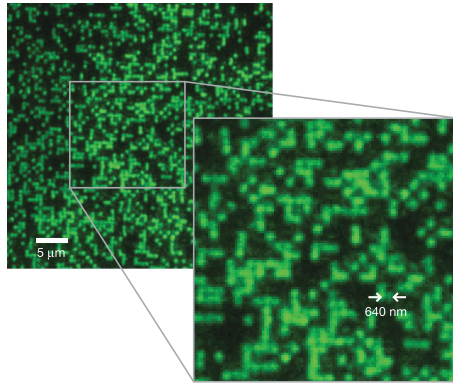
- Time-of-flight $\rightarrow$ MCP $\rightarrow \langle \mathbf{n}(\vec{p}) \mathbf{n}(\vec{p}') \rangle$ (He* experiments @ LCF)

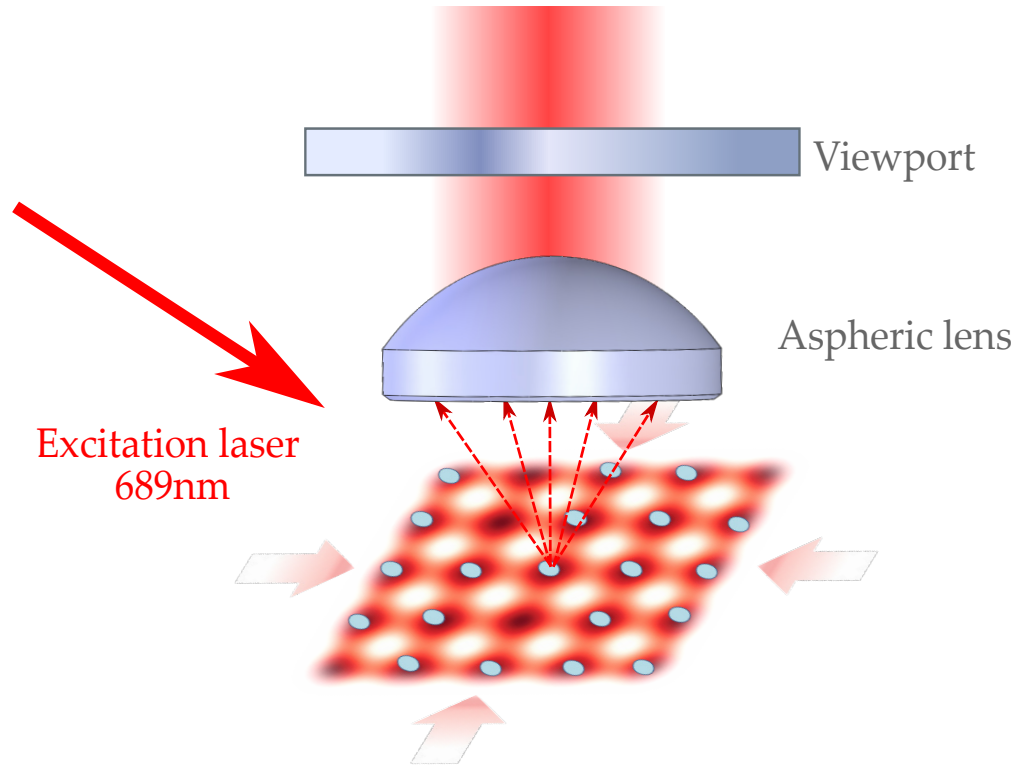


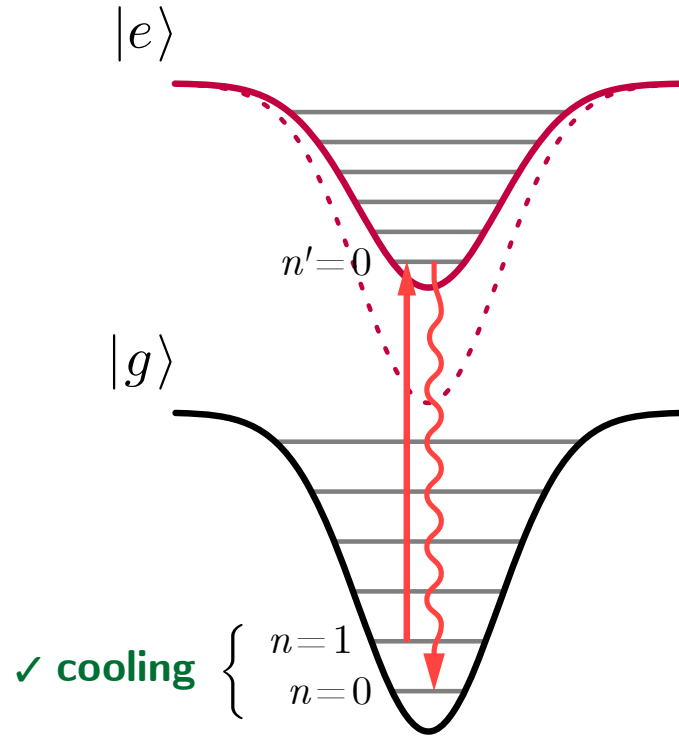
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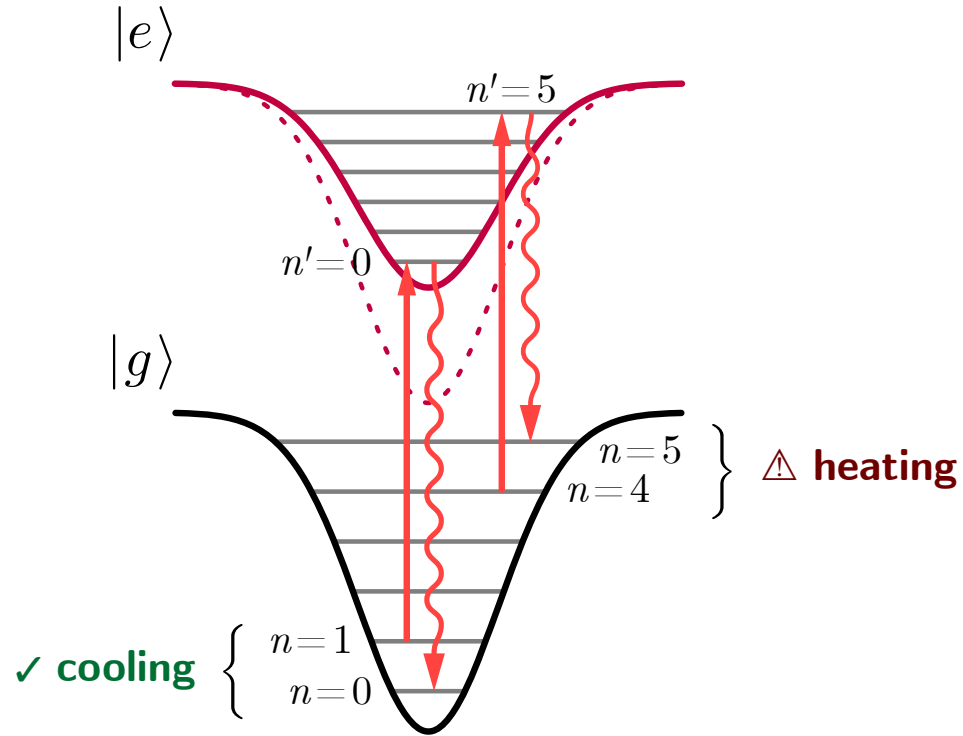
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- In-situ fluorescence imaging : *quantum gas microscopes* $\rightarrow \langle \mathbf{n}(\vec{r}) \mathbf{n}(\vec{r}') \rangle$









1. Oven $\rightarrow$ atomic beam
2. Transverse cooling
3. Zeeman slower
4. Blue MOT (~ 1 s for loading 10^8 atoms)
5. Broadened red MOT (~ 0.1 s)
6. Narrow-line red MOT (~ 0.1 s)
7. Loading of the transport trap
8. Transport (2 s)
9. Red molasses for post-transport cooling (~ 0.5 s)
10. Transfer transport trap $\rightarrow$ evaporation trap
11. Evaporative cooling ($1 \sim 4$ s ?) $\rightarrow$ 3D BEC
12. Loading a single plane of the vertical lattice $\rightarrow$ 2D “BEC”
13. Ramping-up of the horizontal lattices $\rightarrow$ 2D Bose-Hubbard
14. **Physics !** (quench...)
15. Pinning; Microscopy imaging ($1 \sim 2$ s ?)

